



Towards Industrial LES/DNS in Aeronautics Paving the Way for Future Accurate CFD

Vincent Couaillier, ONERA, CFD Department, Châtillon, France Charles Hirsch, NUMECA, Brussels, Belgium Werner Haase, Aeronautics Consultant, Neubiberg, Germany

CEAA 2016, Svetlogorsk, 21- 23 September 2016



Outline

- Short description of TILDA project
- Results overview of TILDA project partners at mid-term
- Highlight of some results regarding DG methods for turbulent flow computation



Objectives TILDA

- The main goal of the TILDA project is
 - to combine efficient high-order numerical schemes (HOMs) and innovative LES and DNS techniques in order to solve complex flow configurations at industrial operational conditions.
 - Obtaining high resolution LES/DNS at the industrial levels (TRL 5-6), reducing the need for experiments and increasing further the predictive capacity of CFD simulations in the full design envelope
- The project aims at performing high-order computations of complex LES/DNS cases:
 - Fully exploiting HPC advancements running on many tens of thousands of processors in a turn-around times of a 1-2 days.
 - Exploiting HOM to reach billions of degrees-of-freedom (DOF) on reasonable grids sizes.





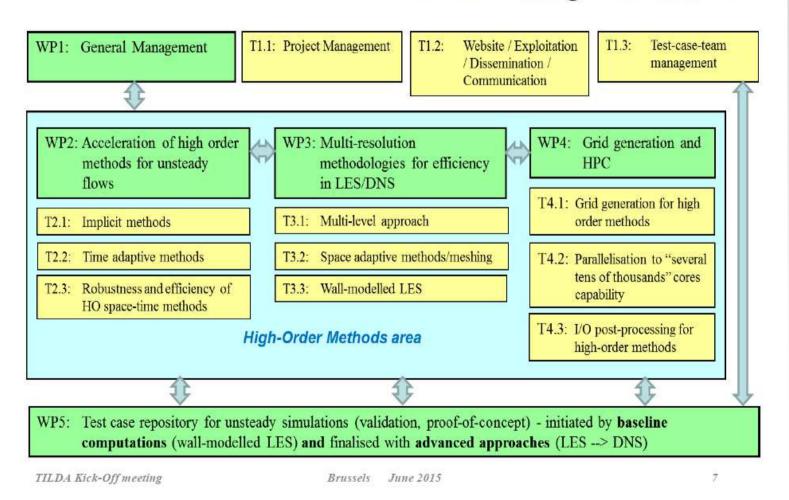
List of Partners

No	Name	Short Name	Country
1	NUMERICAL MECHANICS APPLICATIONS INTERNATIONAL SA	NUMECA	Belgium
2	DEUTSCHES ZENTRUM FUER LUFT - UND RAUMFAHRT EV	DLR	Germany
3	OFFICE NATIONAL D'ETUDES ET DE RECHERCHES AEROSPATIALES	ONERA	France
4	DASSAULT AVIATION SA	DASSAV	France
5	SAFRAN	SAFRAN	France
6	CENTRE EUROPEEN DE RECHERCHE ET DE FORMATION AVANCEE EN CALCUL SCIENTIFIQUE	CERFACS	France
7	CENTRE DE RECHERCHEEN AERONAUTIQUE ASBL - CENAERO	CENAERO	Belgium
8	UNIVERSITE CATHOLIQUE DE LOUVAIN	UCL	Belgium
9	UNIVERSITA' DEGLI STUDI DI BERGAMO	UNIBG	Italy
10	IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE	ICL	United Kingdom
11	FEDERAL STATE UNITARY ENTERPRISE THE CENTRAL AEROHYDRODYNAMIC INSTITUTE NAMED AFTER PROF. N.E. ZHUKOVSKY	TsAGI	Russian Federation





Work Packages Overview





Validation/ve	Proof-of-concept TC		
351 31		1	
TC-F1: Periodic Hill Re _H =10600 LES 13x10 ⁶ points Re _H =10600/19000/37000 (Exp.)	TC-F2: Taylor-Green vortex Re=1600 (DNS) Re=5000 (LES)	TC-F3: Shock boundary layer interaction on swept bump Ma=0.75 Re=1.13 10 ⁶	TC-P1: Jet with/without micro-jets – fluidic injection Ma=0.9 Re=10 ⁶
Justification for Test Case: RANS isn't able to deliver decent results	Case:	Justification for Test Case: Fundamental geometry but complex physics due to shock stability/position	Justification for Test Case: RANS can't compute turbulence effects at all
Quantifiable Objective ² : 1 day on e.g. 50,000 cores	Quantifiable Objective ² :	2-3 days on e.g. 50,000	Quantifiable Objective ² : 2-3 days on e.g. 50,000 cores
[10] [10] [10] [10] [10] [10] [10] [10]		Area of Impact: Wing / turbomachinery	Area of Impact: Aero-acoustics
Test-case Team¹: CENAERO, DLR, UCL, ONERA, CERFACS,	Test-case Team¹: DLR, CENAERO, ONERA, CERFACS, UCL, TsAGI, UNIBG, NUMECA, DASSAV	Test-case Team ¹ : ONERA, CERFACS, UCL, CENAERO, TsAGI,	[142] 이렇게 하다 하나 있다면 하면 하면 하나 있습니다. 그 사는 그 사는 사고를 보고 있었다면 하다 하나 하다.



Proof-of-concept = industrial demonstrator test cases, cont.				
			*	
Falcon business jet	TC-P3: T106C high-lift Cascade Ma-in=0.28 Ma-out= 0.59 Outflow: Re= 80,000 – 150,000	TC-P4: Noise suppressing nozzle with chevrons Npr=2.8; Schlieren & Laser sheet; PIV: Velocity & fluctuations; Noise: 1/3 octavo meas.	TC-P5: Boeing Rudimentary Landing Gear ³ U=40m/s (M≈0.12) Re=UD/v≈10 ⁶	TC-P6: NASA Rotor 37 36 multiple-circular- arc blade Tip Speed= 1500ft/sec Pressure ratio =2.106
Justification for TC: Application challenge full aircraft	Justification for TC: DNS and LES of natural and bypass transition in flight condition	Justification for TC: Environmental aspect, noise suppressing nozzle	Justification for TC: Landing Gear is a major noise source	Justification for TC: Difficult to predict near-stall performance
Quantifiable Objective ² : 2-3 days on e.g. 50,000 cores Area of Impact:	Quantifiable Objective ² : 0.5 day on e.g. 50,000 cores Area of Impact:	Quantifiable Objective ² : 1 day on e.g. 50,000 cores Area of Impact:	Quantifiable Objective ² : 2-3 days on e.g. 50,000 cores Area of Impact:	Quantifiable Objective ² : 2-3 days on e.g. 50,000 cores Area of Impact:
Area of Impact: Aeroacoustics, external aerodynamics	Jet engines, turbo- machinery	Aeroacoustics; nozzle/jet flow	Aeroacoustics; external aerodynamics	Turbomachinery; internal aerodynamics
Test-case Team ¹ : DASSAV, UCL, NUMECA	Test-case Team ¹ : CENAERO, UCL, ICL, ONERA, SAFRAN, NUMECA	Test-case Team ¹ : TsAGI, ICL, UCL	Test-case Team ¹ : DLR, ONERA, ICL, UNIBG, UCL, DASSAV	



TILDA approach for numerical methods

Various HO finite element type methods

- Discontinuous Galerkin methods : U. Bergamo, ONERA, DLR, TsAGI, CENAERO,
 U. C. Louvain, SAFRAN
- Spectral Difference methods : CERFACS
- Flux Reconstruction schemes : IMPERIAL COLLEGE, NUMECA
- Continuous Finite Element methods: DASSAULT Aviation

<u>All these methods use unstructured meshes</u>, either purely tetrahedral meshes or hybrid element types

Comparison with reference FV methods (2nd order but also HO FV methods) are made within the context of the HO CFD workshop and with classical codes used for current applications



Under the TILDA framework, NUMECA is working on the development of an unstructured high-order solver based on Flux Reconstruction (FR) schemes, within the software FINE/OpenTM. The state-of-the-art is an explicit Navier-Stokes solver on unstructured grids composed of every cell shapes (Hexas, Tetras, Prims, Pyrams).

- 1. Work Package 2.1: Various efforts have been undertaken to improve the efficiency of the explicit FR solver,
- BLAS libraries are used in order to boost efficiency in mat-mat operations present in the solver.
- The data structure of solver has been enhanced in order to reduce memory footprint.
 - > On average a 30% reduction of memory is observed for all polynomial orders "p".
- A Tensor product FR formulation has been developed, more efficient and available on Hexa cells.

Ratio time optim.	FineFR_p1	FineFR_p3	FineFR_p5
FR-BLAS solver	x1.09	x1.47	x1.72
FR-Tensor solver	x1.02	x1.85	x4.35

Results on time performance of the Navier-Stokes FR solver: Ratio of times per iteration, of the optimised versions of the solver with respect to the old version prior to optimisation work. Results are obtained in a mesh of 48x48x48 cells.

- 2. **Work Package 3.1:** The extension of the FR solver to handle non-conforming meshes, both in h- and p- senses, is ongoing. This is the first step of an implementation of a MultiLevel approach for under-resolved computations.
- The approach chosen to handle the coupling of non-conforming elements is the so-called "Mortar Element", proposed by Kopriva and Kolias in (Kopriva & Kolias, 1996), (Kopriva, 1996).

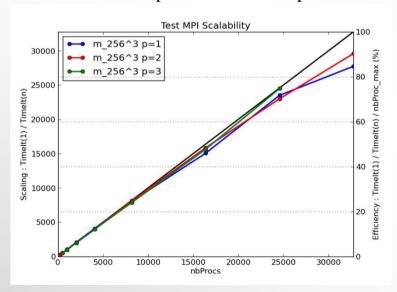




- 3. Work Package 4.2: The parallel scalability of the FR solver has been enhanced.
- Thanks to the design of MPI communicators tailored for high-order methods.

Parallel scalability tests of the FR solver on massive platforms have been conducted. Some specifications are:

- Computation domain is a cube of 256x256x256 cells.
- Only kernels of the "raw" algorithm of the FR solver are measured. Other kernels for pre- or post-processing (solution output, monitor of residuals, ...) are not accounted for.
- Test conducted in the supercomputer Titan.
- Main conclusion: optimal parallel scalability of the FR solver is observed up to ~36000 cores. The next step is the optimisation of kernels for solution output with the aid of parallel I/O libraries.





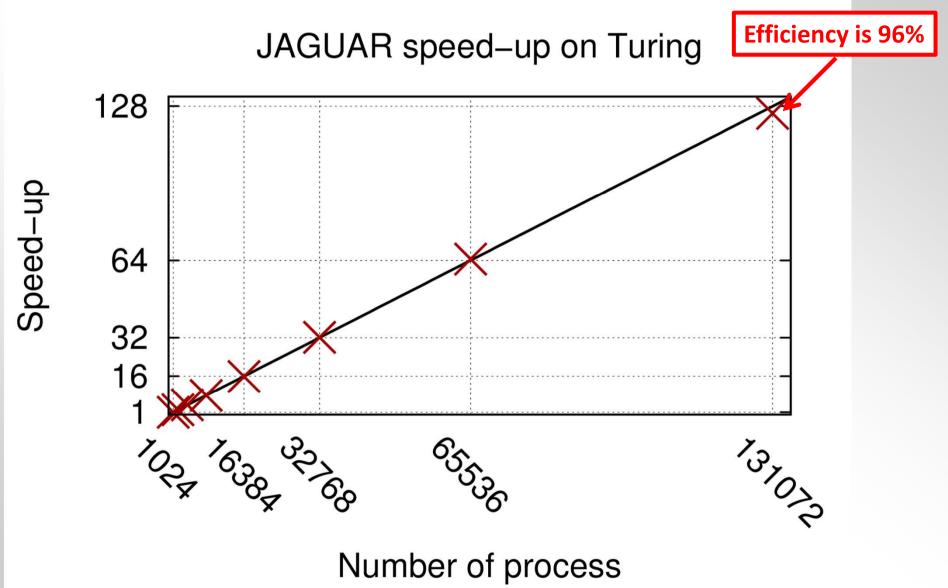
Results on parallel scalability of the laminar FR solver, up to polynomial order p=3 and nbcores =~36000 cores.



- CERFACS aims to use its Spectral Difference solver JAGUAR for massively parallel computations with focus on aeroacoustics with:
 - h/p adaptation (space and polynomial degree)
 - dedicated boundary conditions
 - co-treatment for processing data on the fly
- HPC capability still drives the developments of the Kernel:
 MPI, OpenMP, Hybrid MPI/OpenMP
- Current efficiency shown on the IBM BlueGene/Q at IDRIS
 - Reference test case: 2 097 152 cells, p=4, 262 144 000 DoF
 - flat MPI, 2 threads/processor
 - Reference for 1024 process











Development and testing of PyFR (under Task 4.2):

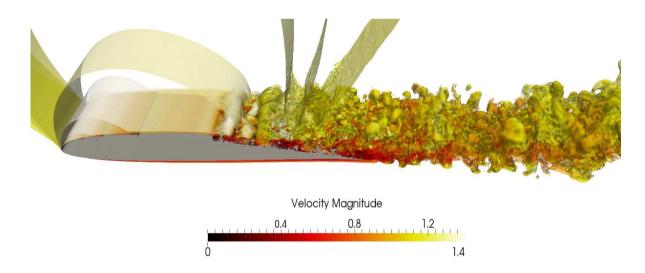
- Cross-platform peta-scale CFD with just 8000 lines of Python!
- Arbitrary order of accuracy in space on mixed element unstructured grids via Flux Reconstruction approach
- Open-source BSD license
- Recent simulations with PyFR on Titan and Piz Daint shortlisted for 2016 Gordon Bell Prize
- Checkout www.pyfr.org





Controlling aliasing driven instabilities (under Task 3.2):

- Aliasing driven instabilities in Flux Reconstruction resulting from, for example, point-wise projection of a non-polynomial flux into a polynomial space, can lead to instabilities
- Investigating de-aliasing strategies to suppress such instabilities
- These include use of new Flux Reconstruction correction functions that are provably stable for 1D linear problems
- Also investigating role of temporal discretisation errors





DLR: Proposed work within TILDA

- Work on efficiency / cost reduction for Scale-resolving simulations
 - Temporal discretization
 - Implicit time integration schemes (WP 2.1)
 - Spatial discretization
 - adaptive mesh refinement with hanging nodes near solid walls for wall-resolved LES (WP 3.2)
 - wall functions for wall-modelled LES (WP 3.3)
 - Parallelization (WP 4.2)
- Management of test cases and tasks
 - TC-F2 (Taylor Green vortex)
 - TC-P5 (Boeing Rudimantary Landing Gear)
 - WP 2.1 (Implicit Methods)
 - WP 3.2 (Space adaptive methods/meshing)

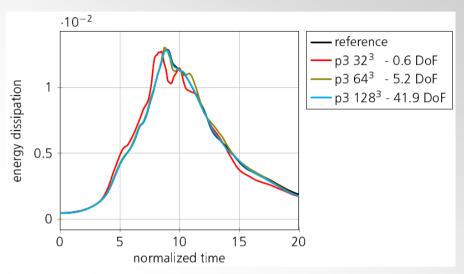




DLR: Implicit time integration schemes (WP 2.1)

Taylor Green Vortex

Taylor Green Vortex at Re=1600 DG, p=3 on 64³ mesh



Scheme	Time step size	Run time	Note
ERK4	0.001	1.0	reference
SDIRK-4	0.1	20.1	Baseline
		0.4	freeze for Jacobian for 2 time steps, nonlinear tolerance 10 ⁻⁴

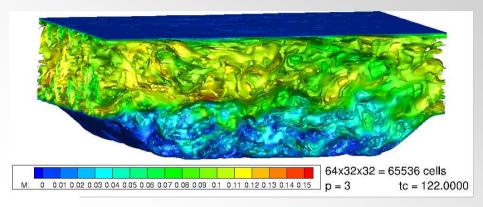


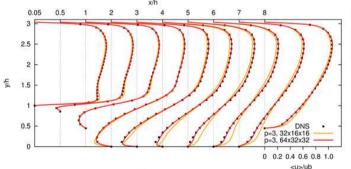


DLR: Near-wall local mesh refinement (WP 3.2)

Periodic Hill test case (Re=2800)

DG discretization Global p-adaptation Quadratic mesh (64x32x32 elem.)





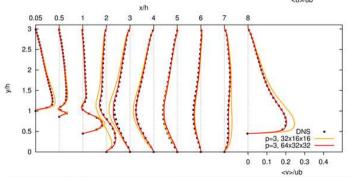
p=3 (4th order)

	# cells	DoFs/eqn
coarse	32x16x16	1.64e5
fine	64x32x32	1.31e6

Ongoing work:

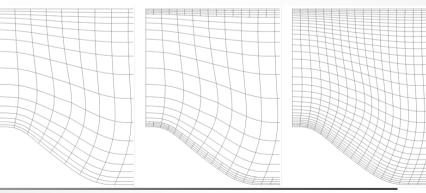
Comparison of solutions

- on globally refined meshes, and
- on near-wall locally refined meshes



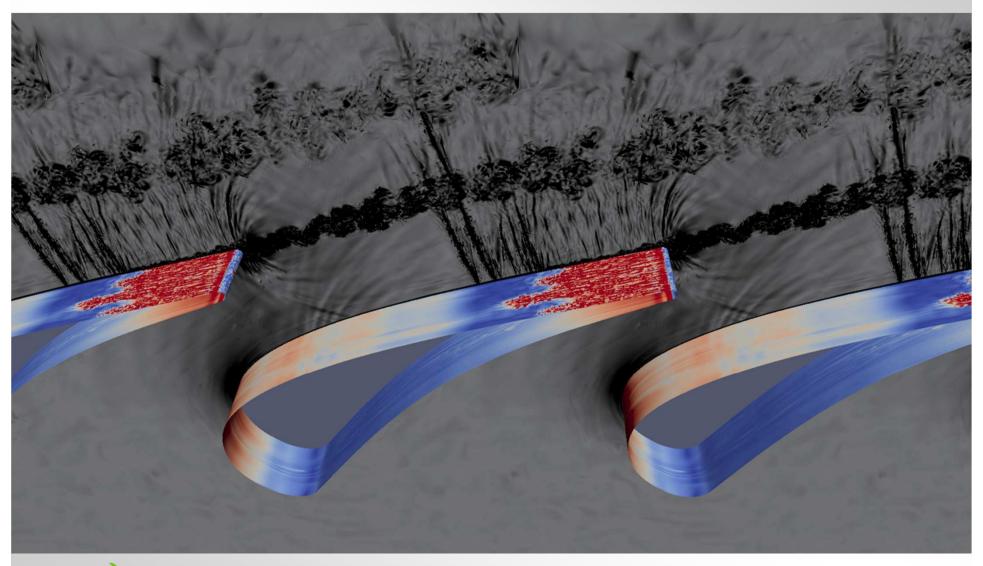
Velocities averaged over the convective time units:

tc = 102 - 122 (mass-weighted averages)



Validation ILES on LS89

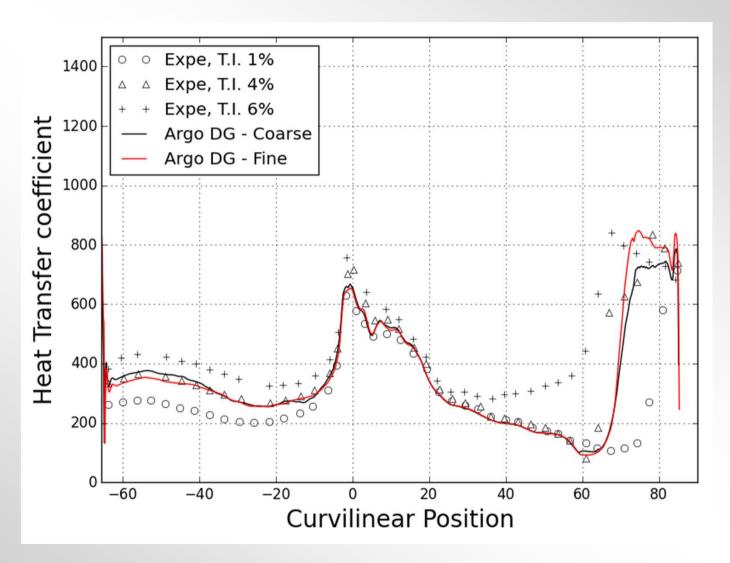






Validation DGM/ILES on LS89







DGM/Wall Modeled ILES - calibration/validation



Apples project / PhD A. Frère

Calibration channel flow Re_{τ} =5.200, 50.000 (prep. IJNMF)

- parametric and physical location of intercept
- order dependence
- normal aspect ratio
- tangential aspect ratio
- grid type



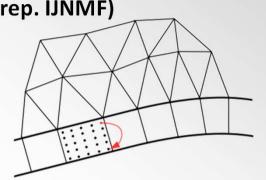
- local / instantaneous (convergence, homogeneity)
- 'lower' orders of interpolation 3 -> 5
- elements on processor parallel scaling

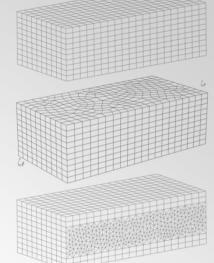
Conclusions

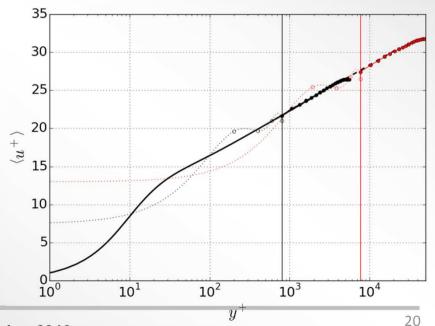
- high order P >= 4 required near wall
- grid type / tangential wall aspect ratio insensitive
- log layer intercept required
- erratic behavior in first cell ...
- ... but very good correspondence later on
- instantaneous and local (<-> averaging) sufficient

Future work

- non-equilibrium models (1D RANS normal to the wall)
- transition criteria



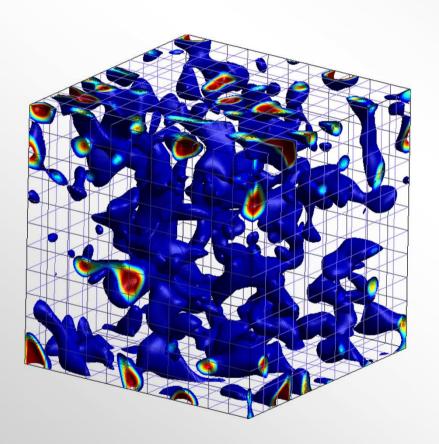


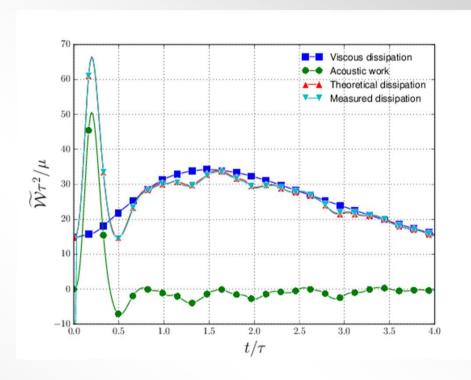




DGM/ILES transonic HIT – Energy balance (CTR)





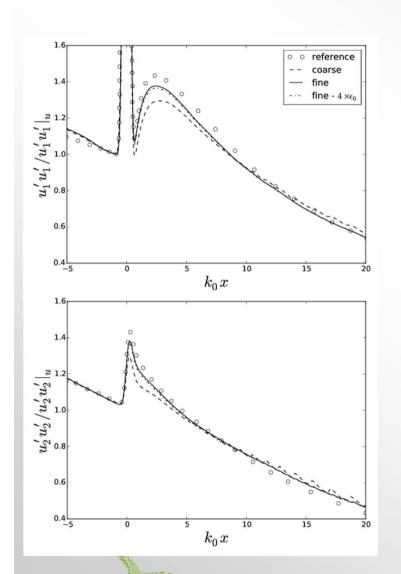


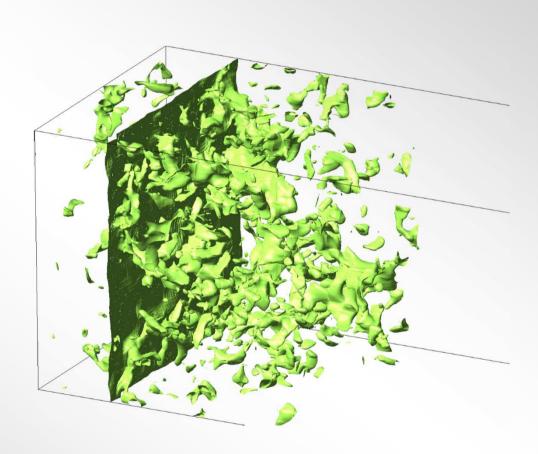
 $M_t = 0.6$, $Re_{\lambda} = 100$, 64^3



DGM/ILES of shock-turbulence interaction (CTR)







M=1.5, $M_t=0.22$, $Re_{\lambda}=100$, 64^2



Description of Dassault Aviation CFD code AeTher



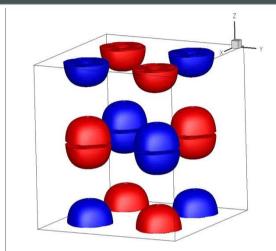
in-house compressible Navier-Stokes solver

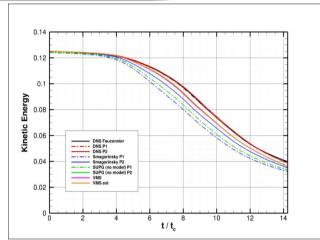
- stabilized continuous Finite Elements formulation
 - SUPG: Streamline-upwind Petrov Galerkin
- symmetric form of the equations written in terms of entropy variables
- up to 4th-order with P3 tetrahedra
- fully implicit time integration
- highly scalable: strong scalability demonstrated up to 16,384 MPI processes

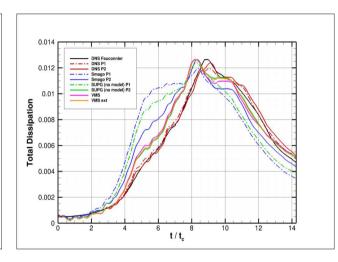


TC-F2: Taylor-Green vortex







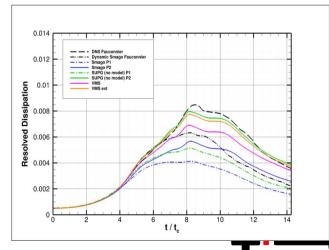


- DNS: 256³, Re=1500
- LES: 64³ (64x coarser)

D. Fauconnier

Development of a Dynamic Finite Difference Method for Large-Eddy Simulation

Ph.D. Thesis, Universiteit Gent, 2008



24 CEEA 2016 – Svetlogorsk – Sept 21-24, 2016

Higher-order LES

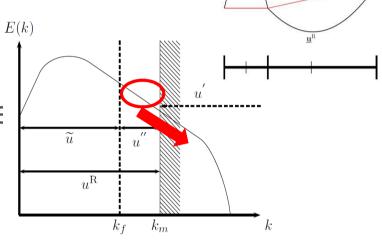


Multi-level approach

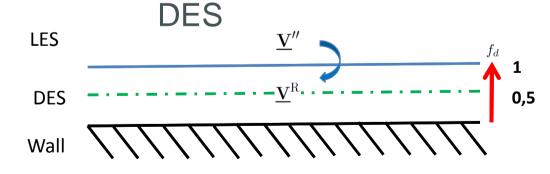
• VMS with explicit filtering at the element level

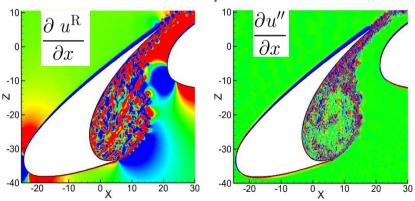
Wall-modeled LES

hybrid approach: VMS-based



efficient separation of scales

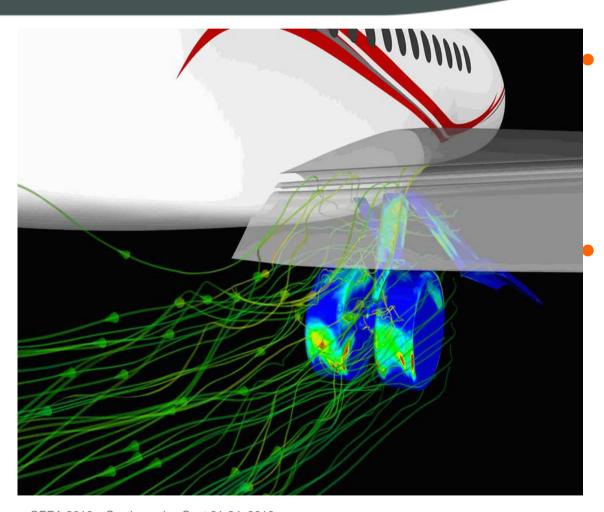






Future work: TC-P2 Generic Falcon business jet in landing configuration





complete **Falcon**

- high-lift devices
- landing gear
- expected turnaround time
- 2-3 days on 50,000 cores





UNIBG's main tasks within TILDA

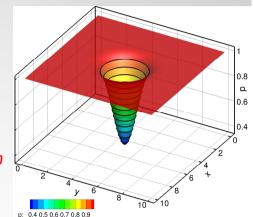
- To apply implicit time integrators to the under-resolved simulation of turbulence
- To take advantage of h/p-adaptation and modern parallel computer architectures

To date Several high-order temporal schemes are implemented

- Modified Extended BDF
- Two Implicit Advanced Step-point (TIAS)
- Explicit Singly Diagonally Implicit R-K (ESDIRK)
- linearly implicit Rosenbrock method

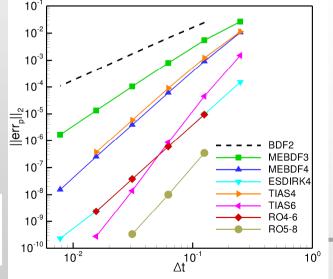
non-linear systems solution

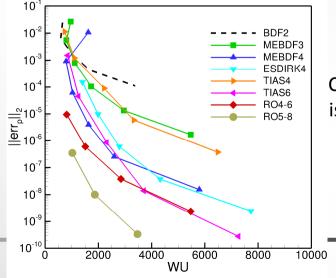
linear systems solution (here via GMRES)



i) Hi-O schemes are more efficient than Lo-O ones for high required accuracy

ii) Rosenbrock-type schemes are appealing both for accuracy and efficiency





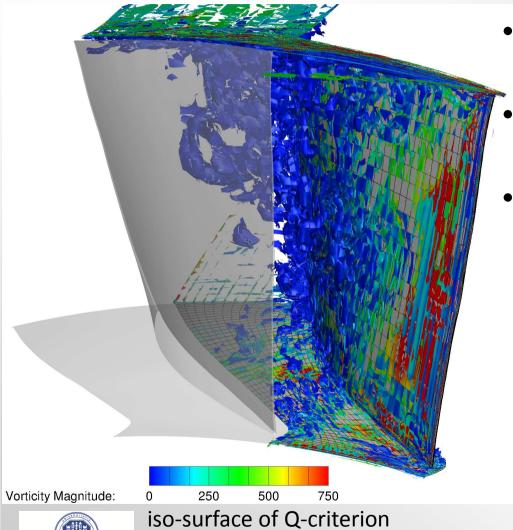
Convection of an isentropic vortex P⁶ solution on 50x50 el.

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X-LES (hybrid RANS\LES) of the transonic flow in the NASA Rotor 37



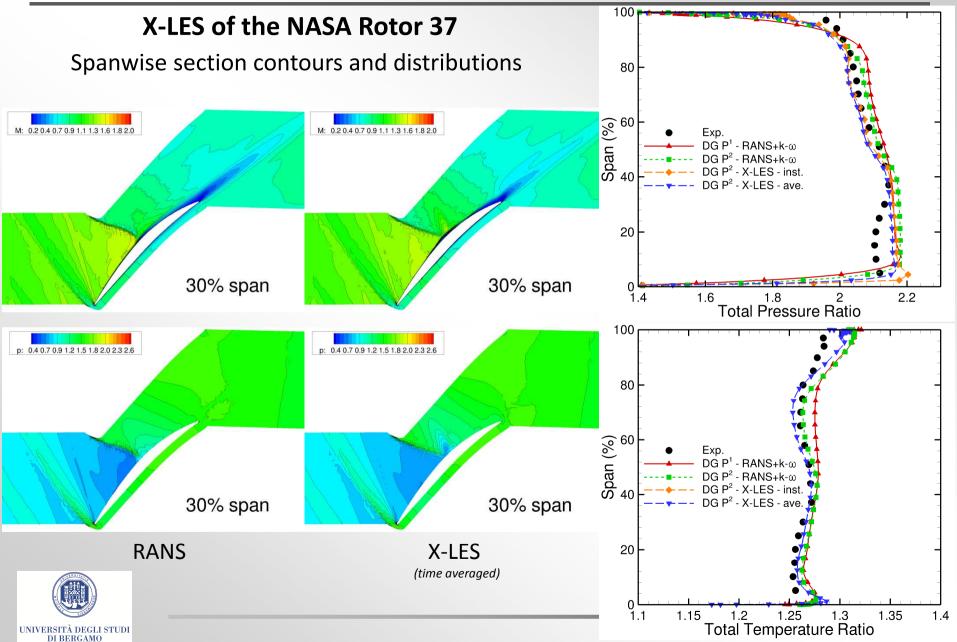
- P² DG computation using a 3rd order 3 stages Rosenbrock scheme (ROS3P)
 - 160512 hexahedral elements with quadratic edges
- Boundary conditions
 - $p_{01} = 101325Pa$
 - $T_{01} = 288K$
 - $\omega = 1800 \text{ rad/s}$
 - $Tu_1 = 3\%$
 - $\alpha_1 = 0^{\circ}$

According to our experience, for a practical usage of X-LES, initializing with RANS seems mandatory

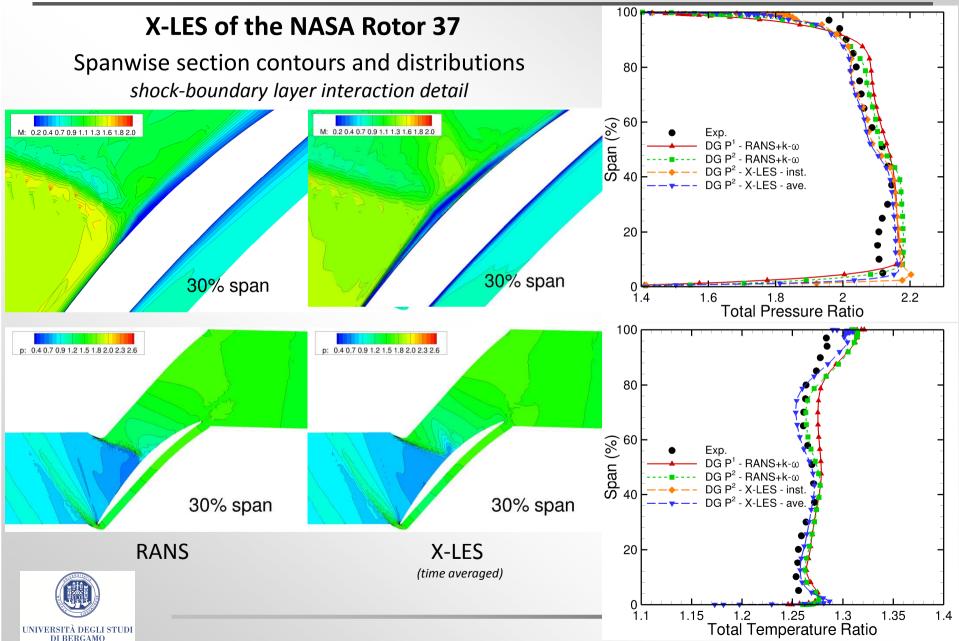
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28







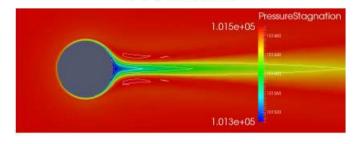




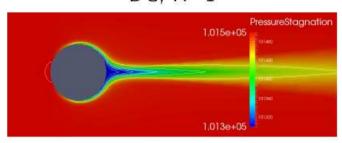
Cylinder. Total pressure flowfield

Grid 128x32x1

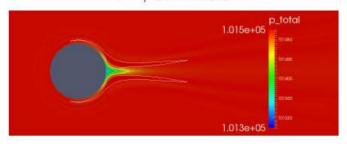
FV, Central



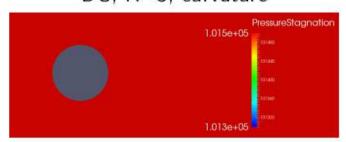
DG, K=1



FV, WENO5



DG, K=3, curvature



TsAGI

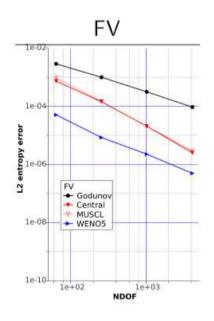
(TsAGI) CEAA, 2016 14 / 26

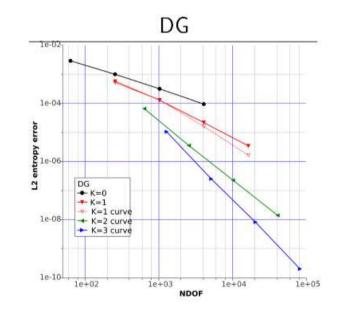


Cylinder. Error of entropy in the L2 norm

$$e_{entropy} = \left(\frac{p}{p_{\infty}}\right) / \left(\frac{\rho}{\rho_{\infty}}\right)^{\kappa} - 1, \qquad Order = 2 \frac{\log\left(e_{i-1} / e_{i}\right)}{\log\left(NDOF_{i} / NDOF_{i-1}\right)}.$$

NDOF = the product of the mesh size and the number of degrees of freedom.





The same result for the drag

TsAGI

(TsAGI) CEAA, 2016 15 / 26



Taylor-Green Vortex. Base TILDA testcase

TsAGI

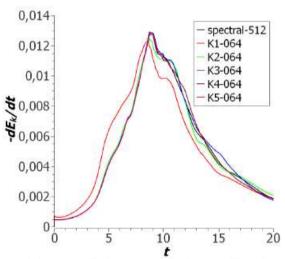
Mandatory results:

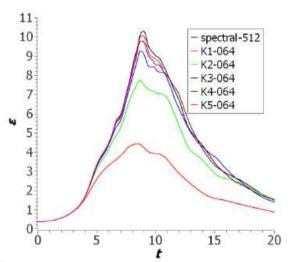
$$E_k = \frac{1}{\rho_0 \Omega} \int\limits_{\Omega} \rho \frac{v \cdot v}{2} d\Omega$$

$$E_k = \frac{1}{\rho_0 \Omega} \int_{\Omega} \rho \frac{e^{i \cdot v}}{2} d\Omega$$



$$\epsilon = \frac{1}{\rho_0 \Omega} \int\limits_{\Omega} \rho \frac{\omega \cdot \omega}{2} d\Omega$$





Comparison with spectral method at fine mesh

W.M. van Rees, A. Leonard, D.I.Pullin and P. Koumoutsakos, A comparison of vortex and pseudo-spectral methods for the simulation of periodic vortical flows at high Reynolds number, J.Comput.Phys., 230(2011), 2794-2805

(TsAGI)

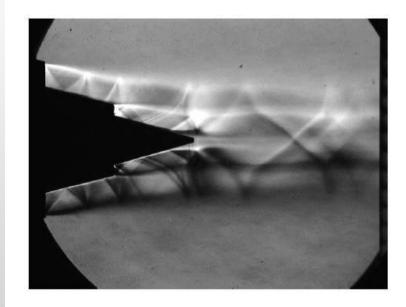
CEAA, 2016

20 / 26

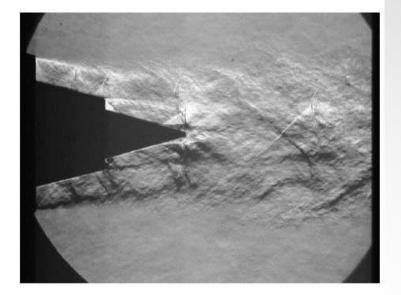


Shlieren-visualization of dual-stream jet. Supersonic uderexpanded jet on inner (1) and outer (2) stream jet

Flow regime - Npr1= 5.0, Npr2=2.8



Exposure equal 0.01 sec



Exposure equal 3 microsec

TsAGI





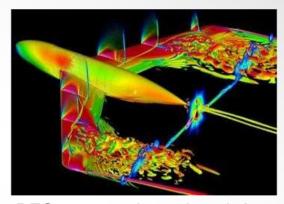
Stakes and prospects in CFD 2020/2030

Progress: 2nd-order CFD based on RANS models mature but ...

- RANS models limited to "nominal" flow configurations
- Mesh convergence analysis show the limitations of classical 2nd-order methods (regularity, resolution, etc.) → improve by means of hp-adaptation
- Accurate imposition of boundary conditions still a problem for sensitive configurations
- Unsteady (LES) computations required for configurations of practical interest

Challenges:

- High-fidelity CFD methods require firstly accuracy
- Level of modeling: Hybrid RANS/LES, LES, DNS
- Accuracy of space-time discretization
- HPC parallelization
- hpm-adaptation for accuracy and efficiency
 - h: mesh refinement
 - p: order of accuracy (polynomial degree)
 - *m* : physical model
- Huge data management for pre-, co-, and post-processing

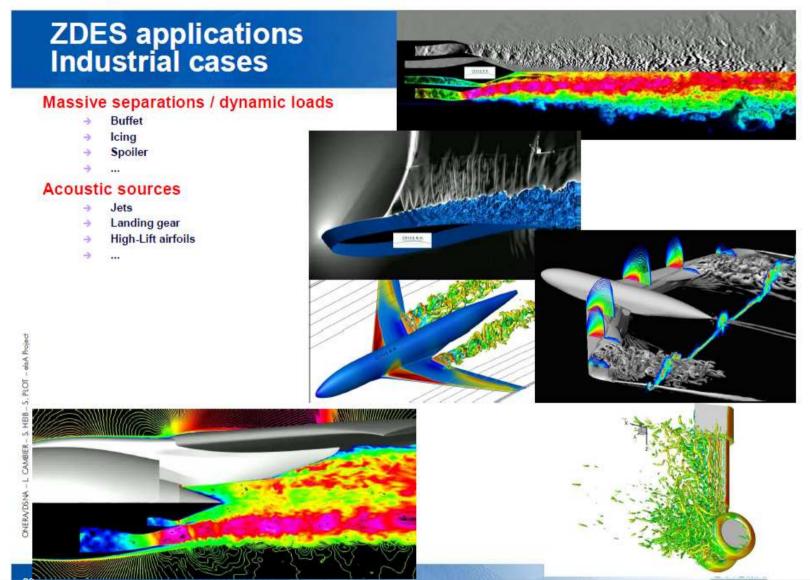


DES computation using elsA





ZDES with elsA







Why high-order DG?

- Arbitrarily high-order of accuracy on unstructured grids
- Low dissipation, dispersion
- Boundary conditions:
 - The order of accuracy of the numerical scheme is conserved at the boundary
 - Possibility to enforce boundary conditions weakly (Collis, 2002)
- Provide local information in physical and spectral space (hp-adaptivity)
- Orthogonal hierarchical basis that supports multiscale turbulence modelling
- Compact schemes \rightarrow ideal for HPC

Cons of high-order DG

- Robustness issues (Runge phenomena at discontinuities)
- Time explicit discretization: (linear scalar advection: Chavent Cockburn '89, Cockburn Shu '91 '01)

$$CFL \leq \frac{1}{2p+1}$$

- High computational cost (volume integral, numerical quadratures, etc.)
- Large memory requirements (large number of DOFs / element)





Aghora: The current status (1/2)

- The full set of compressible Navier-Stokes equations can be solved in 3D
- Modal approach: the degrees of freedom (DoFs) are the coefficients of the polynomial expansion:

$$\mathbf{u}_h(\mathbf{x},t) = \sum_{k=1}^{N_p} \phi^k(\mathbf{x}) \mathbf{U}_j^k$$

- → natural implementation of multiscale turbulence models and p-adaptation.
- Nodal approach (recently implemented, PhD thesis Raphaël Blanchard) → gain in CPU cost
- Multi-element meshes (hexahedra, tetrahedra, prisms)
- Convective fluxes: Lax-Friedrichs, Roe, etc. numerical fluxes across the interfaces.
- Viscous fluxes: Bassi-Rebay 2 (BR2, JCP 1997) scheme or Symmetric Interior Penalty method (SIP)
- Order of the spatial scheme given by the specified polynomial degree
- Shock capturing technique based on entropy production (Guermond et al., 2011)
- Explicit time integration: up to 4th-order Runge-Kutta schemes
- Implicit time integration : several time-integration strategies (Renac et al, JCP 2013)
 - Inexact Newton method : solution of linear system by GMRES + ILU0 preconditioning (with mixed precision algorithms)
 - ESDIRK (Explicit Singly Diagonal Implicit Runge-Kutta)
- CFL evolution from pseudo-transient continuation technique
- Dual-Time stepping technique





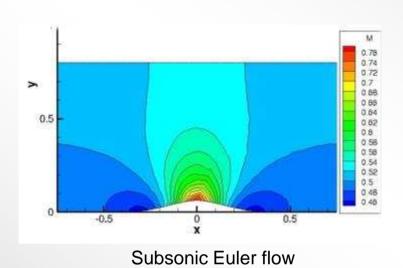
Aghora: The current status (2/2)

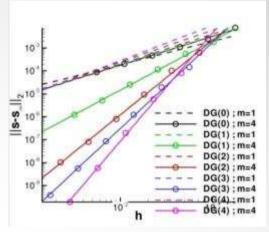
- Economical quadrature rules³ (use element symmetries to reduce number of integration points)
- Shock capturing methods (Hartmann & Houston 2002, Hartmann 2013, Guermond et al. 2011) ppp
- General thermodynamics : $p = p(\rho, \rho e)$ (e.g. stiffened gas, wan der Waals EOS) Turbulence modelling:
- RANS Wilcox $\kappa \omega$ model (Wilcox 1993): $\kappa \omega$ and $\kappa \log(\omega)$ formulations (Bassi et. al 2005, 2009, Hartmann 2012). Spalart-Allmaras model.
- DNS simulations (TGV at Re = 1600, dipole-wall collision problem at Re = 1000, incompressible and 2D periodic hill at $Re_b = 2800$)
- LES simulations: Variational Multiscale Simulation, VMS, and residual-based VMS, RBVMS, (HIT, TGV, channel flow)
- ZDES simulations
- Turbulent injection conditions : SEM (Synthetic Eddy Method)





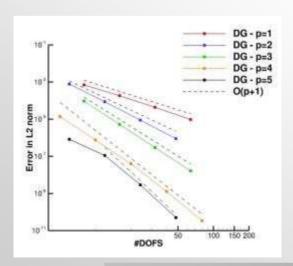
Aghora / DG - Verification of method accuracy : scheme / geometry



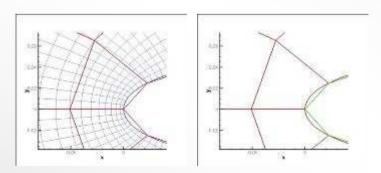


Entropy error vs. Mesh refinement

High-order scheme/geometry for accuracy of HO spectral type schemes (Aghora – HOCFD 2012)

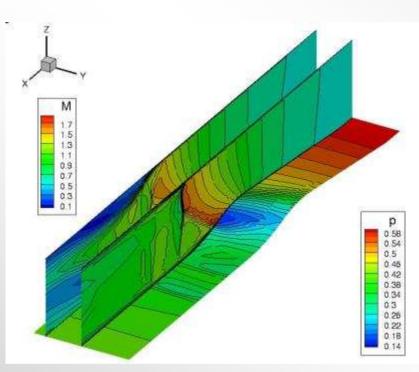


Strong demand on of High-Order meshes



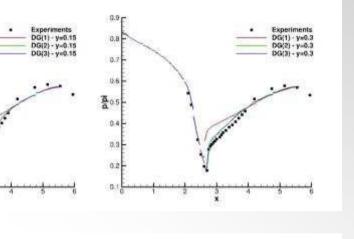


Aghora – Bosse 3D Onera / Calculs DG avec modèle RANS/SA





DG(1) - y=0.9 DG(2) - y=0.9 DG(3) - y=0.9



Implicit method with shock-capturing technique
Accuracy, effiiceny, robustness with HO DG
French GENCI projects 2015-2016
2400 cores using OCCIGEN
F. Renac, Intern. Workshop on High-Order CFD methods
AIAA 2015, ECCOMAS 2016

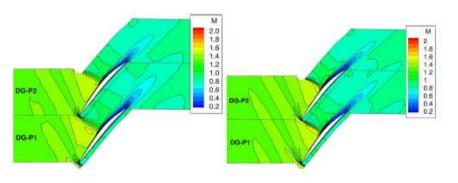


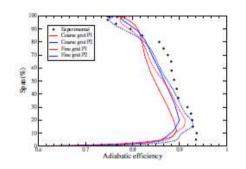




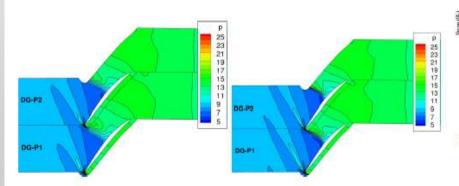
Aghora: NASA ROTOR 37 – DG computations with RANS/SA model

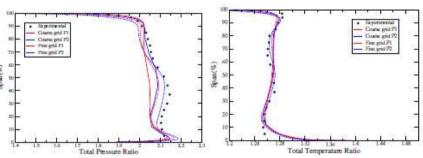
The NASA rotor 37: DG-p1/p2 simulations on hexahedral meshes Coarse mesh with 87,769 points, fine mesh with 672,896 points.





Iso-contours of the Mach number (left: coarse, right: fine).





Spanwise profiles of adiabatic efficiency, total pressure ratio and total temperature ratio.

Iso-contours of the static pressure (left: coarse, right: fine).

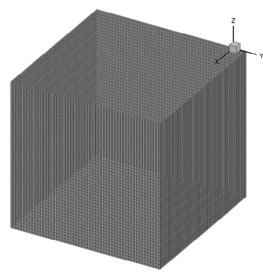




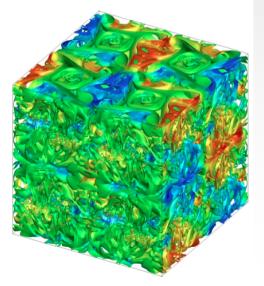
Strong scalability tests

Numerical experiments using the Taylor-Green vortex

- 3D compressible Navier-Stokes equations:
 - DNS of a periodic and transitional flow
 - $M_{\infty} = 0.1$, Re = 1600
 - IC: analytical velocity profile
- Numerics:
 - Explicit time discretization (SSP RK4)







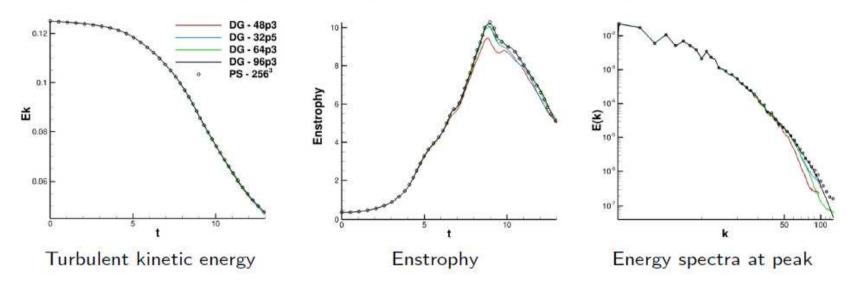
(b) Iso-surfaces of vorticity (t = 14, p = 3)



Taylor-Green Vortex – DNS computations – hp analysis

Decaying turbulence in a periodic box

DG Comp.	DG 48p3	DG 64p3	DG 96p3	DG 32 <i>p</i> 5
Order (p+1)	4	4	4	6
#DoFs / Elements	$192^3 / 48^3$	$256^3/64^3$	$384^3 / 96^3$	$192^3 / 32^3$



o Reference computation : Fourier pseudo-spectral code developed by S. Cant (Cambridge Univ.)









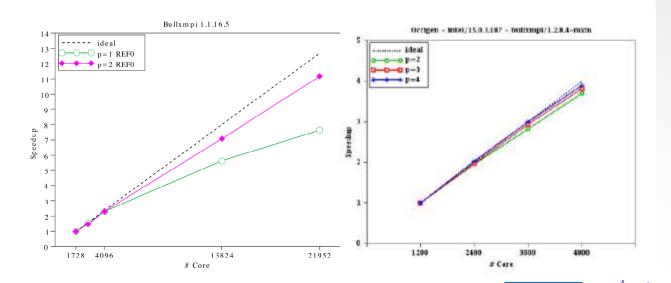
Strong scalability tests

Numerical experiments using the Taylor-Green vortex

• Sensitivity of the polynomial degree p on the speedup with REF0 version on Curie

Strong scalability analysis

- Strong scalability analysis on a mesh with 336 elements
 - ullet Ratio elts/ghosts per domain \sim 4 at the largest scale
- Receive-send message frequency (measured with 13 824 cores)
 - p=1, ~ 41 messages/s
 - p=2, ~ 15 messages/s
 - p = 4, ~ 02 messages/s
- On 21 952 cores with p=2, efficiency of the speedup $\sim 88\%$

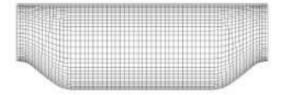


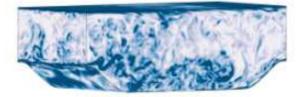
Aghora.

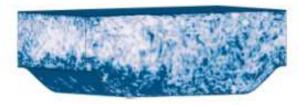




2D periodic hill at $Re_b = 2800$ up to 37 000 : DNS & LES based on WALE approach DG-P3 to DG-P5 on two levels of mesh refinement (0.5 to 4.2 MDOFs)





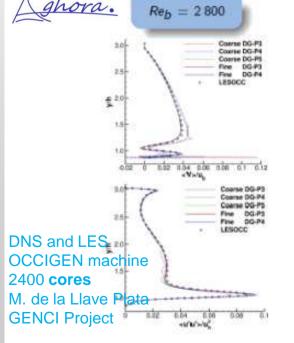


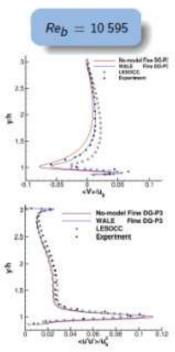
Fine 4th-order mesh $64 \times 32 \times 32$

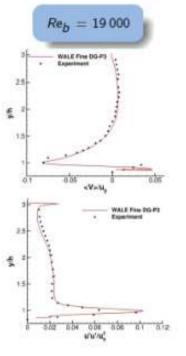
Vorticity magnitude Reb = 2800

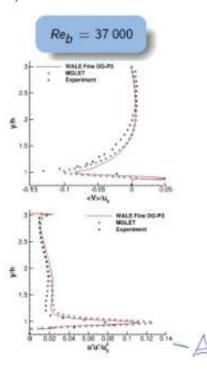
Vorticity magnitude Reh = 10 595

Profiles of mean vertical velocity $\langle V \rangle$ and Reynolds stresses $\langle u'u' \rangle$ at station x=0.5h











Computation synthesis on Periodic hill computations

- DNS at Re_b = 2800 :
 - •h and p convergence analyses highlight the benefit of increasing p rather than reducing h
 - •DG-p5 on coarse mesh (1.77M dofs) in good agreement with reference DNS (13.1M dofs)
 - •Loss of resolution in vicinity of separation point for DG-p3 and DG-p4 coarse mesh simulations → local hp-adaption highly beneficial in marginally resolved areas
- LES at $Re_b = 10,595$:
 - •Solutions from the no-model and the WALE approaches not fundamentally different.
 - •WALE approach → slightly better results near separation point and in recirculation area.

 → smoothing effect on the interface jumps (in particular for <u'u'>)
- WALE-based LES at $Re_b = 19,000$ and $Re_b = 37,000$:
 - •No-model approach does not provide stable simulations at this higher Reynolds number.
 - •Overall good agreement with reference data, main discrepancies near separation point.



AS2 - Transitional flow in the T106C LPT



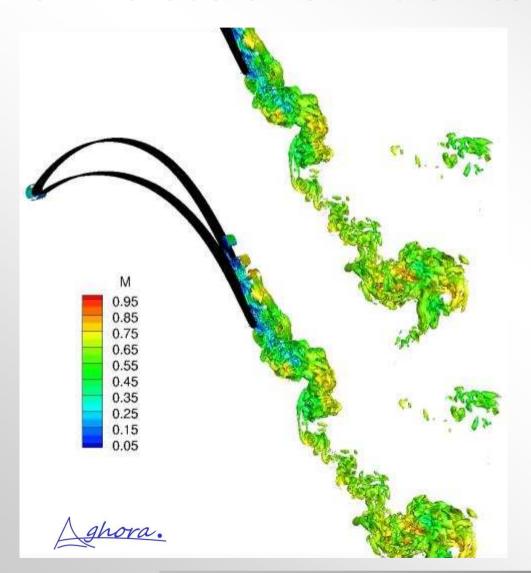
Simulation	# Elements	Order	# MDOFs
DG-P4 Coarse	30,768	5	1.1
DG-P5 Coarse	30,768	6	1.7
DG-P3 Baseline	146,426	4	2.9
DG-P4 Baseline	146,426	5	5.1
DG-P5 Baseline	146,426	6	8.2

DNS and LES OCCIGEN machine 2400 **cores** M. de la Llave Plata GENCI Project

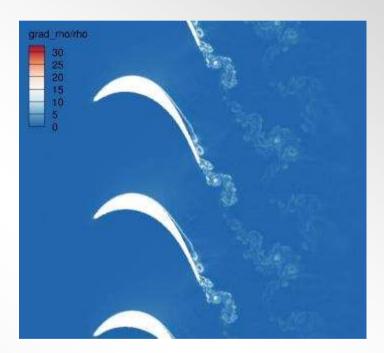
Additional DG-P3 on baseline resolution to study effect of injection angle



AS2 - Transitional flow in the T106C LPT



DG-P3 simulation on baseline grid 2.9 MDOFs



Contours of grad $(\rho)/\rho$





AS2 - Transitional flow in the T106C LPT

Under-resolved DNS simulations & de-aliasing through over-integration p+2 integration points (except for DG-P5 baseline simulation, p+1)

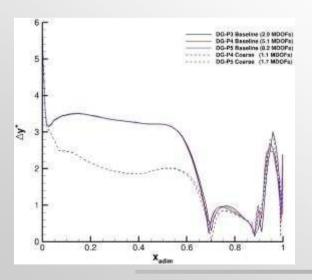
Grid resolution

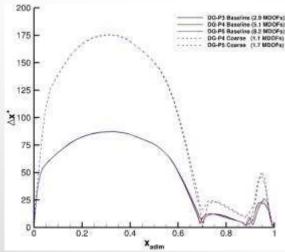
$$\Delta y^{+}_{DG} \approx \Delta y^{+}/(p+1)$$

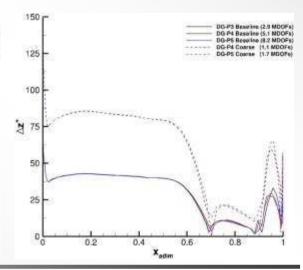
 $\Delta x^{+}_{DG} \approx \Delta x^{+}/(p+1)$
 $\Delta z^{+}_{DG} \approx \Delta z^{+}/(p+1)$

Simulation	Δy ⁺ _{DG}	Δx^{+}_{DG}	Δz^{+}_{DG}
DG-P4 Coarse	0.6	35	16
DG-P5 Coarse	0.5	29	13
DG-P3 Baseline	0.9	20	10
DG-P4 Baseline	0.7	16	8
DG-P5 Baseline	0.6	13	7

Aghora.

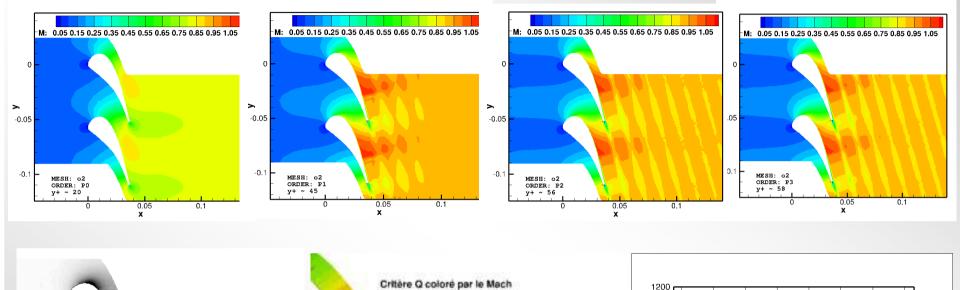


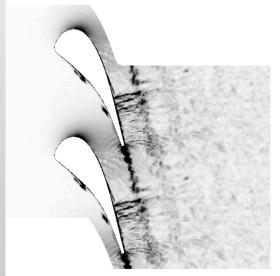


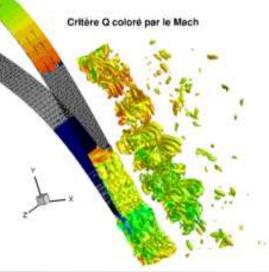


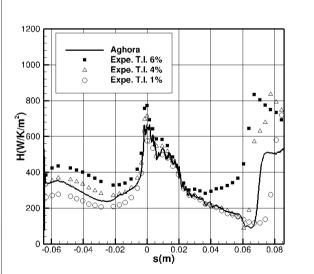










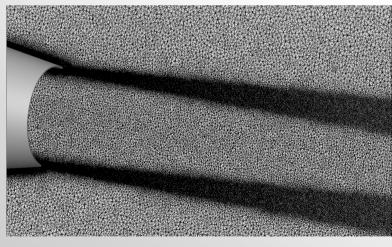




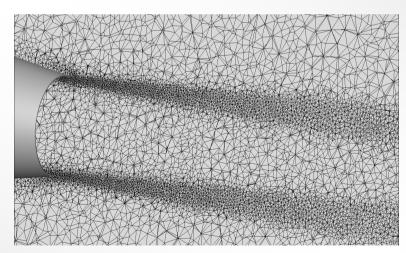
- ☐ Comparison with a reference Finite Volume (FV) solution
 - With mesh grids made from the same mesh file but different resolutions

Grid	Δ/D _j (%)	n _θ	Cut-off (St)	Nb of cells (x10 ⁶)	T.U _j /D _j
CEDRE FV2	0.38	838	1	165	250
Aghora DGp3	2	157	1	3.9	180

At
$$x/D_i = 0$$
 and $r/D_i = 0.5$



CEDRE FV2

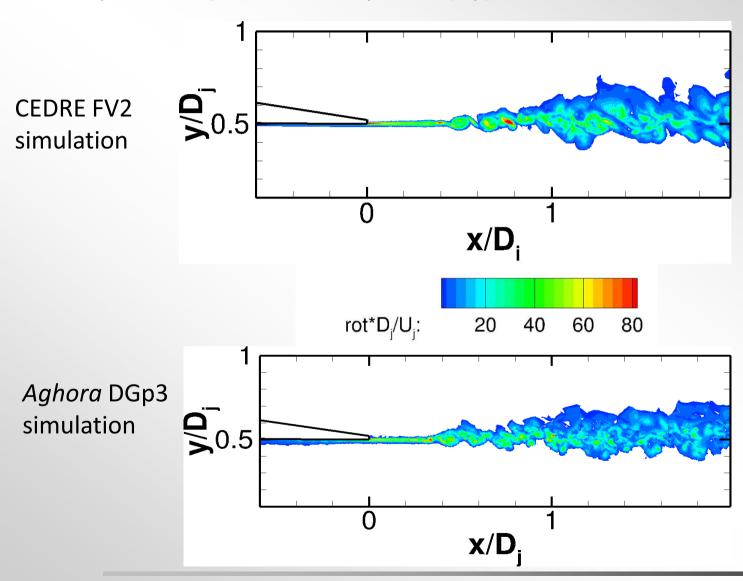


Aghora DGp3





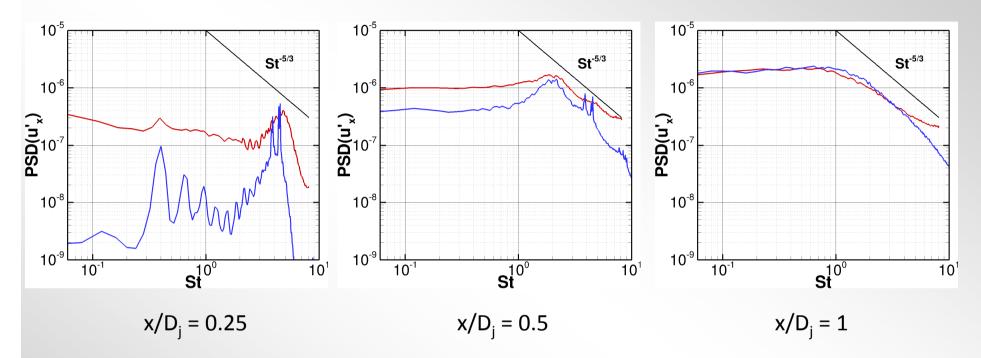
Shear layer development: vorticity norm (x,y)







Shear layer development: velocity spectra (PSD) at r/Dj=0.5



☐ *Aghora* DGp3 simulation:

- Marked peaks visible for $x/D_i \le 0.5$
- Flat spectra for $x/D_i \ge 1$
- => turbulent state reached sooner than the FV2 one

Aghora simulation
CEDRE simulation



Some concluding remarks:

- All HO finite element methods (DG, CFE, FR, SD) computations are able to reproduce the Reynolds-number dependent features of the flow (length of recirculation region, profiles of wall-shear stress and mean pressure distribution).
- Further LES computations require local h and/or p refinement with "spectral type" methods
- HO spectral type methods complementary to classical FV methods (2nd order and HO)
- Use of a hybrid openMP/MPI, GPU/heterogeneous strategy necessary to reduce CPU time for configurations using very coarse meshes in combination with high polynomial degrees.
- Need to implement efficient and accurate post-processing technique
 - Efficient parallel co-processing on HPC architectures
 - Accuracy: remove the unphysical high-frequency due to jumps for marginally resolved simulations
- TILDA organize an open HO CFD workshop: 21-23 November 2016 in Toulouse (Cerfacs)
 https://www.eventbrite.co.uk/e/tilda-symposium-workshop-on-industrial-les-dns-registration-19871723861
- HO methods lead to closer research between CFD and CAA communities for High Accuracy fine turbulence prediction
- HO spectral type methods complementary to classical FV methods (2nd order and HO)



Outline