

Large Scale Motion in a Dual Stream Jet

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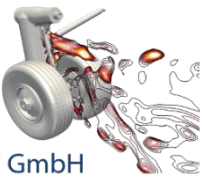
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Simulation of a dual stream jet

Computational Experiment on the noise sources in a dual stream jet

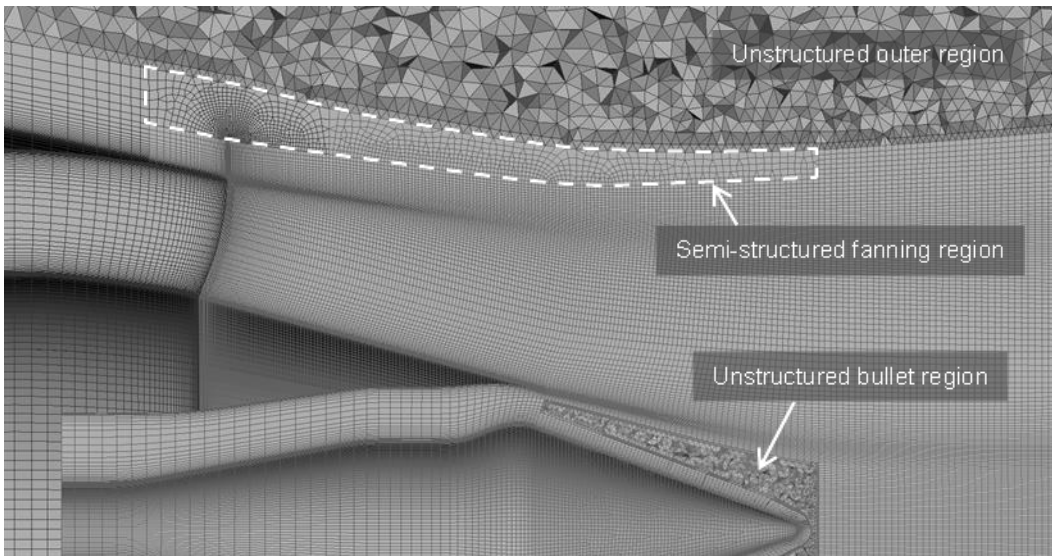
- Hybrid RANS-LES (DES) with recent developments concerning treatment of grey area problem (Mockett et al 2016)
- Simulation performed with a time step corresponding to a sampling Strouhal number $f_s D_e / U_e = 1035$.
- All source-relevant flow quantities stored every 32nd time step for later source analysis. Maximum Strouhal number of analysis = 16.
- Simulation was run over 186 convective time units D_e / U_e .
- Data stored on 4 TB hard drive for later source analysis



Grid

- The grid consists of around 28.5 million cells, with 160 cells applied in the azimuthal direction
- Hybrid structured-unstructured grid. Structured meshing inside the jet plume region coupled with unstructured meshing elsewhere

- Detail of grid in vicinity of nozzle (Mockett et al. 2016)



Sources of jet noise

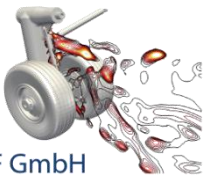
- Convective Lighthill equation to account for the flight stream

$$\frac{1}{a_0^2} \left(\frac{\partial}{\partial t} + U_i \frac{\partial}{\partial x_i} \right)^2 p - \frac{\partial^2 p}{\partial x_i^2} = q$$

- Source

$$q = \frac{\partial^2}{\partial x_i \partial x_j} (\rho u_i u_j - \tau_{ij}) - \left(\frac{\partial}{\partial t} + U_i \frac{\partial}{\partial x_i} \right)^2 \left(\rho - \frac{p}{a_0^2} \right) \quad u_i = v_i - U_i$$

- **Quadrupole** radiation to acoustic far field requires storage of three velocities u_i .
- **Dipole** radiation to acoustic far field requires storage of three density gradients
- Pressure stored in addition



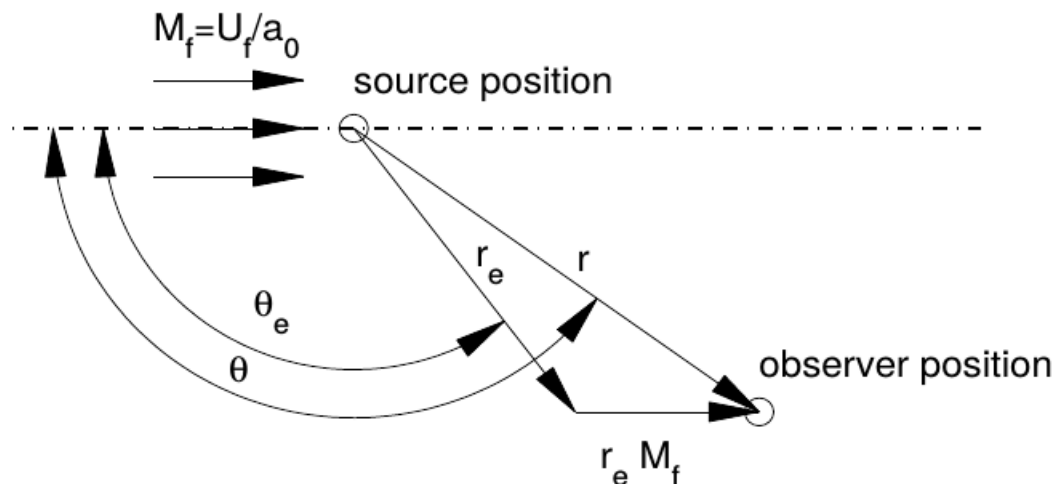
Pressure as source variable

- Solution of convective Lighthill equation for an unbounded field

$$p'(x_i, t) = \frac{1}{4\pi} \int_V \frac{q(x_i, y_i, t_r)}{r_e D_f} dV(y_i)$$

Doppler factor
 $D_f = 1 - M_f \cos \theta_e$

- **Valid everywhere, including the source region**
- Integral finite for $r_e \rightarrow 0$ ($x_i \rightarrow y_i$)
- p' describes influence of q in vicinity of source position y_i .



r_e is emission distance

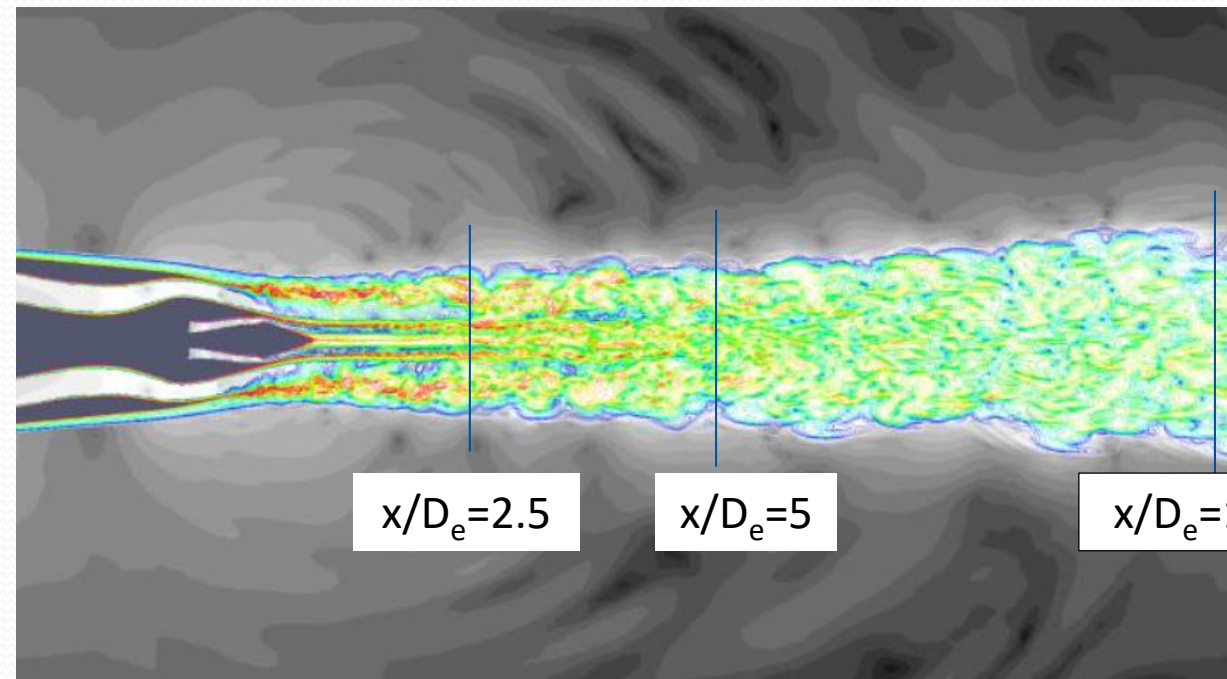
θ_e is emission angle



Unsteady pressure in jet

Unsteady pressure is related to sources

Pressure field studied at $x/D_e = 2.5, 5, 10, 20$



Snapshot of simulation with locations of source analysis

$x/D_e = 2.5$

$x/D_e = 5$

$x/D_e = 10$

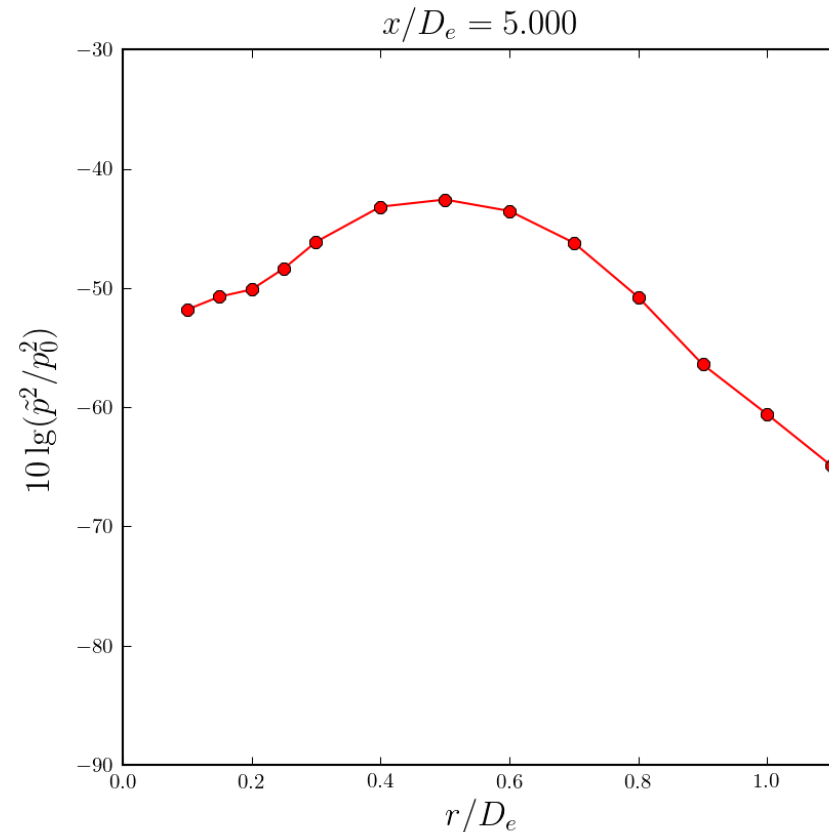
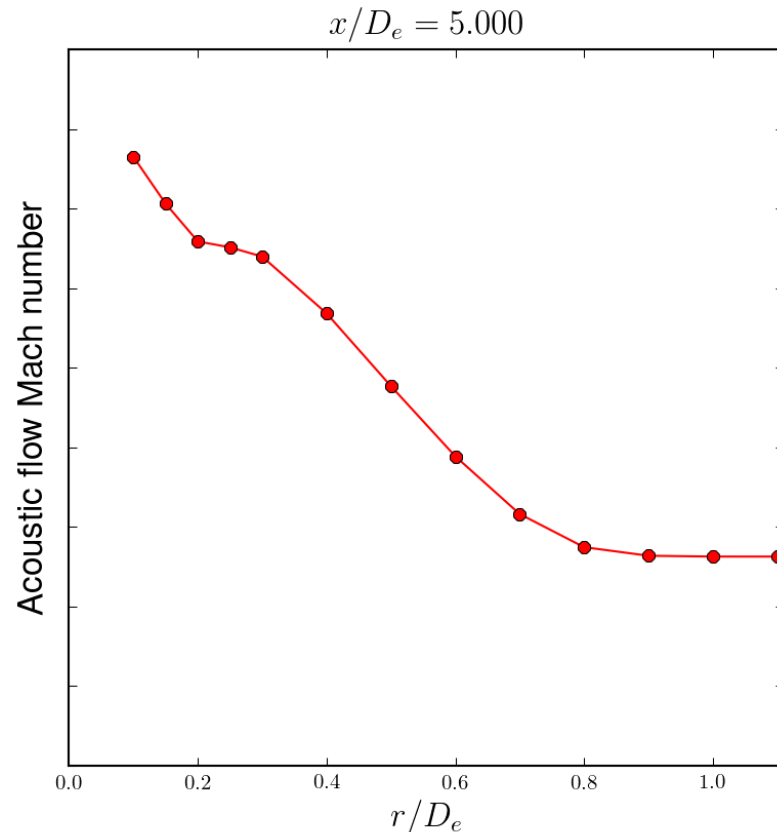


$x/D_e = 20$



Mean velocity and mean square pressure

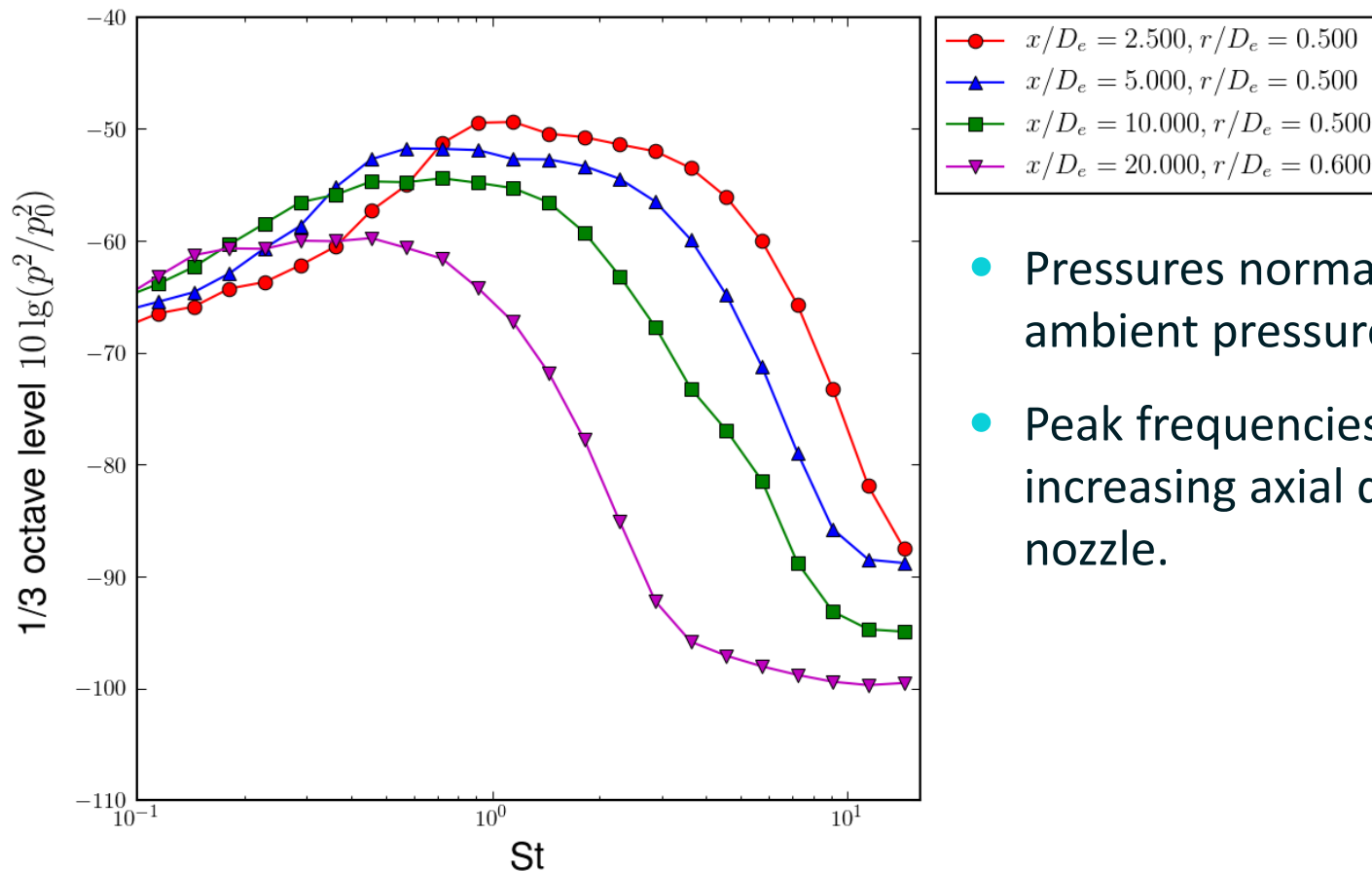
$x/D_e = 5$



- Pressure fluctuations largest where radial velocity gradient largest
- Valid for all axial positions in jet



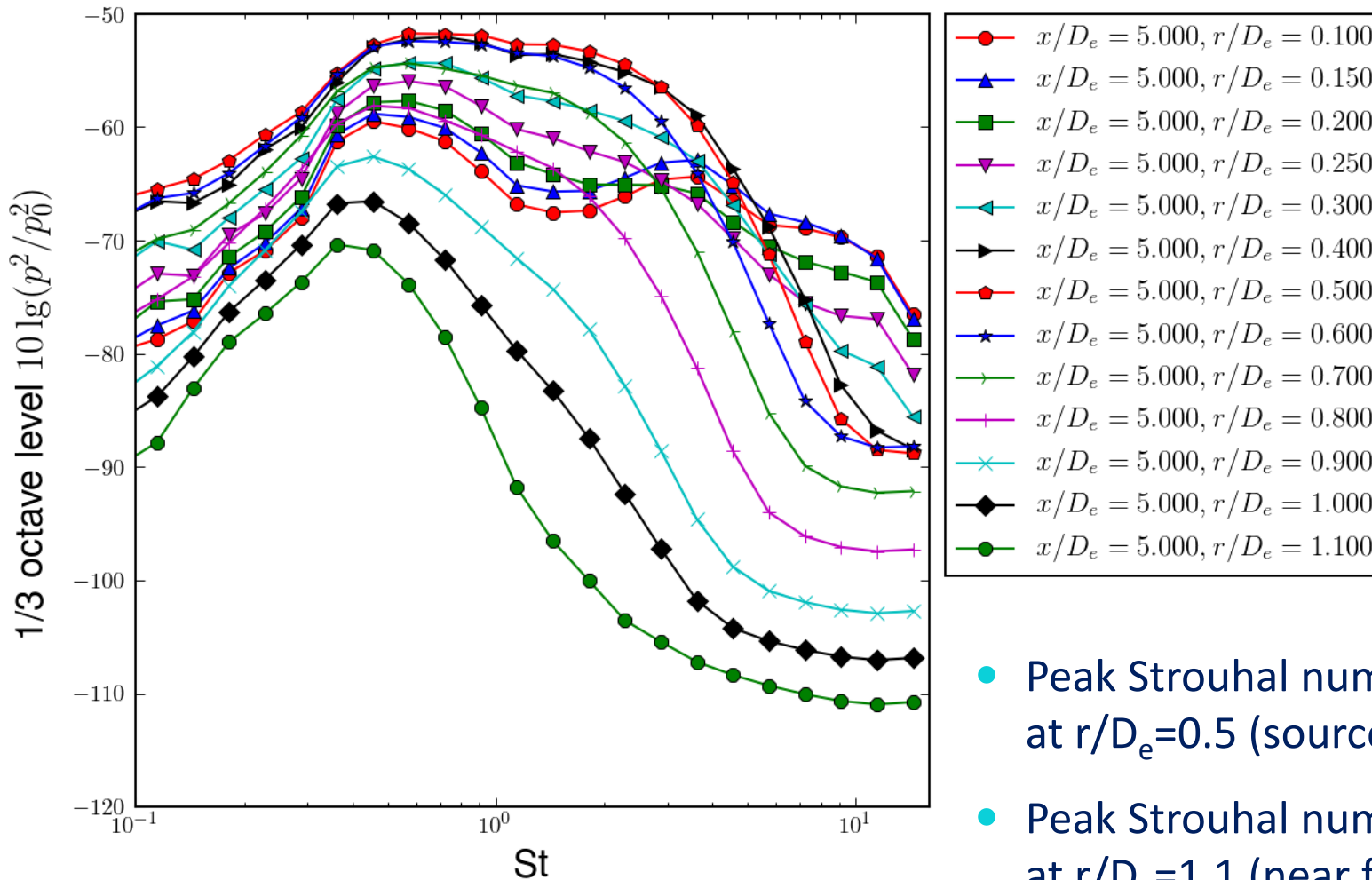
One-third octave band spectra for various x/D_e



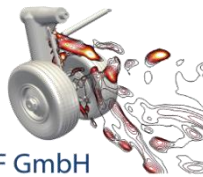
- Pressures normalized with the ambient pressure p_0 .
- Peak frequencies get smaller with increasing axial distance from the nozzle.



One-third octave band spectra for $x/D_e=5$

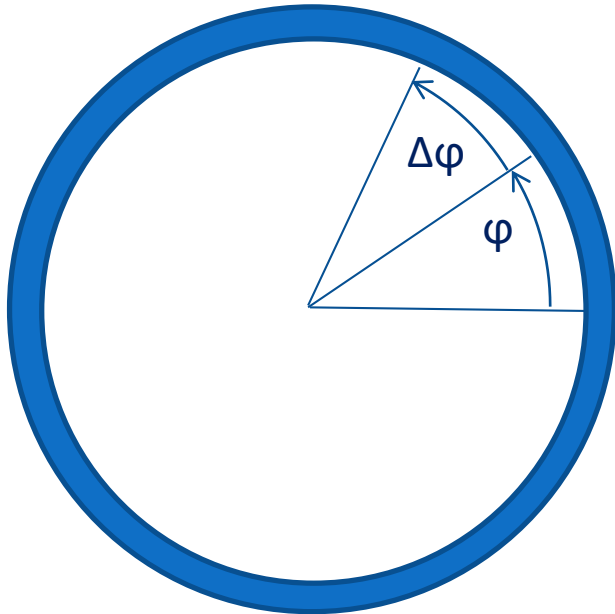


- Peak Strouhal number $St=0.7$ in at $r/D_e=0.5$ (source field)
- Peak Strouhal number $St=0.4$ at $r/D_e=1.1$ (near field)

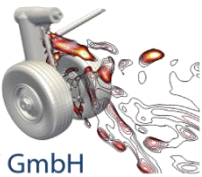


Identification of large scale structures

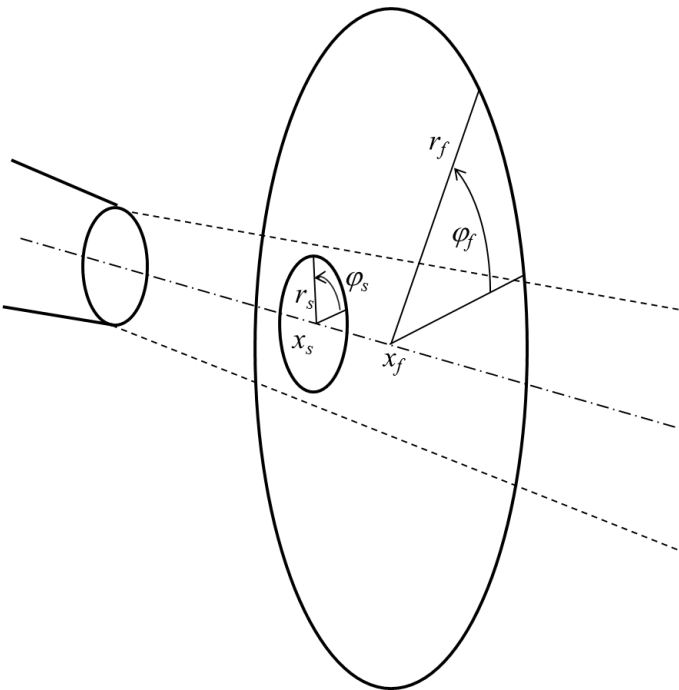
- Large scales can be studied with two-point cross-spectra
- Ring source element for azimuthal source separation.



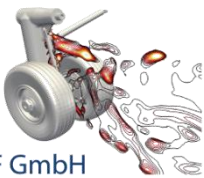
- Cross spectrum only function of frequency and azimuthal angle difference $|\Delta\varphi|$
- Cross spectra as function of $|\Delta\varphi|$ can be decomposed into Fourier series



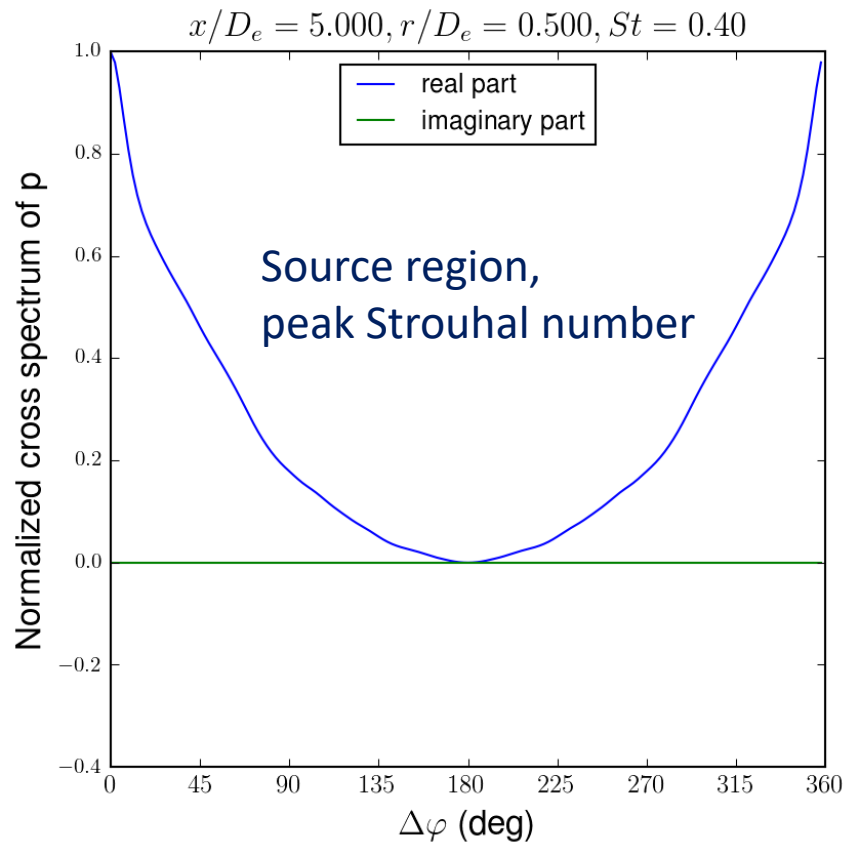
Azimuthal components of unsteady flow and sound fields



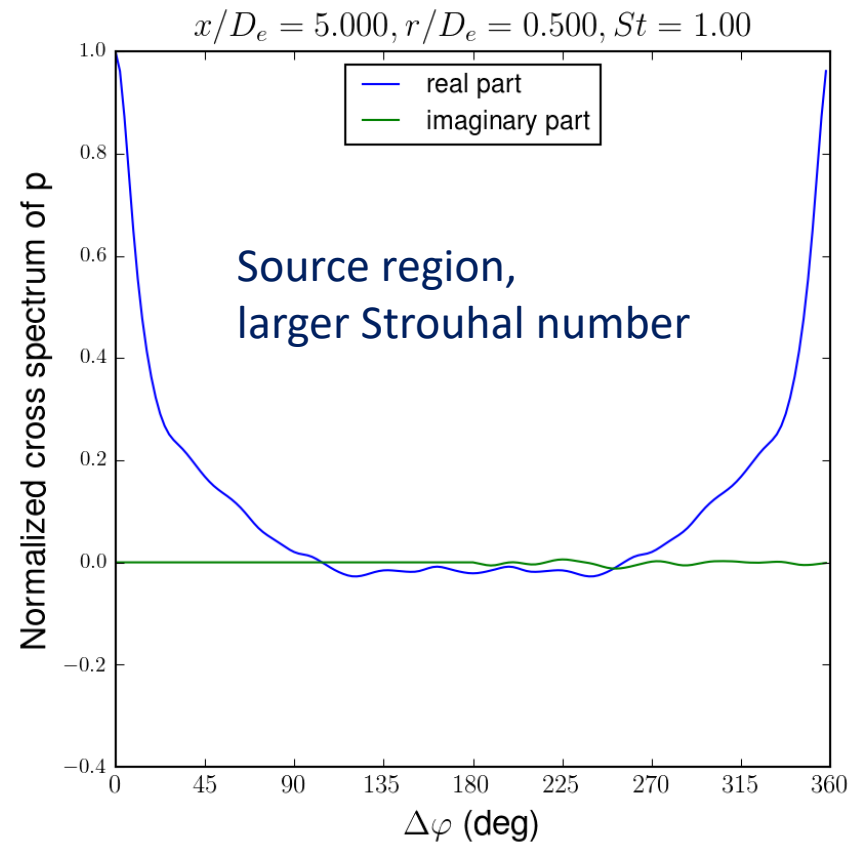
- Decomposition into azimuthal components m possible for any flow variable, including q or p
- Each far-field m is caused by the same m of sources in flow field (Michalke 1972)
- Pressure field inside jet dominated by low-order m (Experiments Armstrong et al 1977)
- Far field dominated by low-order m (Experiments Maestrello 1977)
- Results of computational experiment are now shown



Cross spectra of pressure on a ring



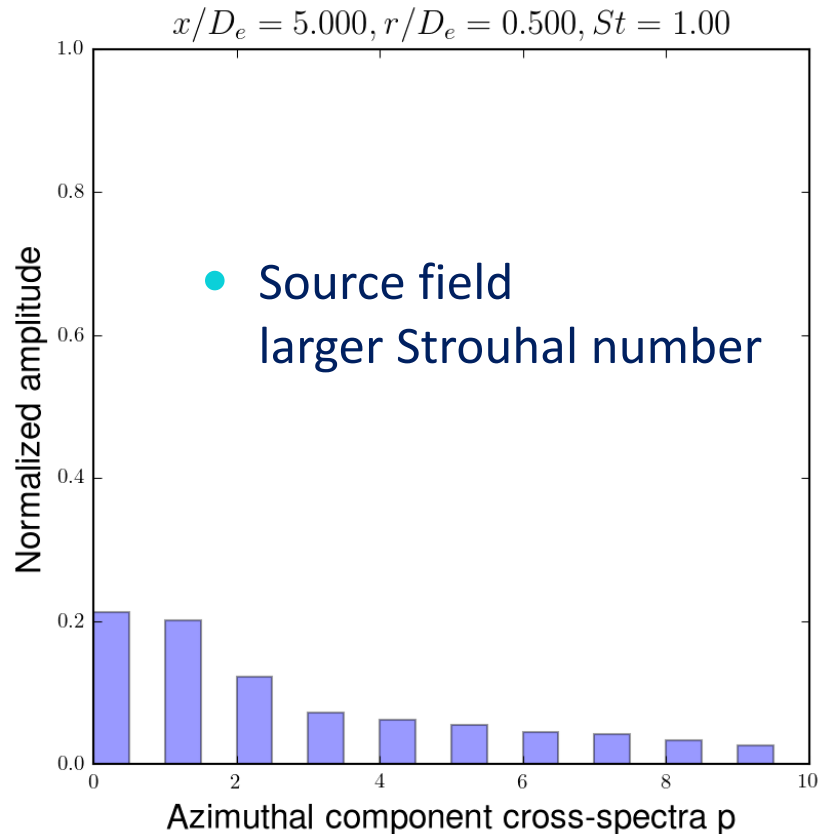
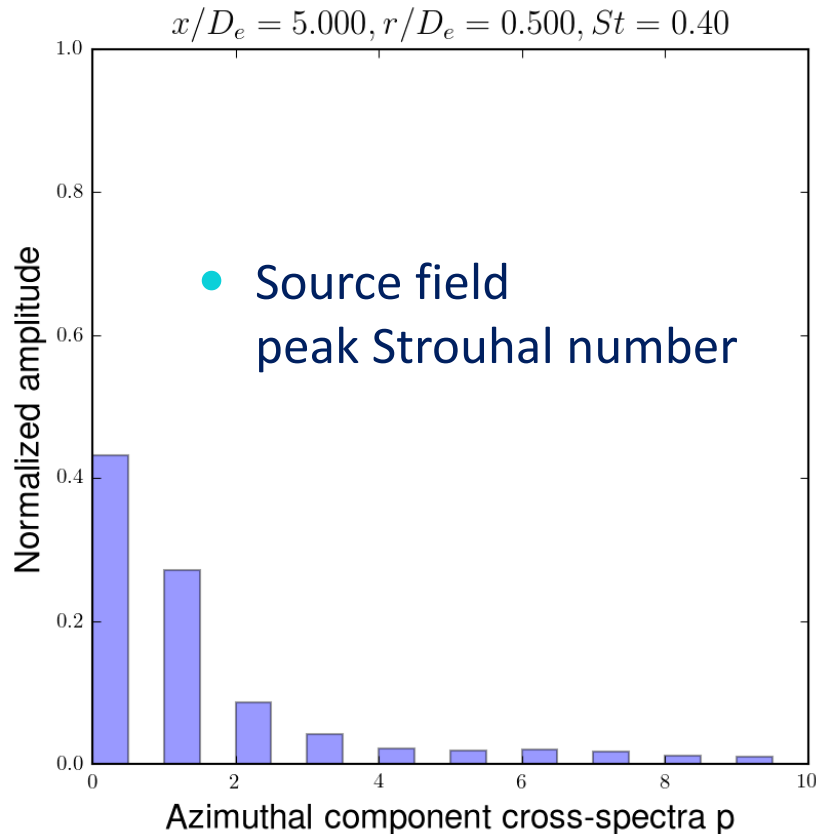
- Peak Strouhal number in middle of shear layer
- Gradual decrease of real part



- Higher Strouhal number in middle of shear layer
- Rapid decrease of real part



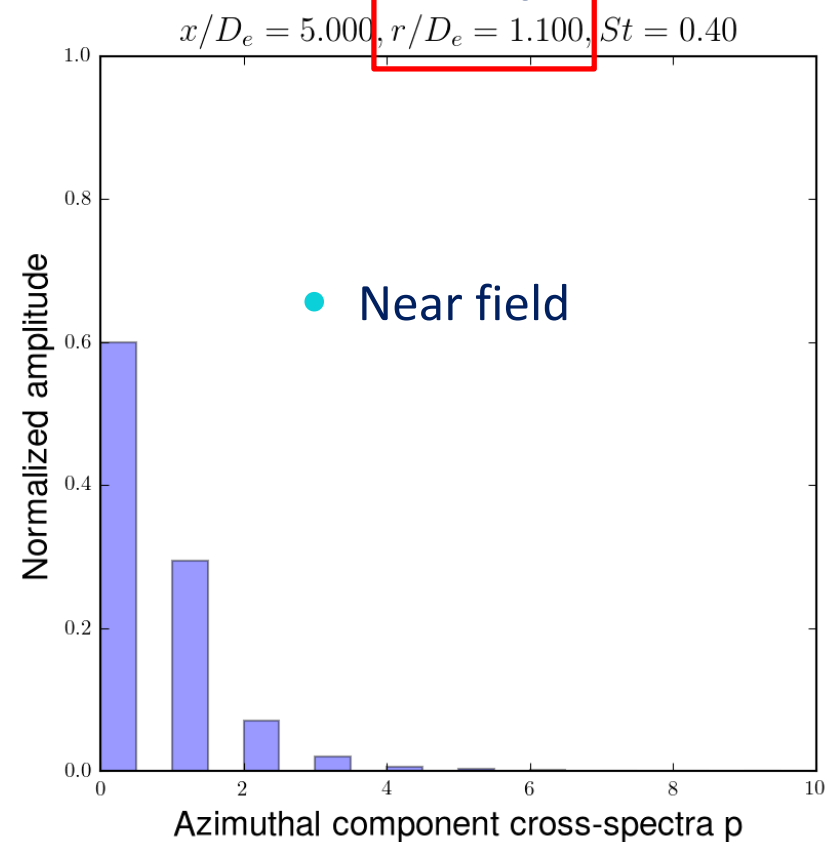
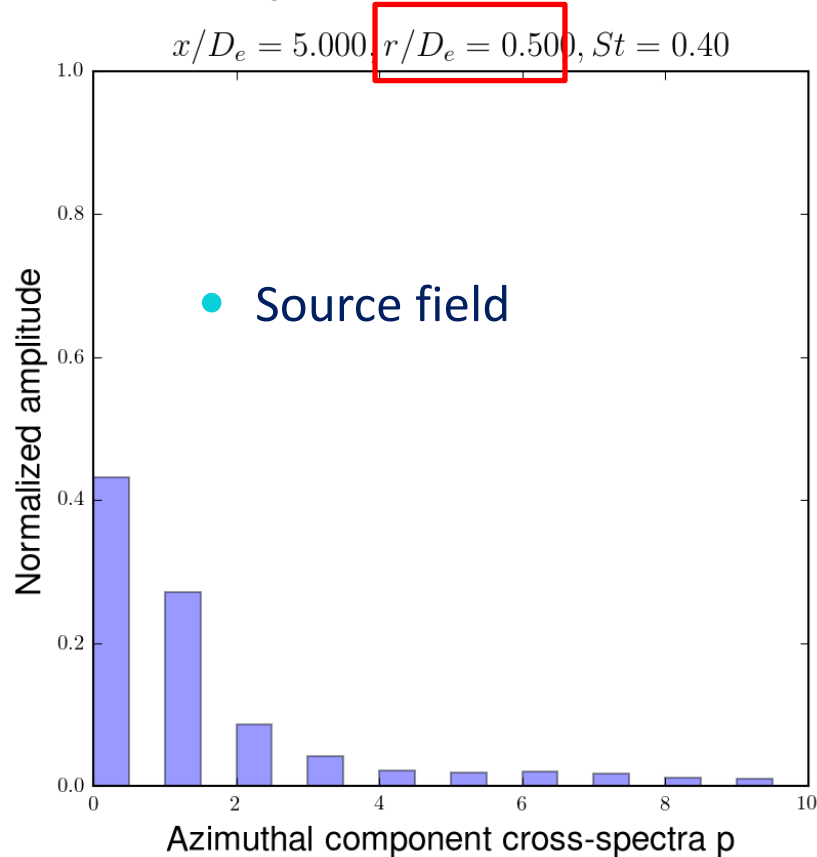
Decomposition into azimuthal Fourier components



- $m=0$ and $m=1$ components dominate source field
- Amplitude decay faster for higher Strouhal number, less efficient radiation
- Pressure fluctuations for both St almost identical



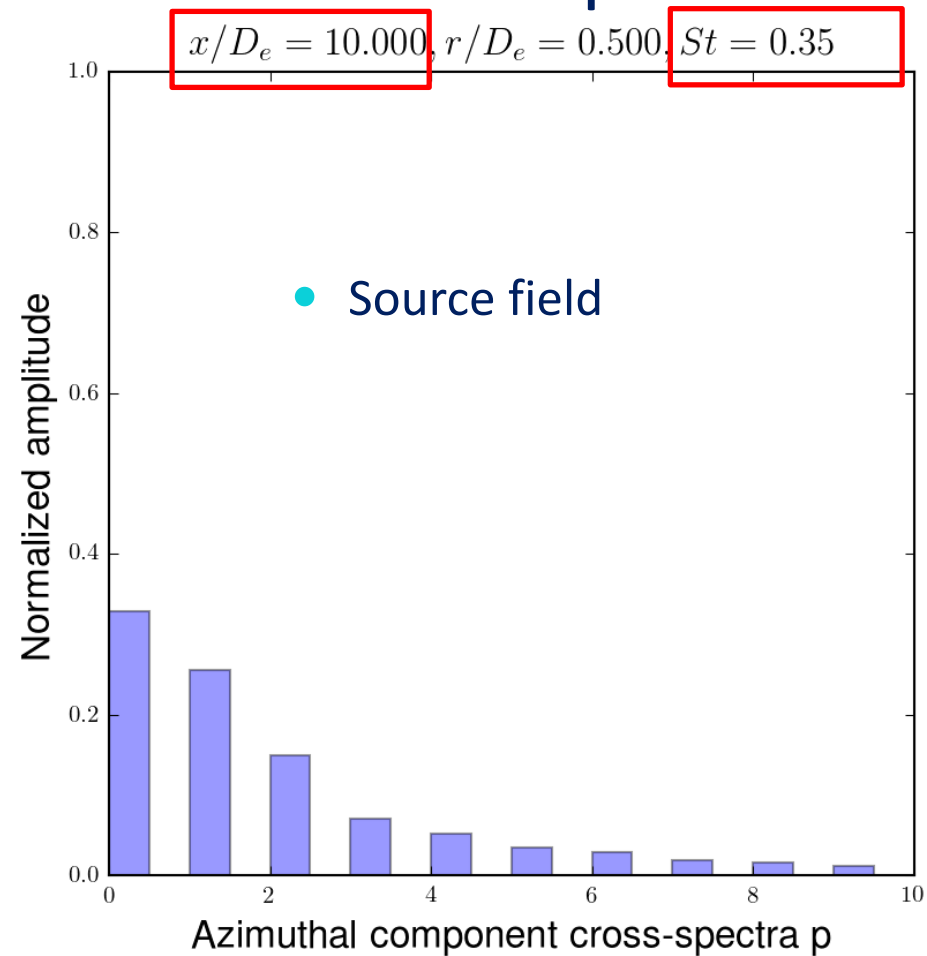
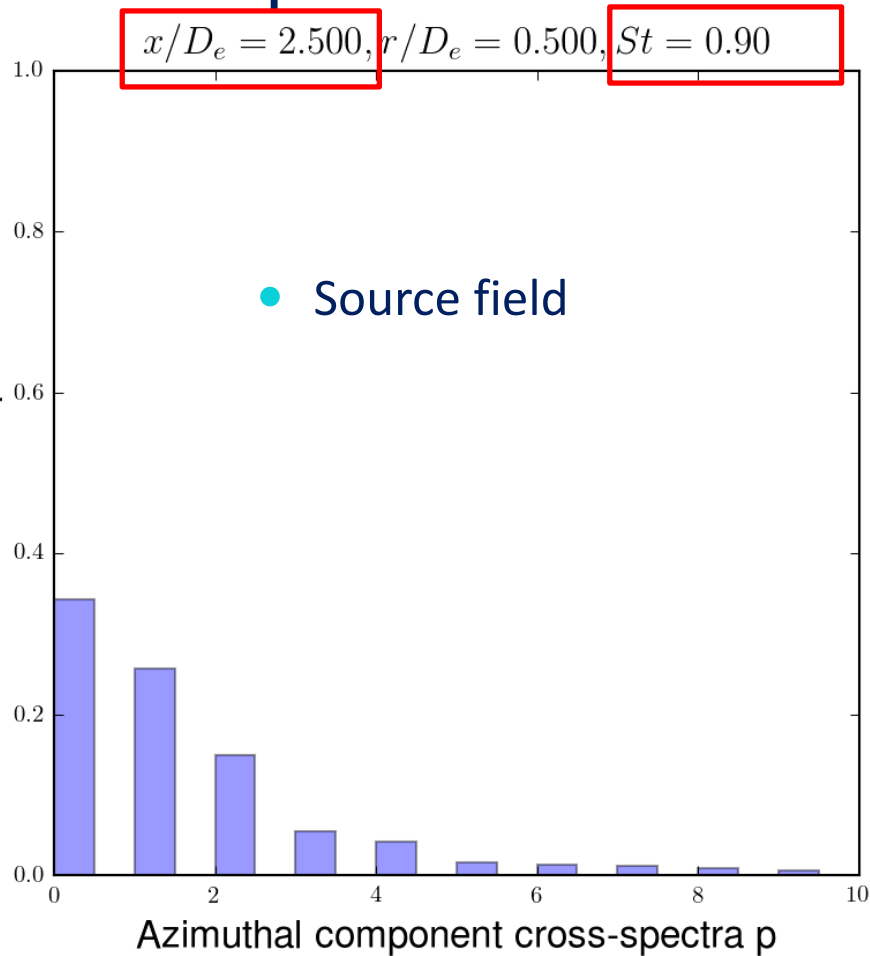
Decomposition into azimuthal Fourier components



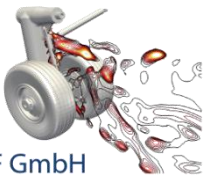
- Low order m are larger in near field than in source field because of lower radiation efficiency



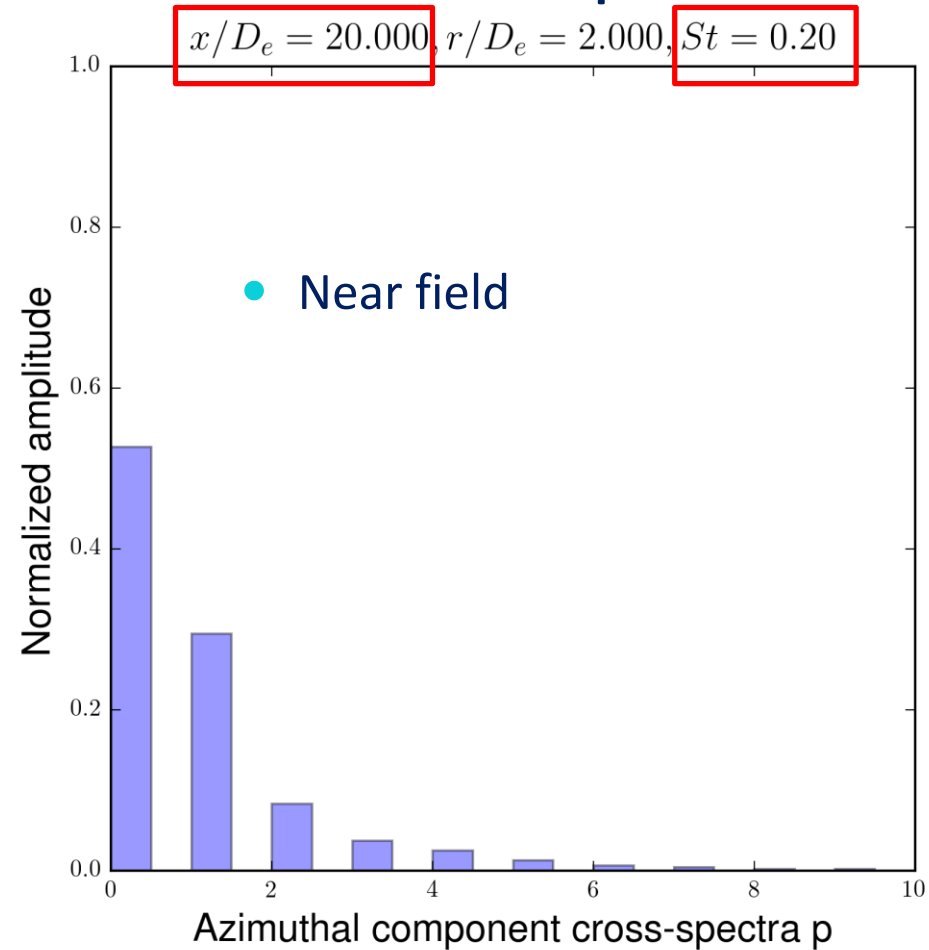
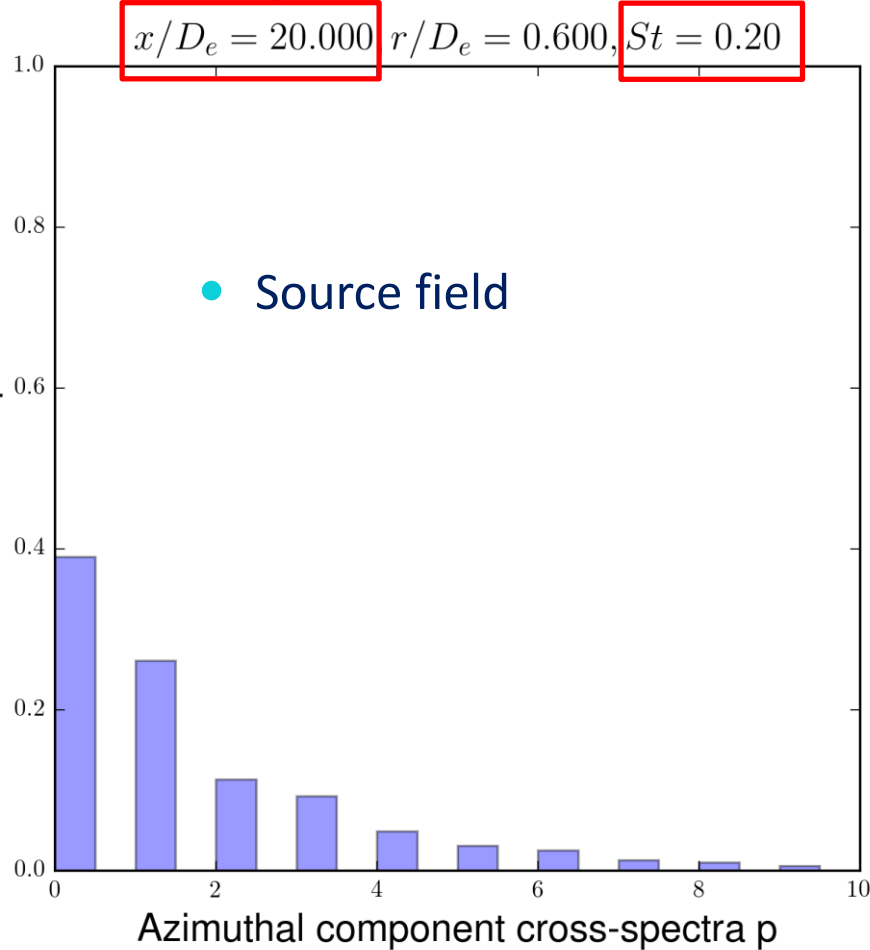
Decomposition into azimuthal Fourier components



$m=0, 1,$ and 2 components dominate source field at $x/D_e=2.5$ and $x/D_e=10$, levels almost identical



Decomposition into azimuthal Fourier components

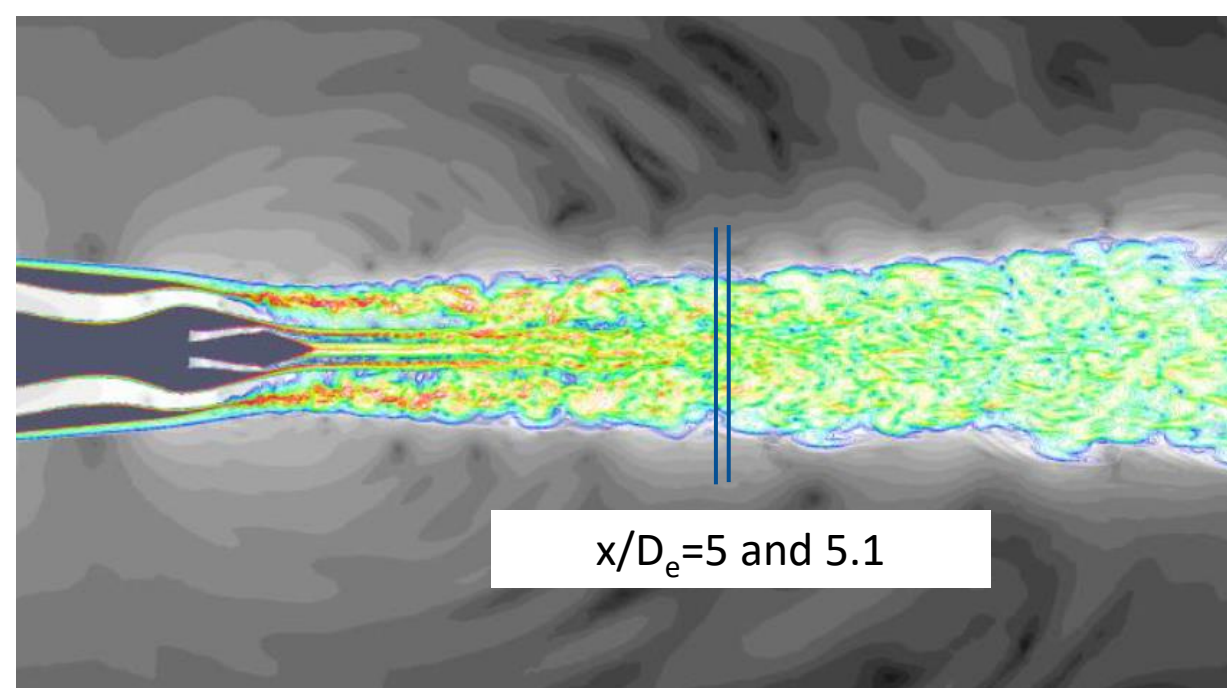


$m = 0$ and 1 components dominate source field and near field at $x/D_e=20$



Phase speeds

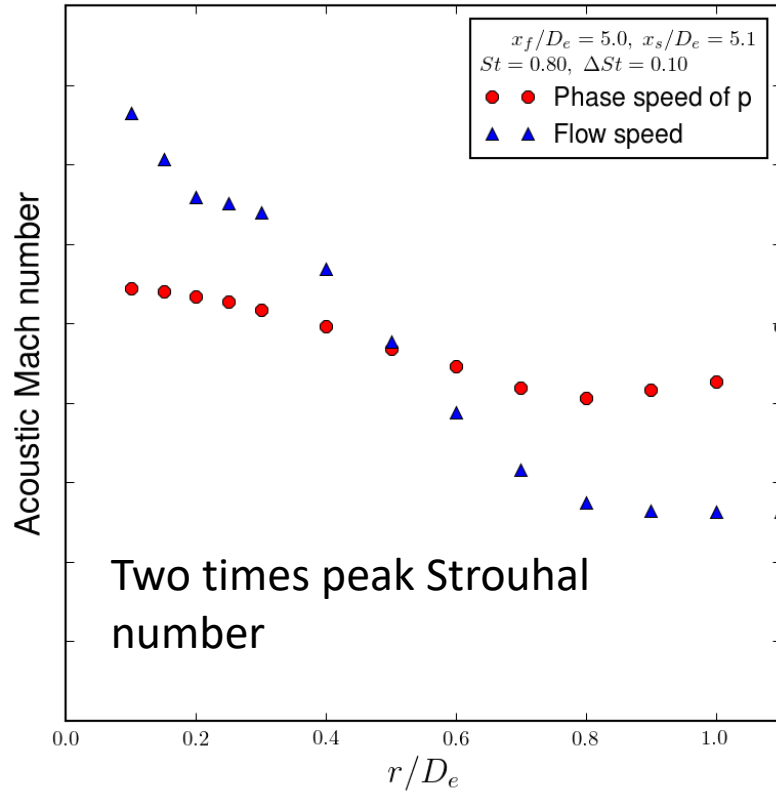
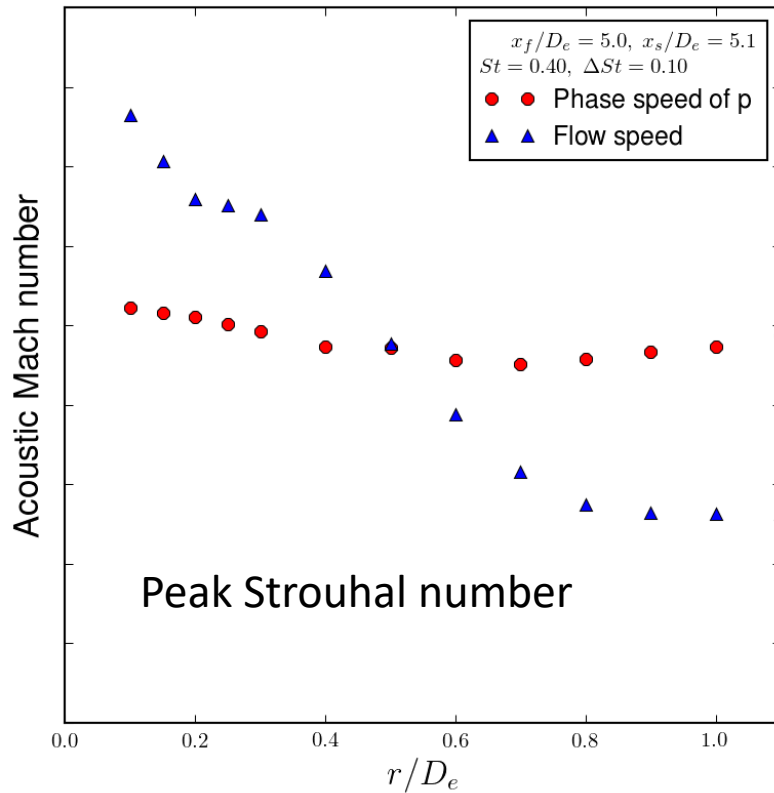
Cross-spectral density between two axial positions
Results shown for $x_1/D_e = 5.0$ and $x_2/D_e = 5.1$



Snapshot of simulation with
location of phase speed
analysis



Phase speeds $x/D_e=5$



- Phase speed almost independent of radius
- Even in near field outside jet
- Result similar for all other axial positions
- Pressure fluctuations dominated by the influence of wave-like fluctuations related to the instability of the jet shear layer.



Conclusions

- Jet noise sources dominated by contribution of low-order azimuthal modes
- Noise sources are results of wave-like motion
- High frequencies caused by wave-like motion close to nozzle
- Low frequencies caused by wave-like motion further downstream
- Only a few azimuthal components contribute to the near-field radiation and likely even less to the far-field radiation
- The noise sources are concentrated at the radial location with the steepest radial velocity gradient.
- A cylindrical jet noise source model is likely sufficient
- “Small scale stuff” in source region is ineffective radiator
- “Small scale stuff” may even mask large scale motion



Conclusions 2

- Moving eddy model for jet noise sources is completely wrong.
- In the critical layer (phase speed = flow speed) the frequency of a moving eddy would be zero.
- Lighthill (1954) and Ffowcs-Williams (1963) erred in this respect.
- Michalke (1972) was right when he introduced the wave model for jet turbulence.

Acknowledgement

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References

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