

Aircraft Noise Simulation at DLR

Roland Ewert

DLR Institute of Aerodynamics and Flow Technology
Technical Acoustics

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Knowledge for Tomorrow



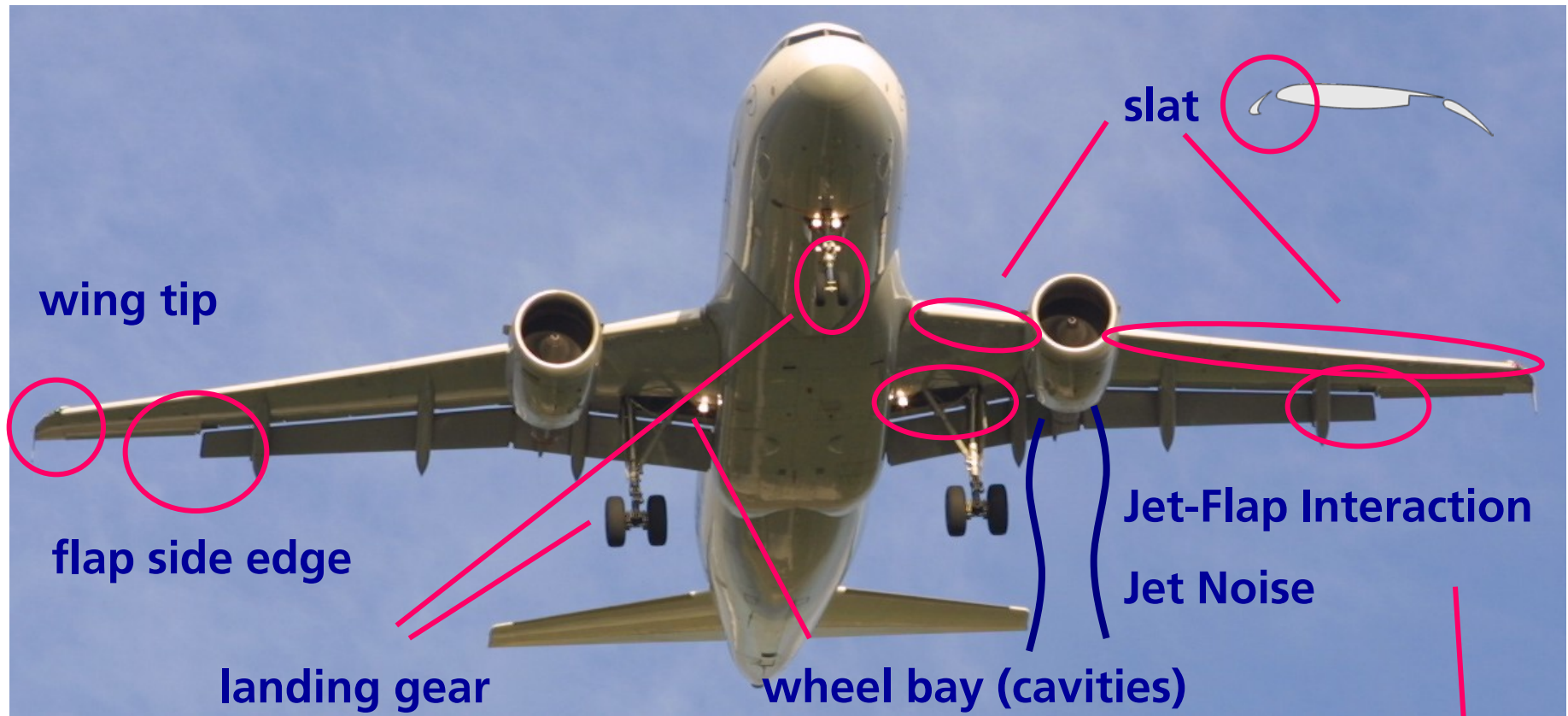
Outline

- Aeroacoustic problems tackled at DLR Braunschweig
- Overview of simulation approaches
- Surface integral methods
 - Fast Multipole BEM tool
 - Influence of simplified propagation physics
- Volume discretization approach
 - Direct noise computation (DNC)
 - RANS based modeling of AFN with stochastic sound sources
 - DGM for aeroacoustic simulations



Sources of exterior noise at aircraft

Re-Number of order 10mio!



Sources of interior noise at aircraft

- **exterior excitation:**

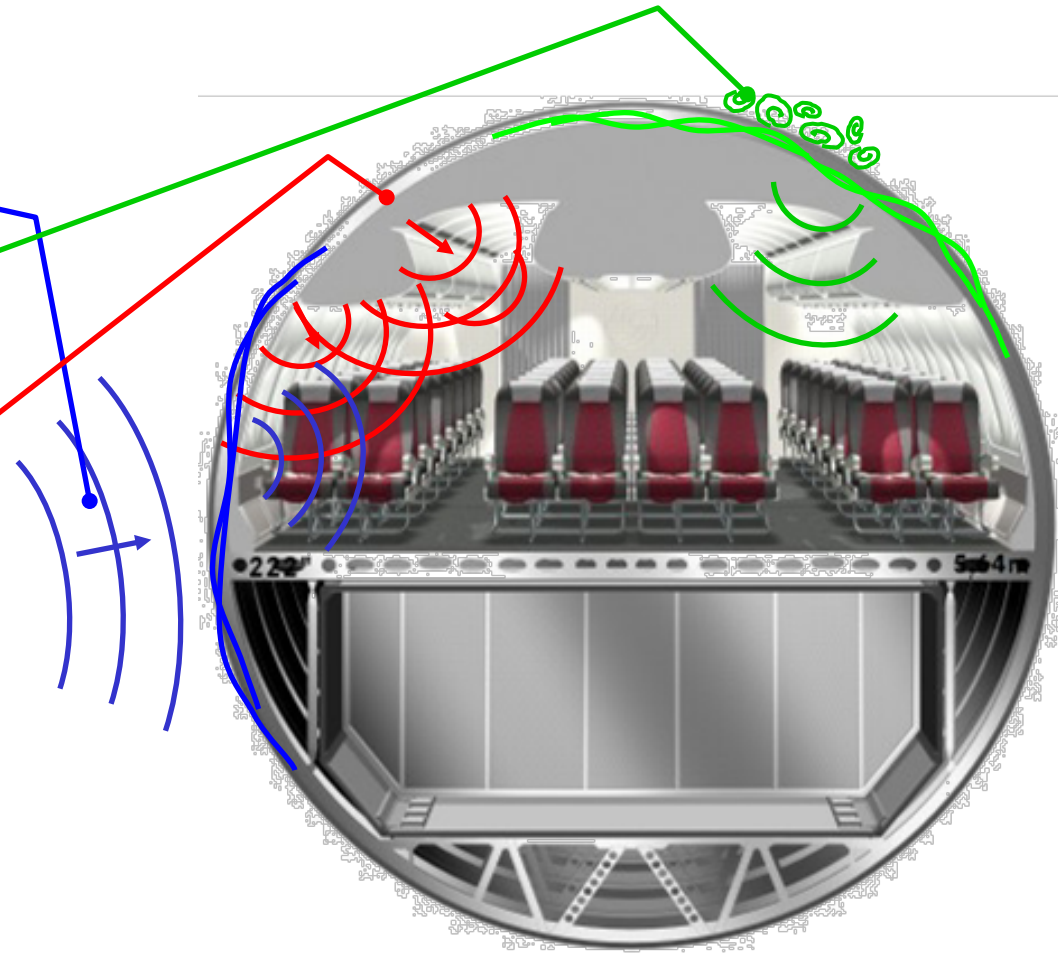
airborne engine noise

fuselage boundary layer

- **interior excitation:**

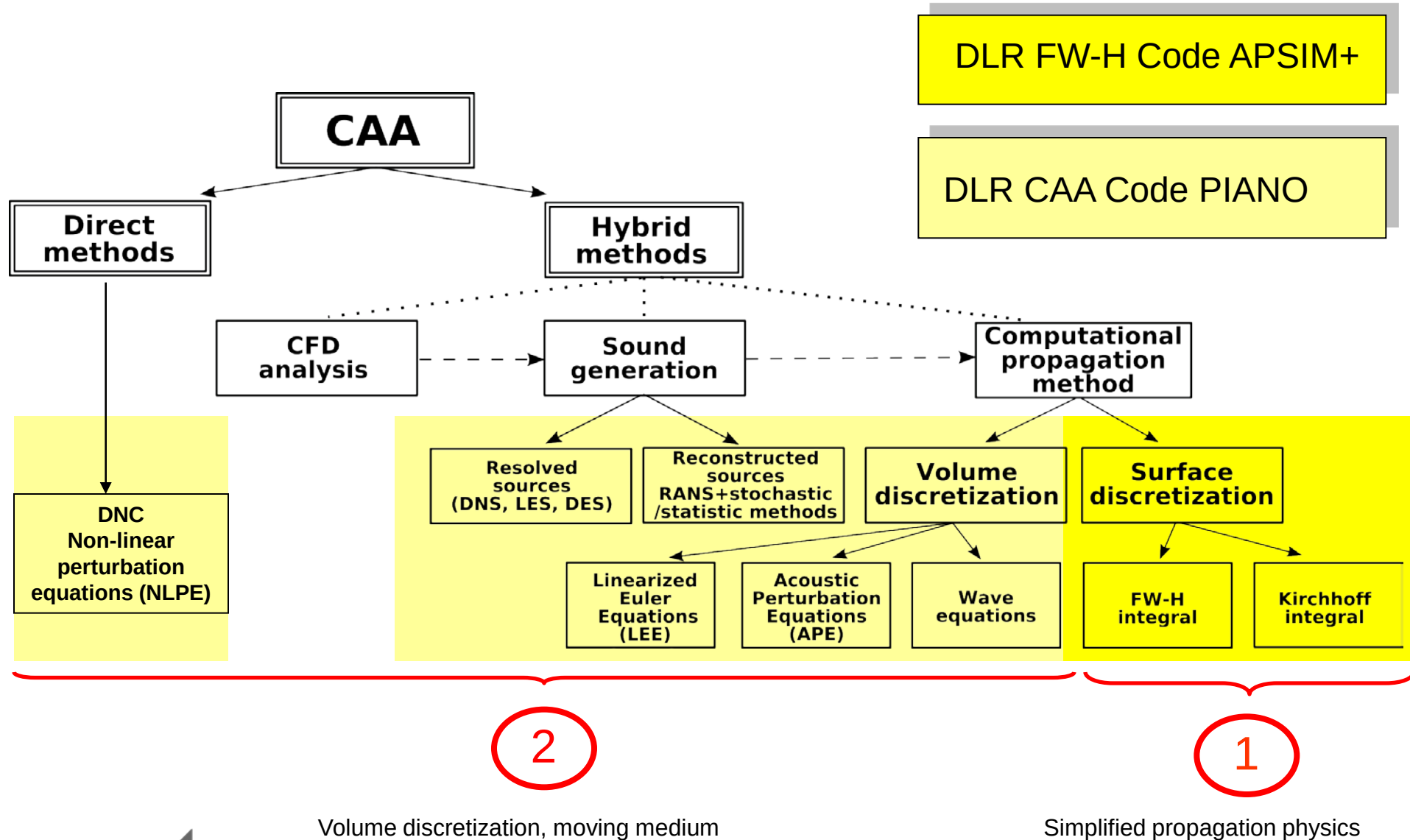
air system

(hydraulic system)



Aeroacoustic Simulation

Paths of simulations in Computational Aeroacoustics (CAA)



1

Tools for solution of wave equation

Direct propagation and acoustic installation

Source

Interface model

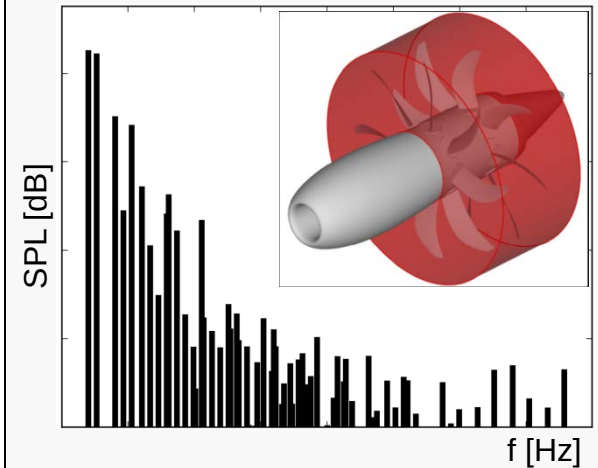
Wave equation

URANS/CAA
analyt.models

Direct: FW-H APSIM+
Installation:
Ray tracer SHADOW
Fast Multipole BEM

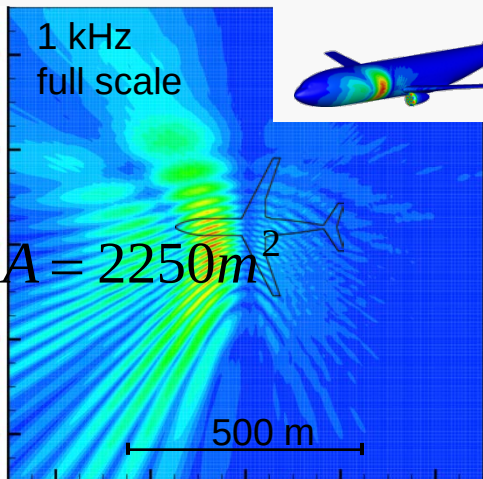
⇒ computation of acoustic installation + a/c farfield

Open rotor noise



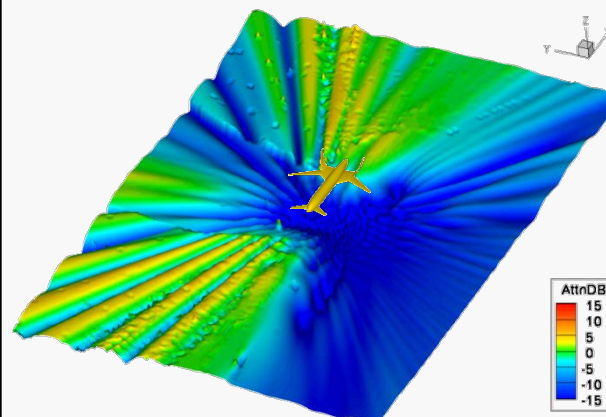
Flow: TAU/ sound: APSIM+

Acoustic a/c installation fan



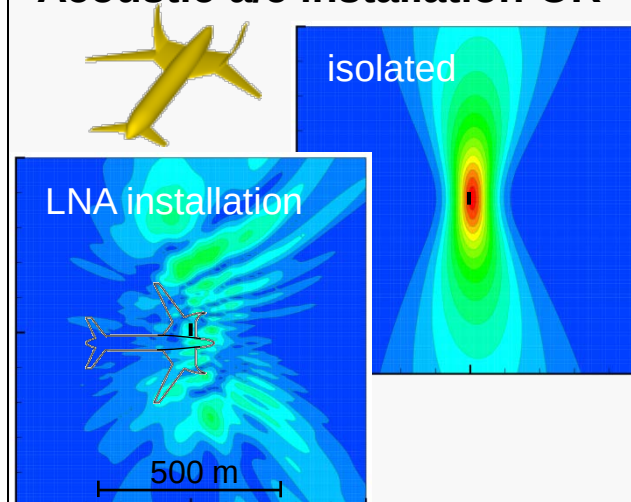
source: anal. (RRD)
sound: FM-BEM

Ultra fast installation estimation



source: directed point source
noise: SHADOW

Acoustic a/c installation OR



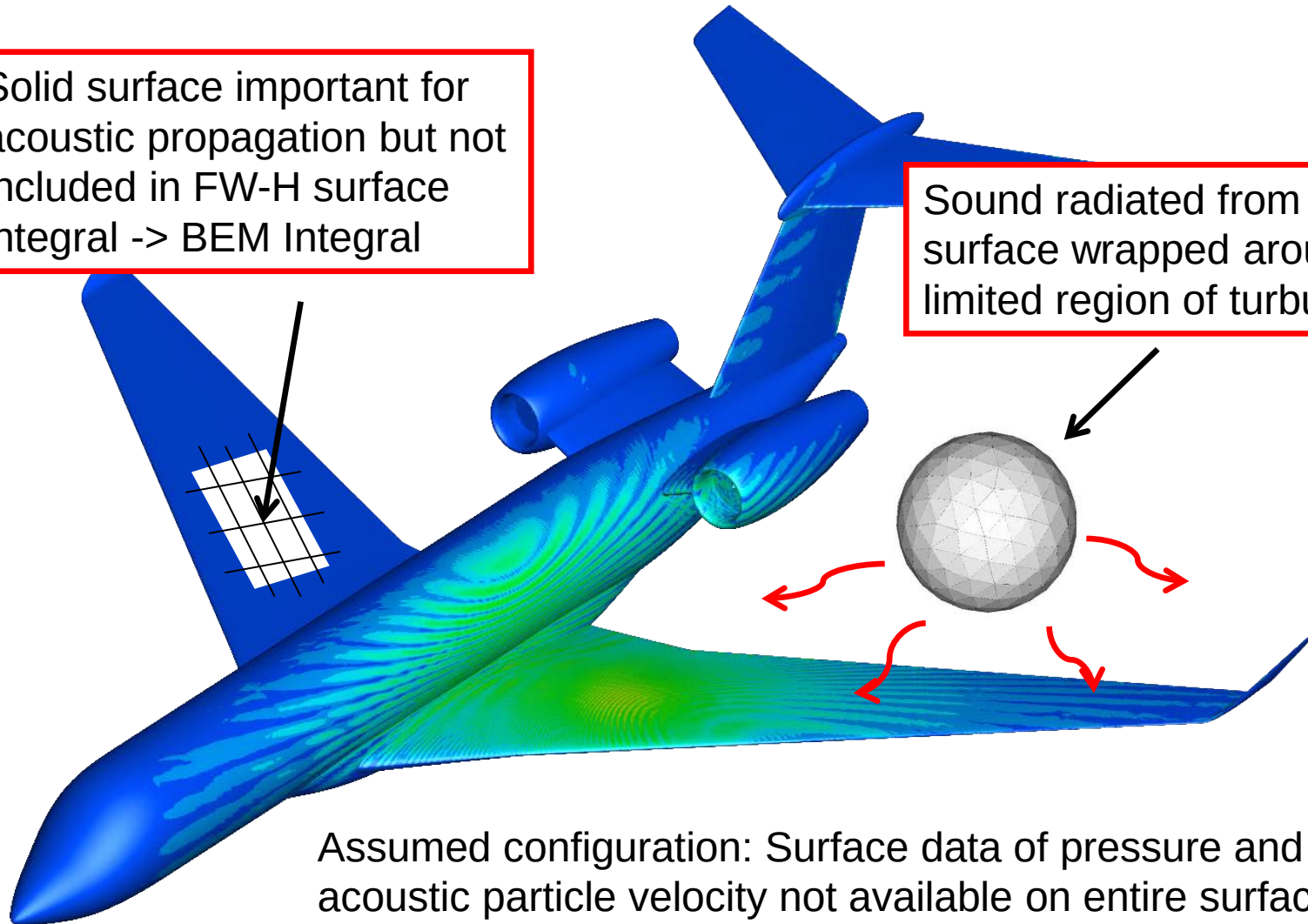
source: TAU fed analytical model
noise: FM-BEM



FW-H becomes FW-H + BEM if unsteady surface data is not available on the entire surface

Solid surface important for acoustic propagation but not included in FW-H surface integral -> BEM Integral

Sound radiated from FW-H surface wrapped around limited region of turbulence



Assumed configuration: Surface data of pressure and acoustic particle velocity not available on entire surface

Boundary Element Method

- Solution of the (Helmholtz) wave equation
- Integral equation for the **surface pressure**: **Burton/Miller** formulation with wall admittance Y

$$\left[1 + \alpha Y\right] \frac{p(x)}{2} - \int p(y) \left[1 + \alpha \frac{\partial}{\partial n_x}\right] \left[\frac{\partial}{\partial n_y} - Y\right] G(x-y) d\Omega_y = \left[1 + \alpha \frac{\partial}{\partial n_x}\right] p_{Inc}(x)$$

- **Very large system of linear equations**
 - Six elements per wave length necessary
- **Direct solver** (e.g. Gauss procedure)
 - Matrix is full, complex, and non-symmetric
 - Extremely expensive for higher frequencies (i.e. > 1 kHz)
- **Iterative solver**
 - No storage of matrix required
 - **Fast matrix vector multiplication** is necessary
 - **Fast Multipole Method** (FMM) is method of choice



Boundary Element Method - Memory

- 6 elements per wave length λ
- Number of triangle elements N , Surface A

$$N \approx 6^2 \frac{A}{\lambda^2}$$

- **A340:** $A \approx 2250m^2$
- 341 Hz, $N \approx 8.1 \times 10^4$
- **2800 Hz**, $N \approx 5.46 \times 10^6$
 - Matrix Elements: 2.982×10^{13}
 - Single precision storage: 2.385×10^{14} Bytes, ca. **240 TB** Memory
 - Also working memory needed ...
 - Tianhe-1A-NUDT (2 of TOP500) has about 230 TB Memory ...



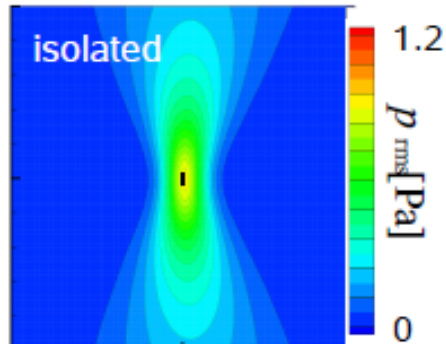
Fast Multipole Method

- Iterative solution of BEM equation
- Acceleration of matrix-vector product from $O(N^2)$ to $O(N \log(N))$
 - Splitting of every row of product into near and far field terms
 - Calculation of far field interactions by a series expansion
 - Far field contributions are collected and distributed over an Octree covering the geometry
- Example: Full scale aircraft (surface 582 m²)
 - 2170000 Triangles
 - Wavelength 0.1 m (3410 Hz)
 - 48 GB total memory (4 nodes)
 - 150s for one iteration step on 32 cores (Opteron 2.7 GHz)
 - 200 iteration steps (conjugate residual method)

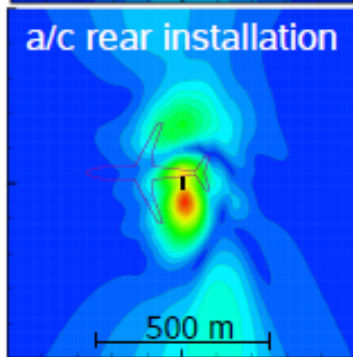


CROR acoustic installation effects configuration studies

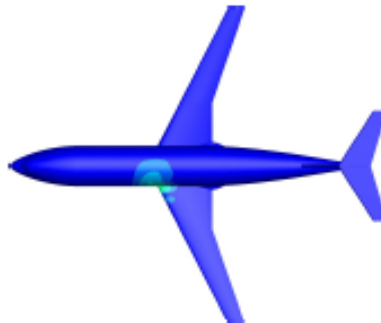
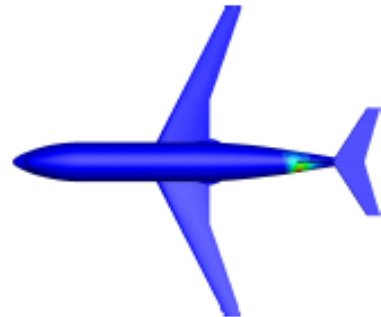
conventional a/c



a/c rear installation



a/c wing installation

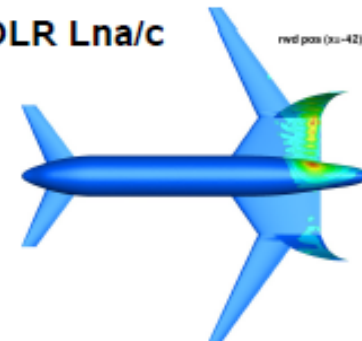


3 dB **increase**

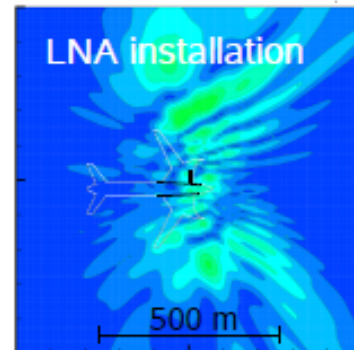
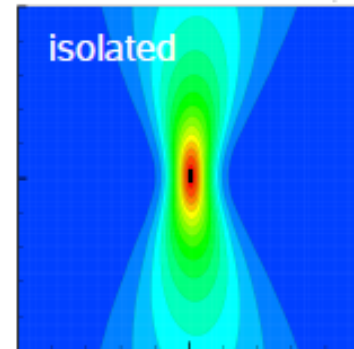
Footprints of loading
noise 120m below a/c
for BPF of front rotor

Flow
→

DLR Lna/c



DLR Lna/c



10-12 dB **reduction**

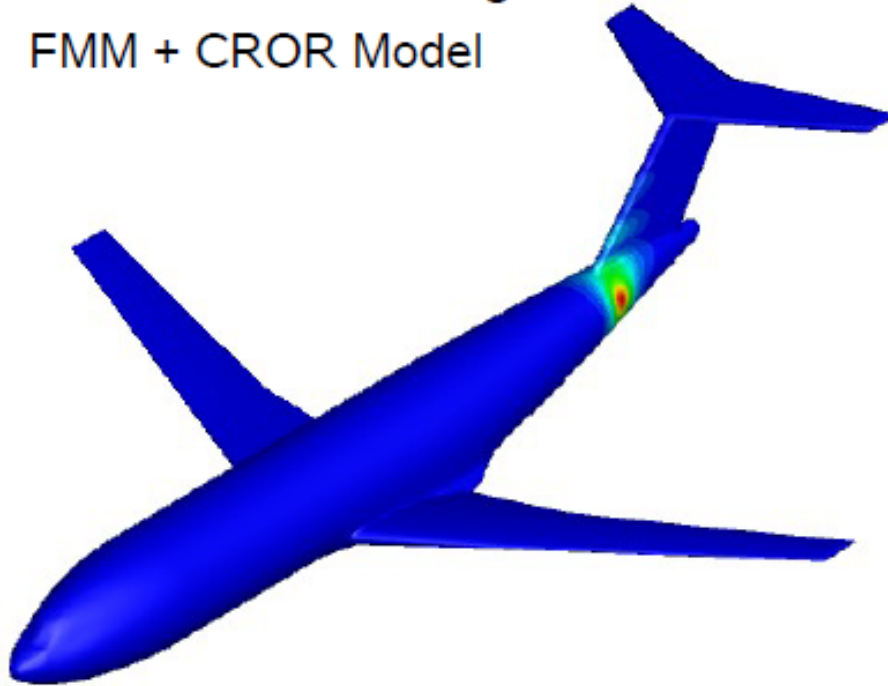
Source: uRANS
Sound: FMM BEM



F6OR Configuration

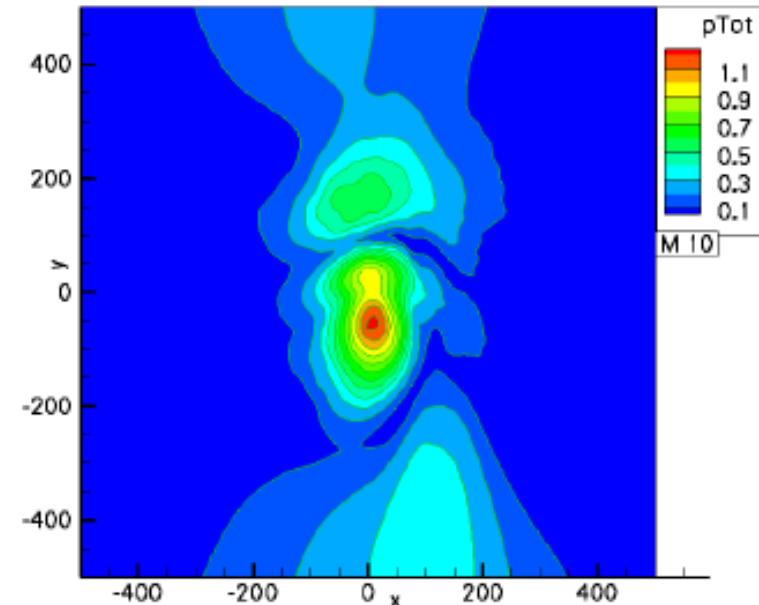
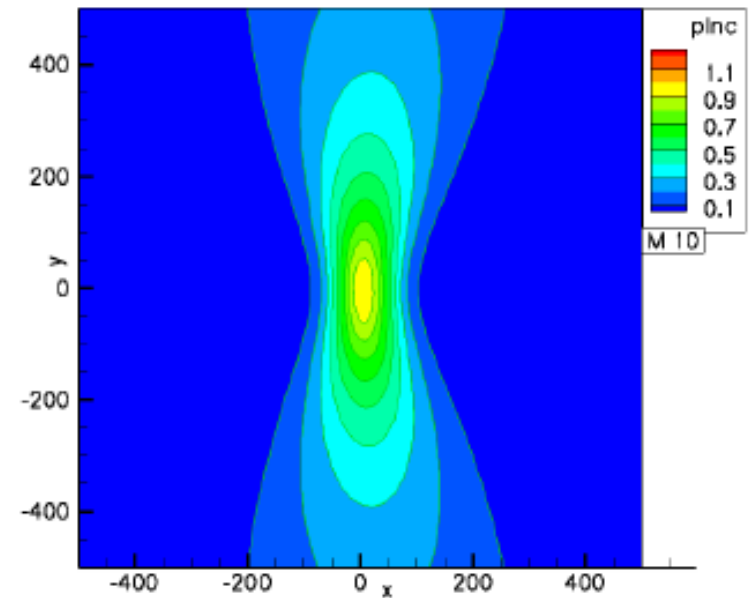
Front rotor installation effect

- 50,000 Surface Triangles
- FMM + CROR Model



$B_f=10$

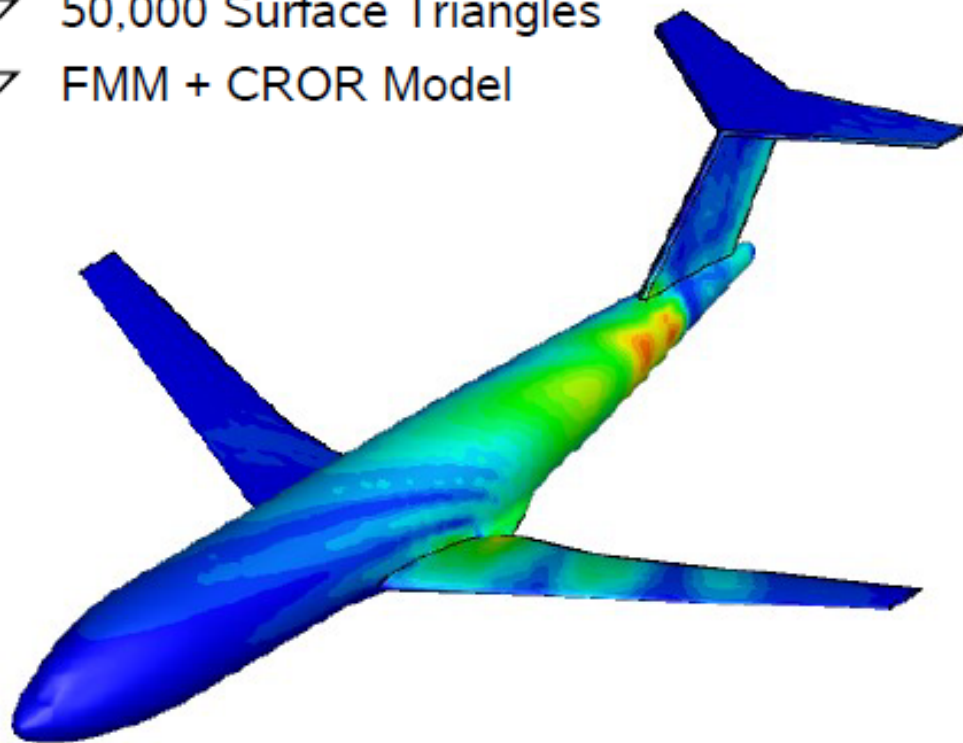
Source: uRANS
Sound: FMM BEM



F6OR Configuration

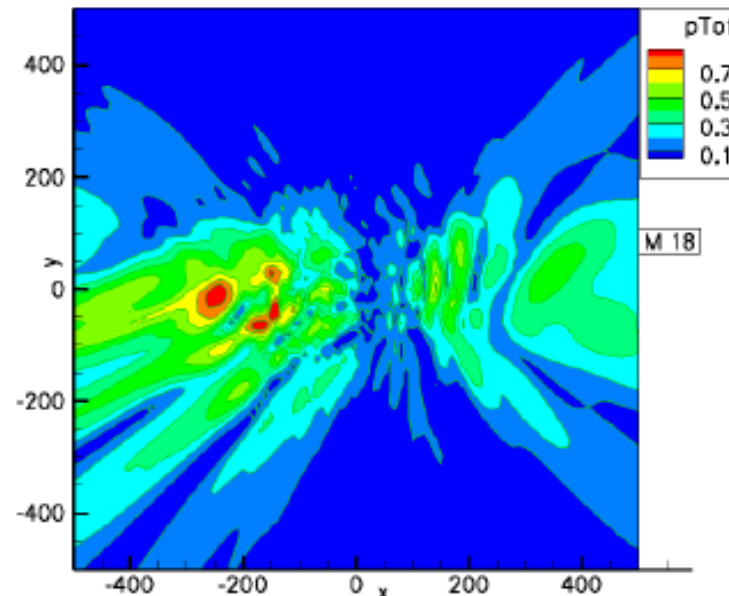
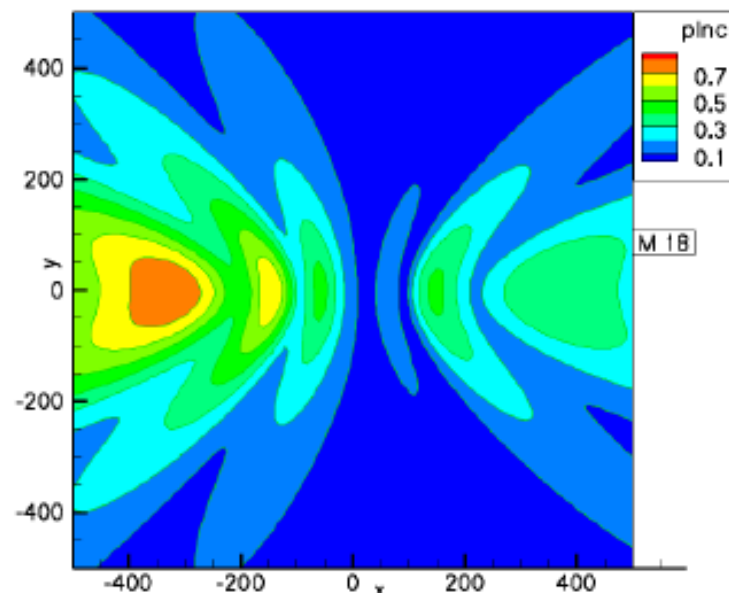
Interaction Harmonics

- 50,000 Surface Triangles
- FMM + CROR Model



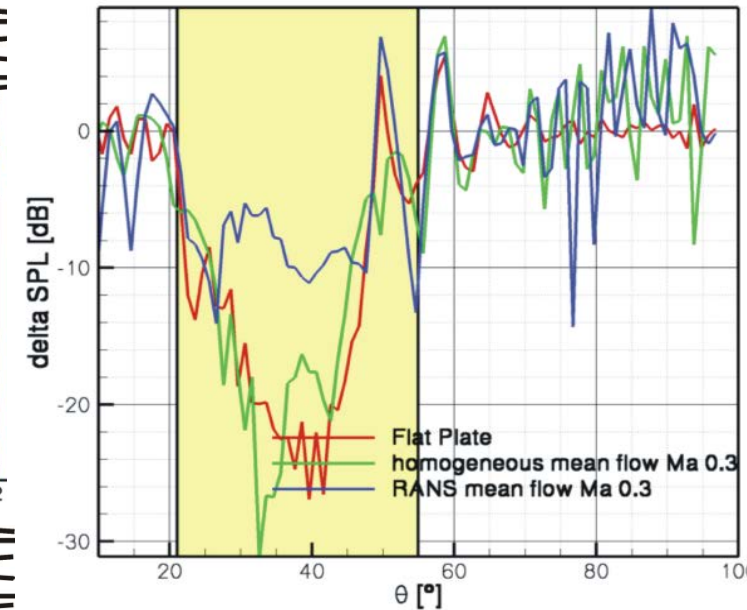
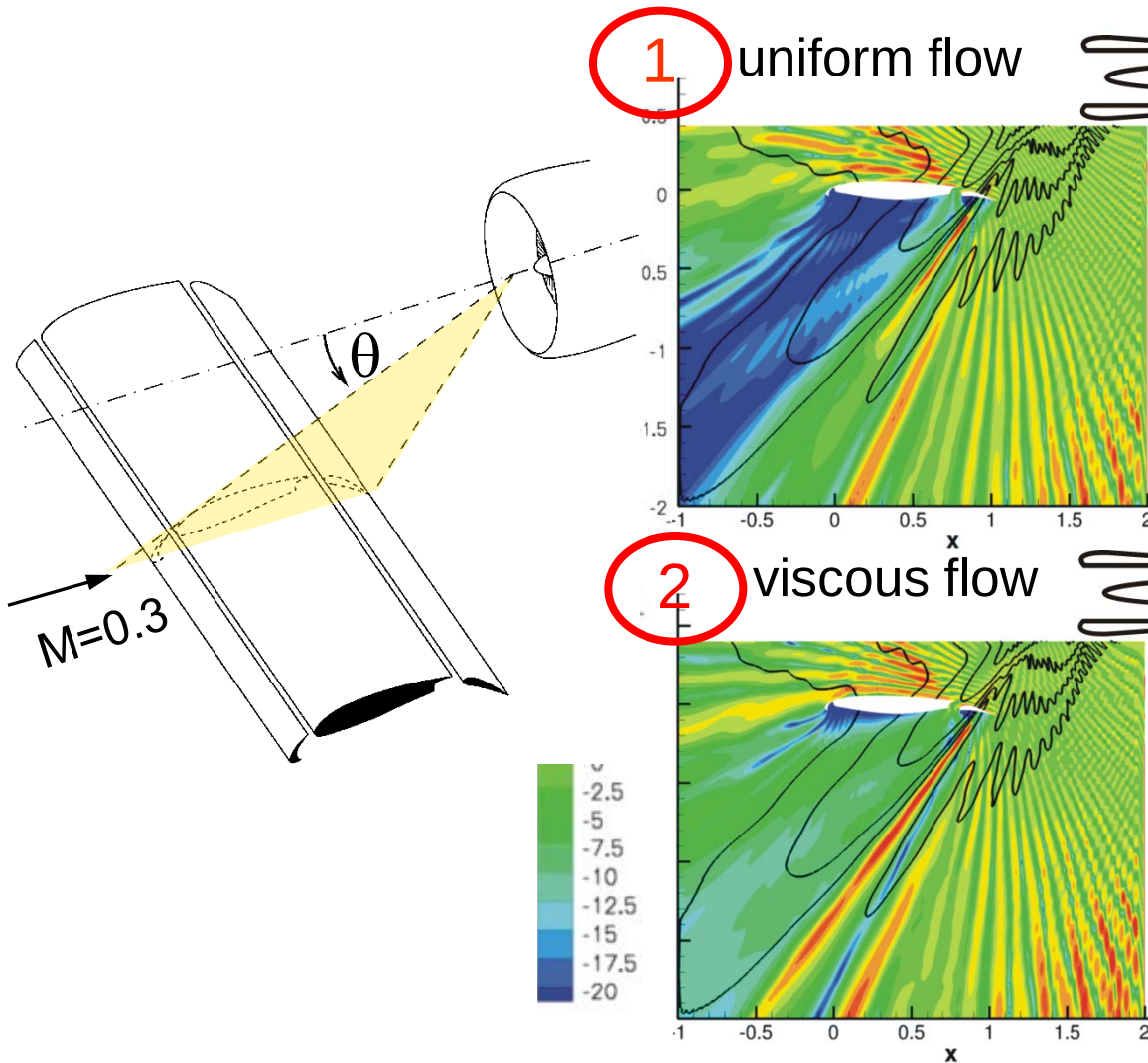
$$B_f + B_a = 18$$

Source: uRANS
Sound: FMM BEM



Importance of acoustic propagation effects

Installation effect on fan tones at High Lift Wing



Simplified flow assumption overpredicts shielding by 10dB!

Strong viscous flow effects on noise shielding even at low M

(experience from EU project NACRE)

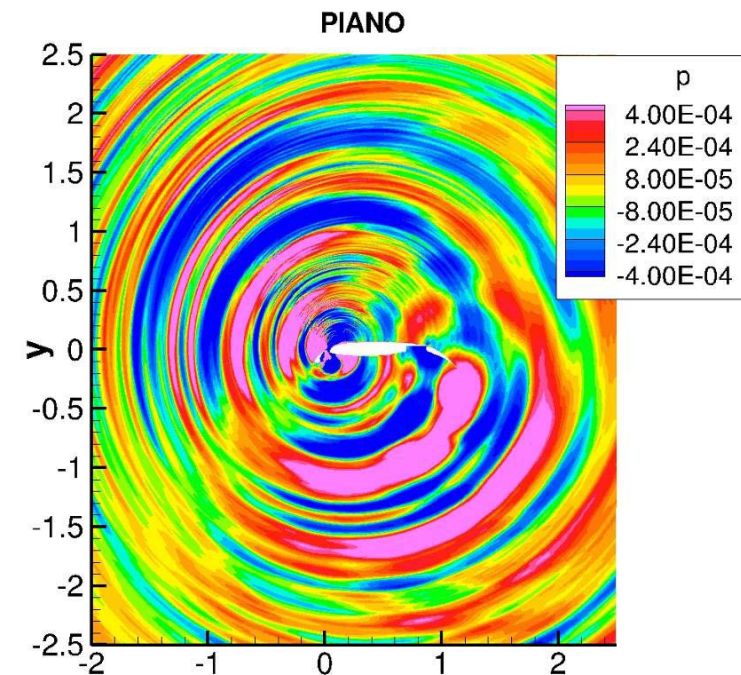
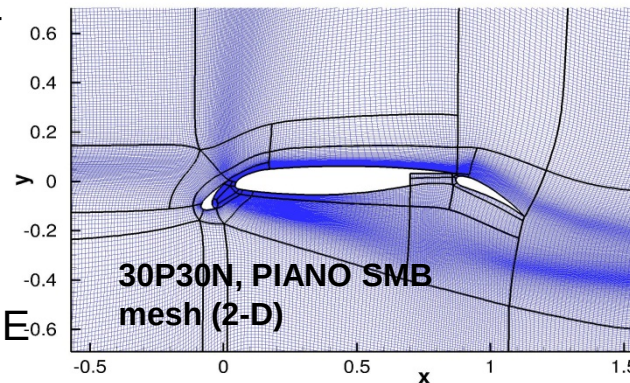


Slat Noise Simulations

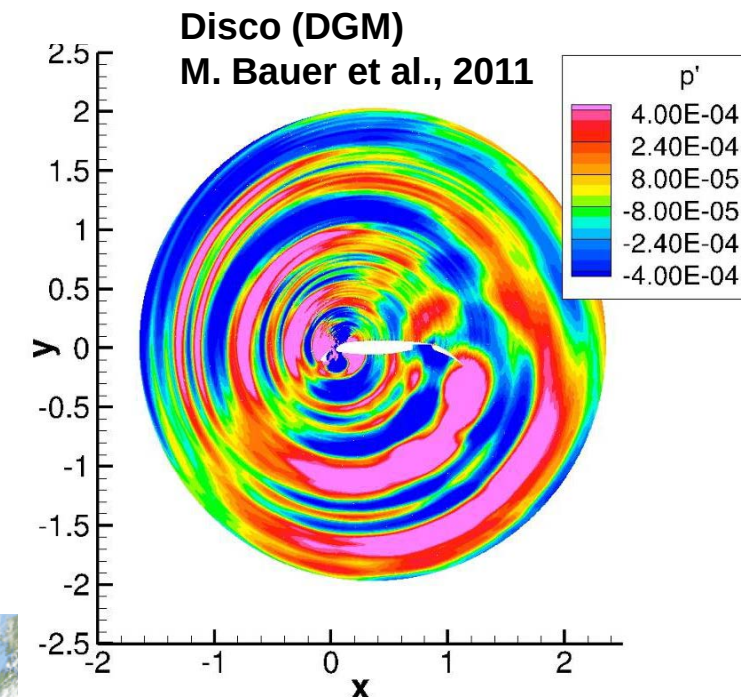
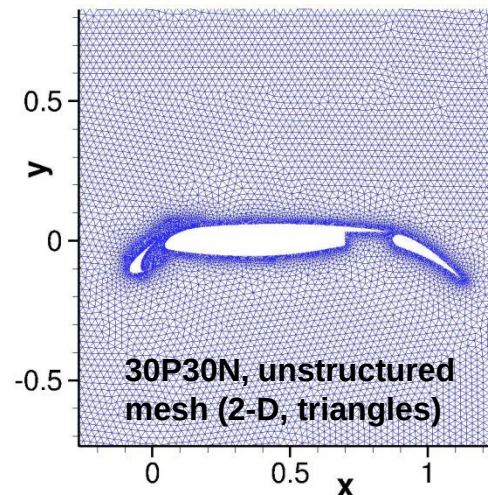
Extension to unstructured CAA, 30P30N high-lift airfoil

2

- PIANO code of DLR based on structured multi-block (SMB) meshes + finite differences
- Dispersion Relation Preserving (DRP) scheme (Tam & Webb 1993)
- LEE, APE, NLEE, NLPE



- Simplified mesh generation based on unstructured meshes with high-order methods
- Discontinuous Galerkin methods for CAA (Bauer et al. 2011)
- LEE and APE



Governing equations

- **Navier-Stokes equations in primitive variable notations**

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} + \frac{\nabla p}{\rho} = \frac{\nabla \cdot \boldsymbol{\tau}}{\rho},$$

$$\frac{\partial p}{\partial t} + \mathbf{v} \cdot \nabla p + \gamma p \nabla \cdot \mathbf{v} = (\gamma - 1)(\boldsymbol{\tau} \cdot \nabla) \cdot \mathbf{v} - (\gamma - 1) \nabla \cdot \mathbf{q}.$$

Flow field decomposition into a steady and fluctuating part

$$\rho = \rho^0 + \rho', \quad \mathbf{v} = \mathbf{v}^0 + \mathbf{v}', \quad p = p^0 + p', \quad \boldsymbol{\tau} = \boldsymbol{\tau}^0 + \boldsymbol{\tau}', \quad \mathbf{q} = \mathbf{q}^0 + \mathbf{q}'.$$



- Viscous PENNE(*) equations with steady base flow (“NLPE”) (**)

$$\begin{aligned}\frac{\partial \rho'}{\partial t} + \mathbf{v} \cdot \nabla \rho' + \mathbf{v}' \cdot \nabla \rho^0 + \rho \nabla \cdot \mathbf{v}' + \rho' \nabla \cdot \mathbf{v}^0 &= r_1^0, \\ \frac{\partial \mathbf{v}'}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v}' + (\mathbf{v}' \cdot \nabla) \mathbf{v}^0 + \frac{\rho'}{\rho} (\mathbf{v}^0 \cdot \nabla) \mathbf{v}^0 + \frac{\nabla p'}{\rho} &= \frac{\nabla \cdot \boldsymbol{\tau}'}{\rho} + \frac{\rho^0}{\rho} r_2^0, \\ \frac{\partial p'}{\partial t} + \mathbf{v} \cdot \nabla p' + \mathbf{v}' \cdot \nabla p^0 + \gamma p \nabla \cdot \mathbf{v}' + \gamma p' \nabla \cdot \mathbf{v}^0 &= \\ &(\gamma - 1)[(\boldsymbol{\tau}' \cdot \nabla) \cdot \mathbf{v} + (\boldsymbol{\tau}^0 \cdot \nabla) \cdot \mathbf{v}' - \nabla \cdot \mathbf{q}'] + r_3^0.\end{aligned}$$

with residual turbulent viscous and heat fluxes

$$\begin{aligned}r_1^0 &= 0, \\ r_2^0 &= -\frac{\nabla \cdot \boldsymbol{\tau}^{t0}}{\rho^0}, \\ r_3^0 &= -(\gamma - 1)[(\boldsymbol{\tau}^{t0} \cdot \nabla) \cdot \mathbf{v}^0 - \nabla \cdot \mathbf{q}^{t0}].\end{aligned}$$

(*) PENNE = Perturbed Nonconservative Nonlinear Equations, L. N. Long. *AIAA Paper 2000-1998*, 2000.

(**) primitive variables approach of NLDE (Morris et al., JCP 133, 1997; Terracol, Flow, Turb. & Comb, 77, 2006)



- No-slip boundary condition

Physics requires: $\mathbf{v}_{wall} = 0$.

Introducing $\boldsymbol{\sigma} = \boldsymbol{\tau} - p\mathbf{I}$ into momentum equations of Navier-Stokes equations yields

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = \frac{\nabla \cdot \boldsymbol{\sigma}}{\rho}.$$

To satisfy $\frac{\partial \mathbf{v}}{\partial t} \stackrel{!}{=} 0$, $\nabla \cdot \boldsymbol{\sigma} \stackrel{!}{=} 0$

For viscous PENNE equations:

$$\sigma'_{ij} = \tau'_{ij} - p' \delta_{ij}$$

$$u^0 = v^0 = w^0 = 0 \quad (\text{from RANS background flow simulation})$$

$$u' = v' = w' = 0 \quad (\text{to be enforced at end of each time step})$$

Realized via 3 ghost values of $\boldsymbol{\sigma}$ on ghost points beneath wall

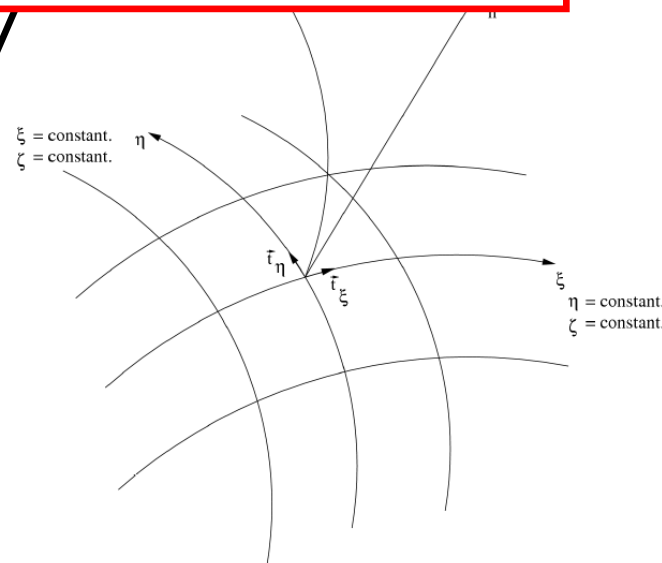


Fig. 3 Sketch of curvilinear coordinates w.r.t. wall boundary of a body fitted grid.



- Adiabatic boundary condition

For an adiabatic wall, heat flux through the wall must be zero, i.e.

$$\vec{q} \cdot \vec{n} = 0.$$

The thermal equation of state reads

$$\frac{dp}{p} - \frac{d\rho}{\rho} = \frac{dT}{T}.$$

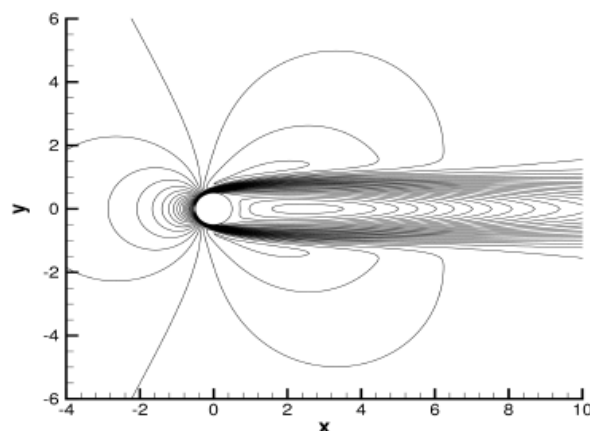
After decomposition and rearrangement

$$\frac{\partial \rho'}{\partial n} = n_j \frac{\partial \rho'}{\partial x_j} = -n_j \left[-\frac{\rho}{p} \frac{\partial p'}{\partial x_j} - \frac{\rho'}{p} \frac{\partial p^0}{\partial x_j} + \frac{p'}{p} \frac{\partial \rho^0}{\partial x_j} \right],$$

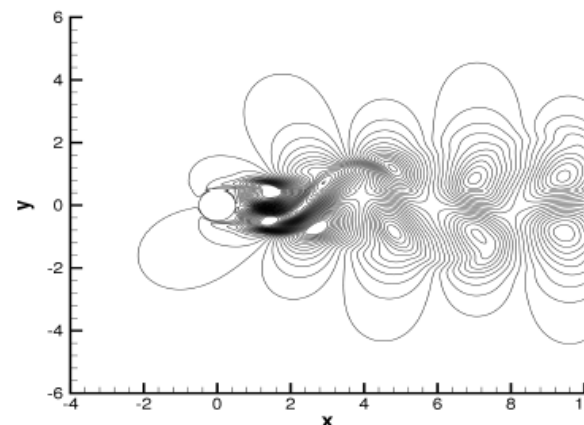
$$\rho'_{i,-1,k} = \frac{1}{c_0} \left\{ -\sum_{m=0}^5 c_{m+1} \rho'_{i,m,k} + \left[\frac{\partial \rho'}{\partial n} - \sum_{l=1}^3 n_l \left(J_{1l} \frac{\partial \rho'}{\partial \xi} + J_{3l} \frac{\partial \rho'}{\partial \zeta} \right) \right] / \sum_{l=1}^3 n_l J_{2l} \right\}.$$



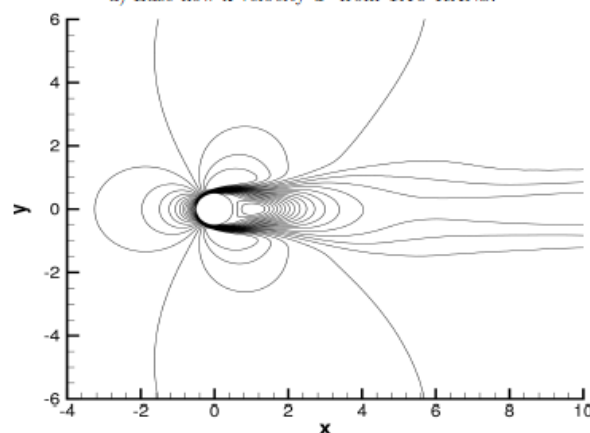
CAA simulation of flow around a circular cylinder, $Re=150$, $M=0.1$, 0.2 , and $0.3(*)$



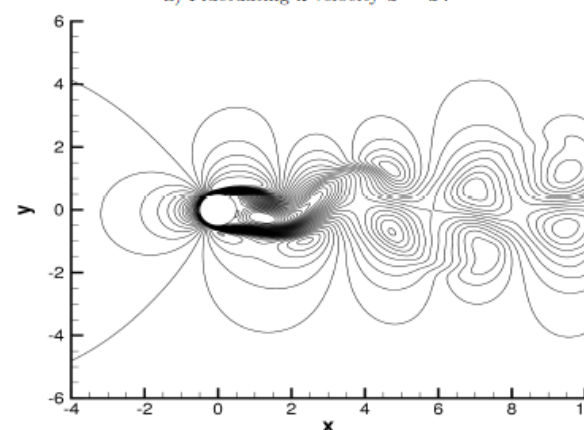
a) Base flow x-velocity u^0 from TAU RANS.



a) Fluctuating x-velocity $u' - \bar{u}$.



b) Mean x-velocity $u^0 + \bar{u}$ with added mean contribution from PIANO.



b) Total x-velocity $u^0 + u'$.

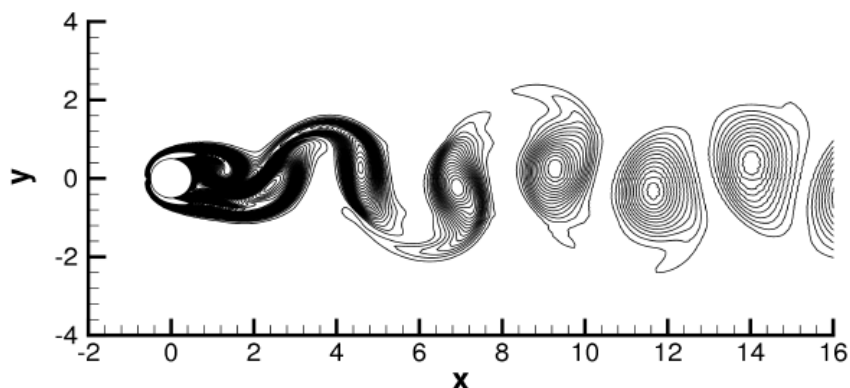
Base and mean-flow contour lines.

Fluctuating and total-flow contour lines.

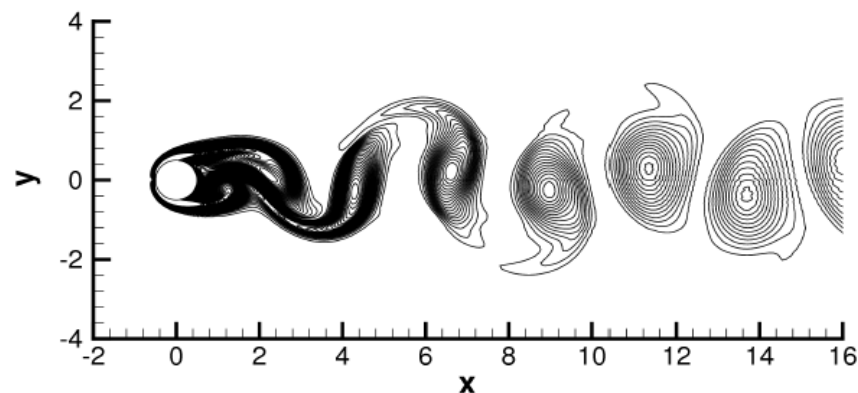
(*) O. Inoue and N. Hatakeyama, *JFM*, Vol(471):285–314, 2002.



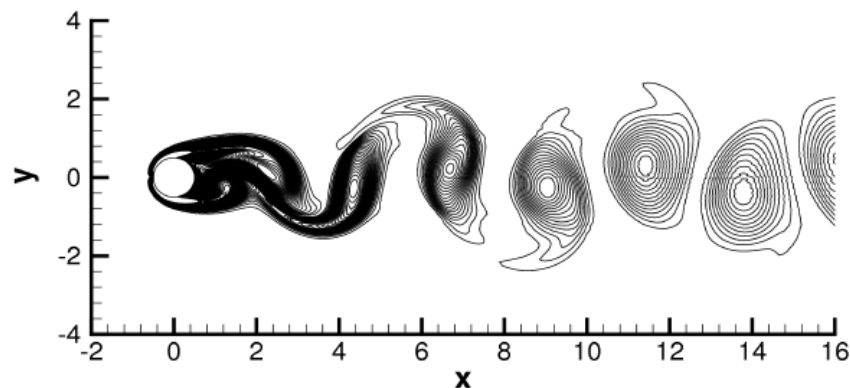
Numerical verification for circular cylinder simulation



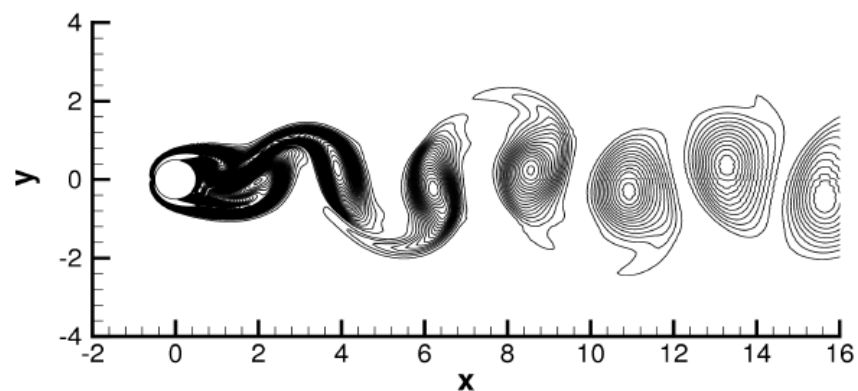
a) $t = 1511.25$.



a) $t = 1507.5$.



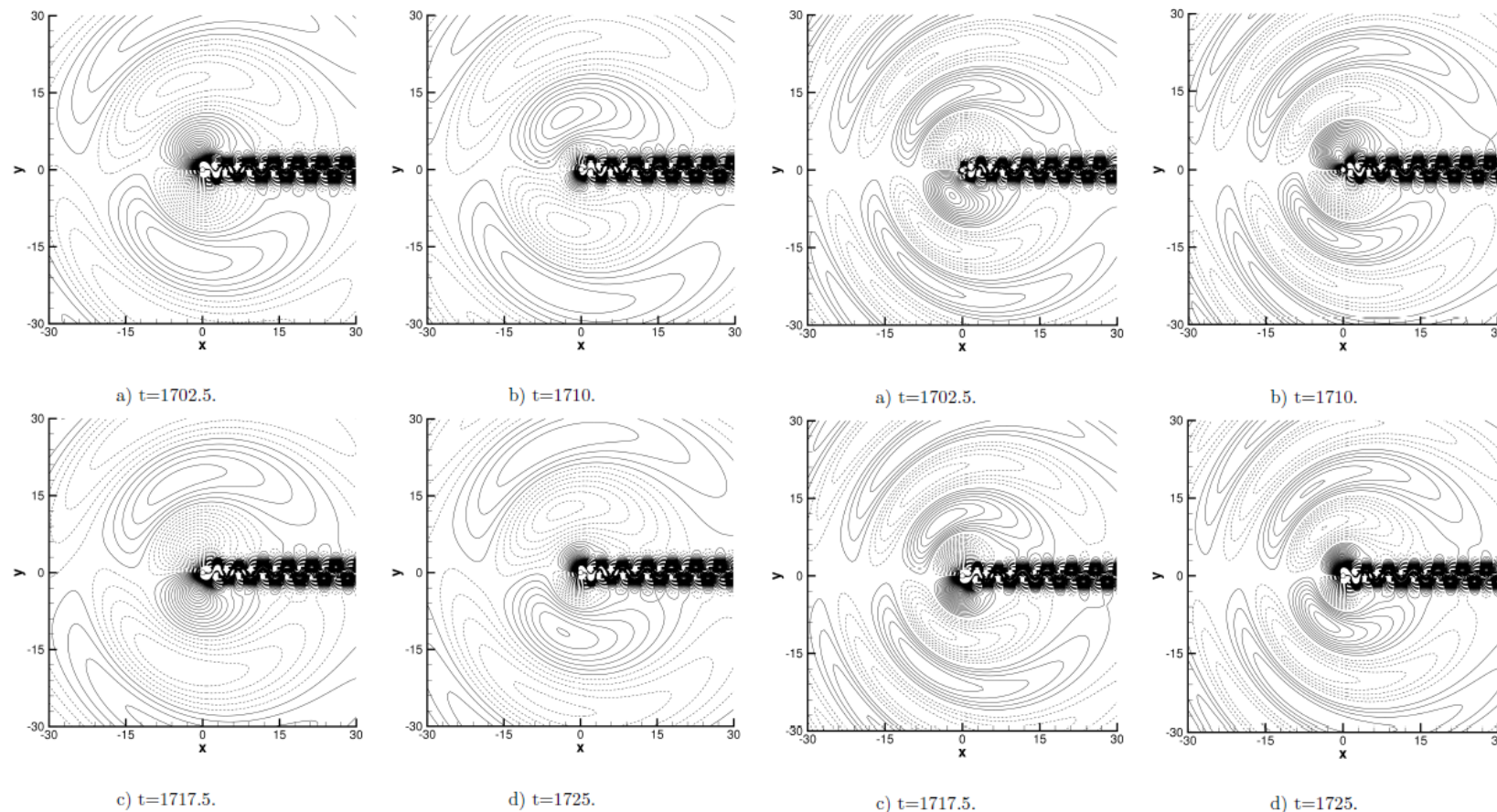
b) $t = 1526.25$.



b) $t = 1511.25$.

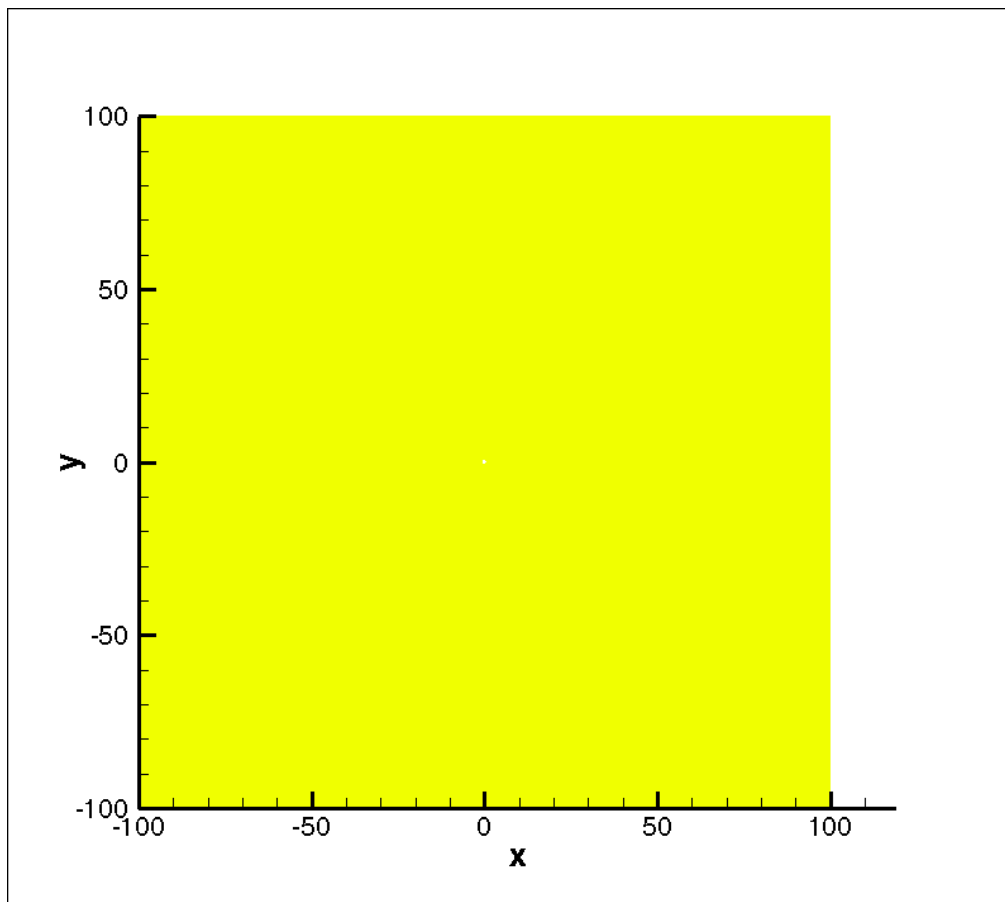
Time development of vorticity field for $Re = 150$, $M = 0.2$ (left), $M = 0.3$ (right).



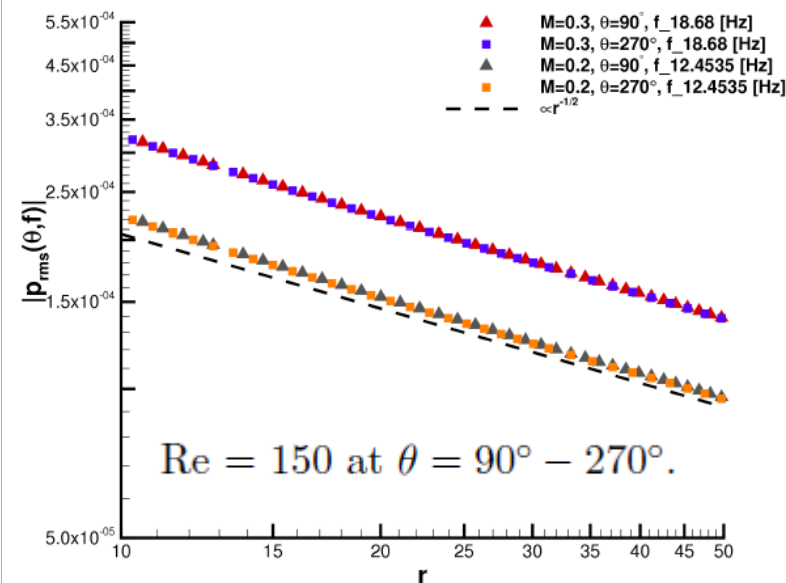


Time development of pressure fluctuation for $Re = 150$, $M = 0.2$ (left), $M = 0.3$ (right), $St=0.176$ ($M=0.1$), $St=0.185$ ($M=0.2$), $St=0.190$ ($M=0.3$) (Inoue: $M=0.2$, $St=0.185$)

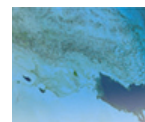
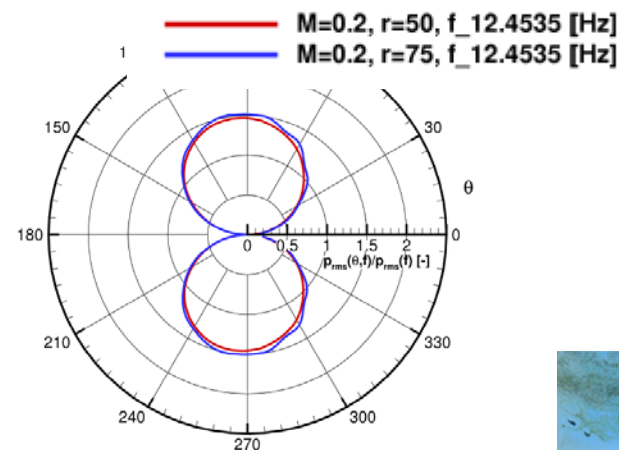
CAA simulation of flow around a circular cylinder



Time development of pressure fluctuation for
 $Re = 150$, $M = 0.2$



Decay of pressure peaks for $M = 0.2-0.3$,



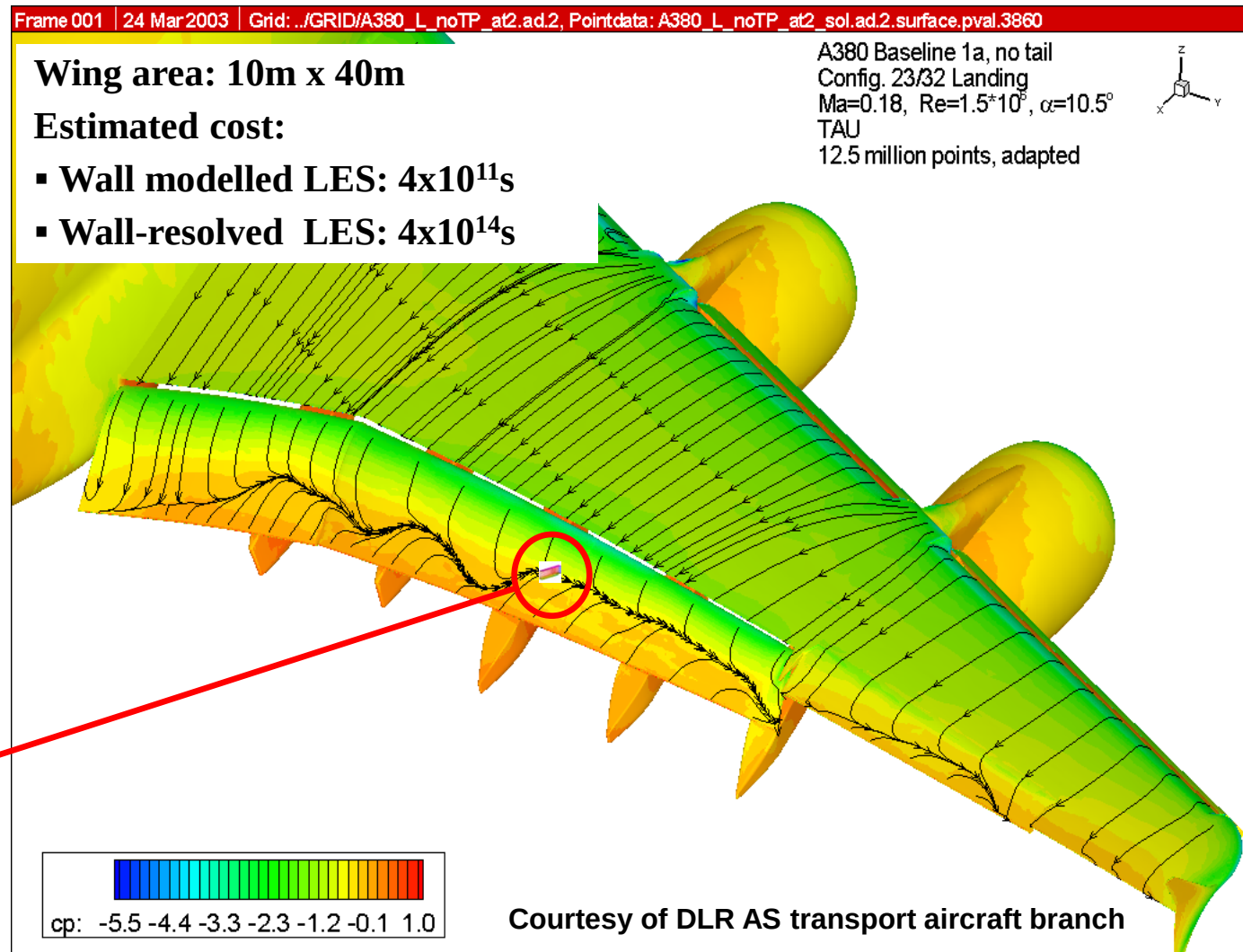
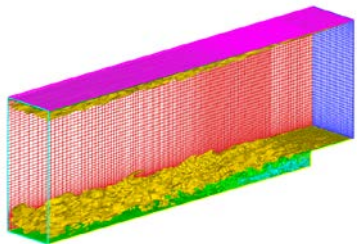
General motivation of stochastic noise modeling

Estimation of computational cost for A380 take-off/landing configuration

Attached boundary layer flow with separation on flap of a wing at high-lift
„approximated“ by flow over a backward facing step.

LES with wall-functions
Surface: 0.38m x 0.05m

Cost: 10⁶s on single CPU
(= 20days)

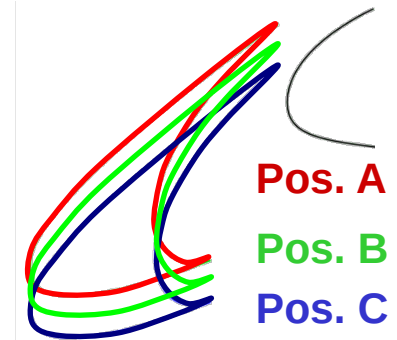


Tobias Knopp

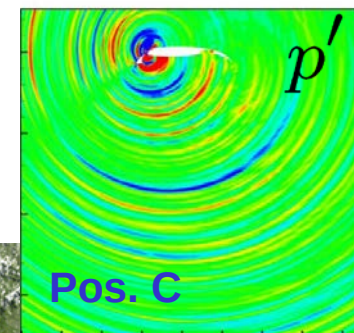
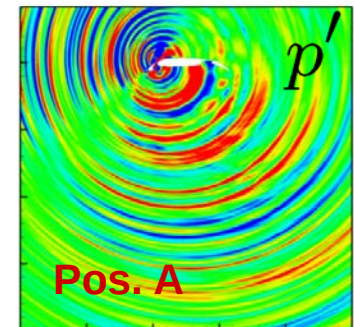
General motivation of stochastic noise modeling

Need for fast design-to-noise simulation tools for turbulence related noise generation

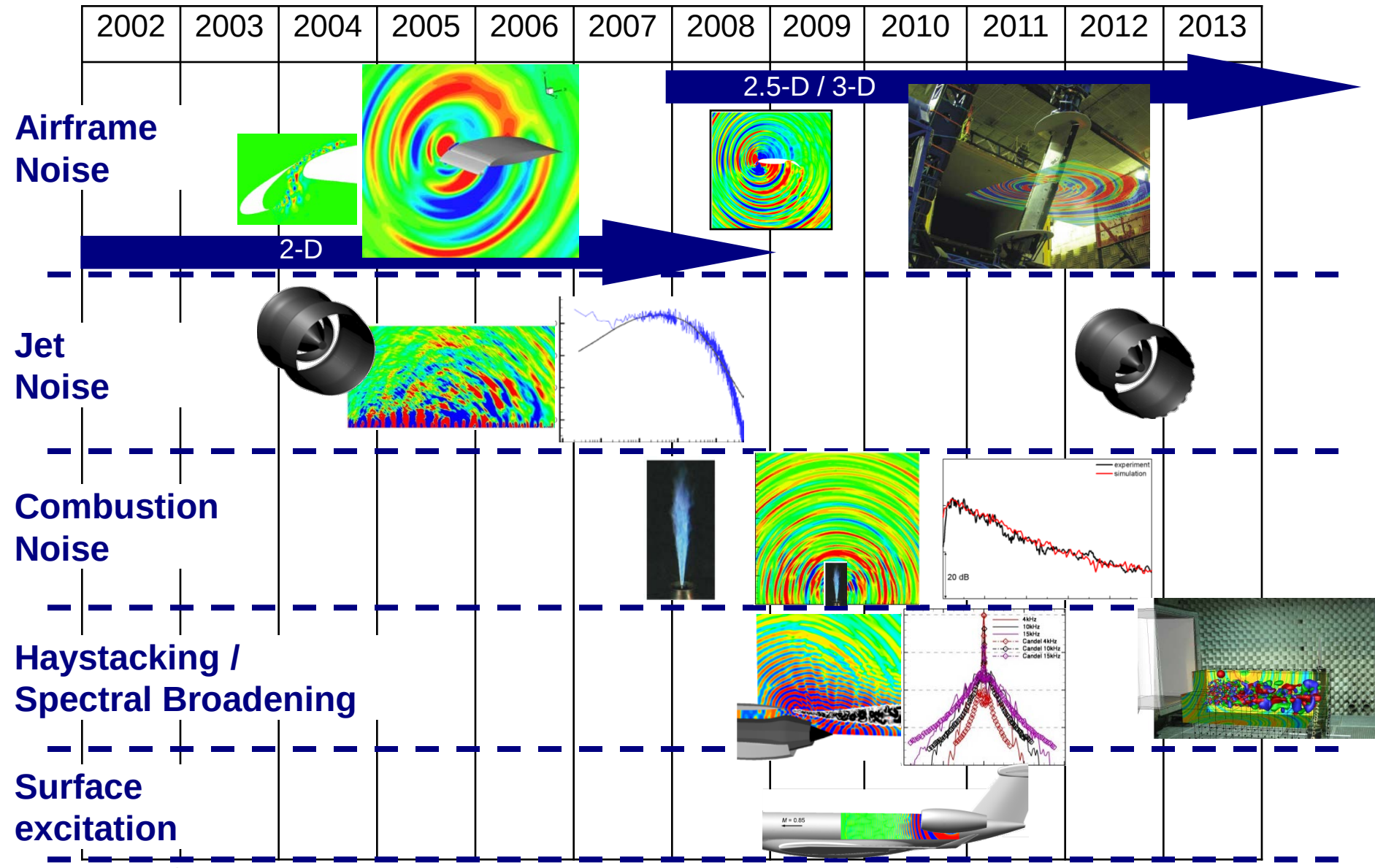
- Tools need for the fast simulation of turbulence related broadband noise (BBN) for aeroacoustic design purposes (design-to-noise) in an industrial environment
- Short turnaround times needed
- 'First principle based method' needed, which is applicable to small standard variations but also to new designs
- Reynolds Averaged Navier-Stokes (RANS) equations standard tool in aerodynamics today
- Scale resolving simulation (DNC, DNS, LES, DES+FW-H) useful to study noise and understand new noise source mechanism but still too expensive for aeroacoustic design purposes today and in the near future
- In the meantime need for a RANS equivalent in CAA for BBN predictions



Example: slat setting variation: impact on aerodynamics and noise



Stochastic noise prediction methods at DLR



Statistical Noise Theory (SNT)

Two-point cross-correlation function and sound spectrum

Spectrum of p'

Acoustic propagation

$$S(\mathbf{x}, \omega) = \iiint \hat{G}(\mathbf{x}, \mathbf{x}_1, \omega) \hat{G}^*(\mathbf{x}, \mathbf{x}_1 + \mathbf{r}, \omega) \times$$

This one is modeled empirically, i.e. based on measured shapes

$$\times \langle q_s(\mathbf{x}_1, t) q_s(\mathbf{x}_1 + \mathbf{r}, t + \tau) \rangle e^{i\omega\tau} d\tau d^3\mathbf{x}_1 d^3\mathbf{r}$$

Two-point cross-correlation of turbulent source



Statistical Noise Theory as the Basis of Stochastic Source Models

Historical Overview

1952

Lighthill
Ribner

1977

Mani, Balsa & Gliebe

1992

Khavaran, Krejsa & Kim

1999

Tam & Auriault

2003

Harper-Bourne

2004

Morris & Bouluriaan

2005

Khavaran, Bridges & Georgiadis

2006

Raizda & Morris

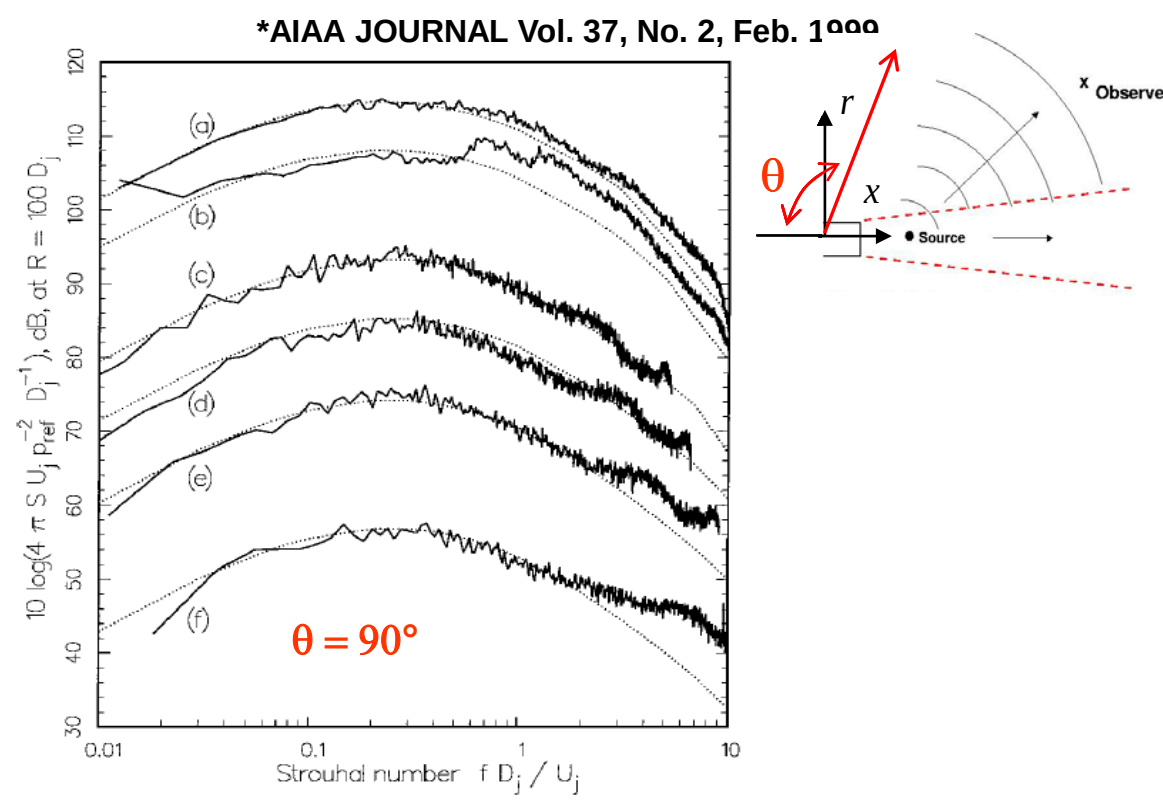
2010

Karabasov et al.

2011

Leib & Goldstein

Tam & Auriault 1999*: adjoint LEE (spectral space) + equivalent source vs. Measurements



Quintessence: SNT are capable to capture general broadband trends quite well (but: for simple jet nozzles and mainly under 90°)

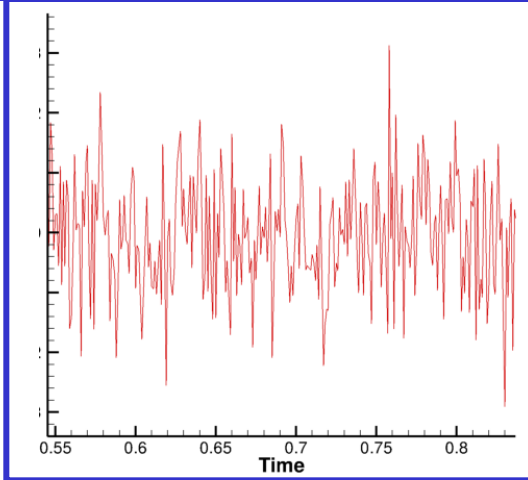


Stochastic Methods: SNT solved in time w. state-of-the-art CAA

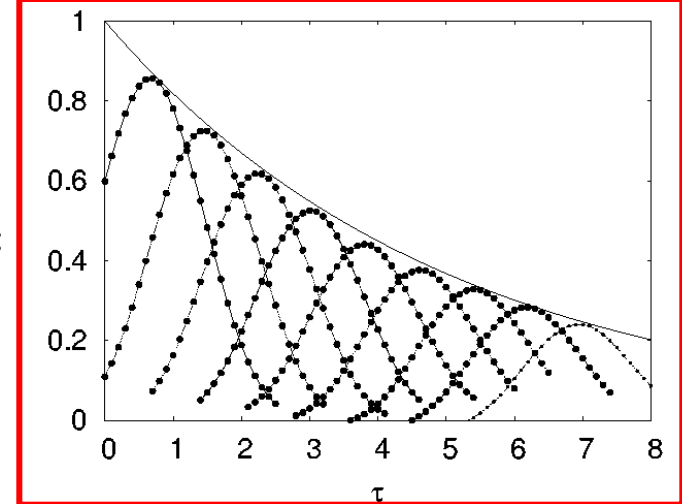
Principle

- Realize synthetically fluctuating source with desired two-point statistics

$$q_s(\mathbf{x}, t) =$$



$$\langle q_s q_s \rangle =$$



- Solve acoustic analogy with fluctuating source in the time domain

Acoustic propagation
(wave operator)

$$p' = q_s$$

- Sample pressure data and compute sound spectra
- Sound spectrum corresponds to that of SNT if
 - acoustic propagation model is the same
 - two-point cross-correlation model is identical

'Don't believe it!
Prove it to me!!!!'



Stochastic Methods in CAA

Historical Overview

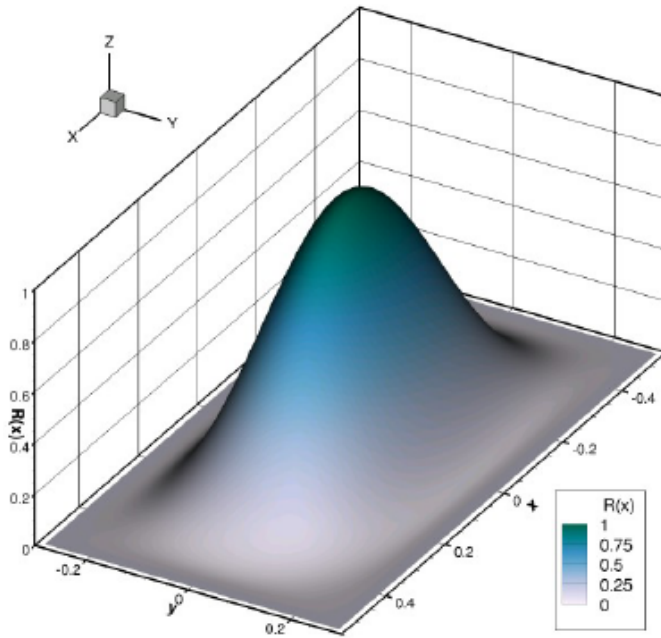
2012	Cozza et al.	→ <i>ESDF</i> , cross-correlation method
2011	Dieste & Gabard	→ Cyclostationary turbulence, <i>RPM</i>
2011	Casalino et al.	→ <i>SNGR</i> type of model applied to NACA0012 trailing edge noise
2010	Dieste & Gabard	→ Evolving turbulence model, <i>RPM</i>
2009	Siefert & Ewert	→ Sweeping evolving turbulence model and faster filter for <i>FRPM</i>
2009	Dieste & Gabard	→ Random particle method, cross-correlation model
2007	Ewert	→ Fast Random Particle-Mesh Method (<i>FRPM</i>) (increased efficiency)
2006	Ewert	→ Random Particle-Mesh Method (<i>RPM</i>) - cross-correlation model for CAA
2005	Ewert et al.	→ <i>SDF</i> , first stochastic cross-correlation model for CAA
2004	Bauer et al.	→ <i>SNGR</i> trailing edge noise prediction operational
2003	Billson et al.	→ Langevin equation based evolving turbulence for <i>SNGR</i>
2000	Kallitzin et al.	→ Attempt to model trailing edge noise with <i>SNGR</i>
1996	Bailly et al.	→ Stochastic Noise Generation and Radiation (<i>SNGR</i>) approach – Fourier space based
1994	Bechara et al.	→ Fourier space based approach for CAA
⋮	⋮	⋮
1970	Kraichnan	→ Spatial Fourier mode model in moving frame



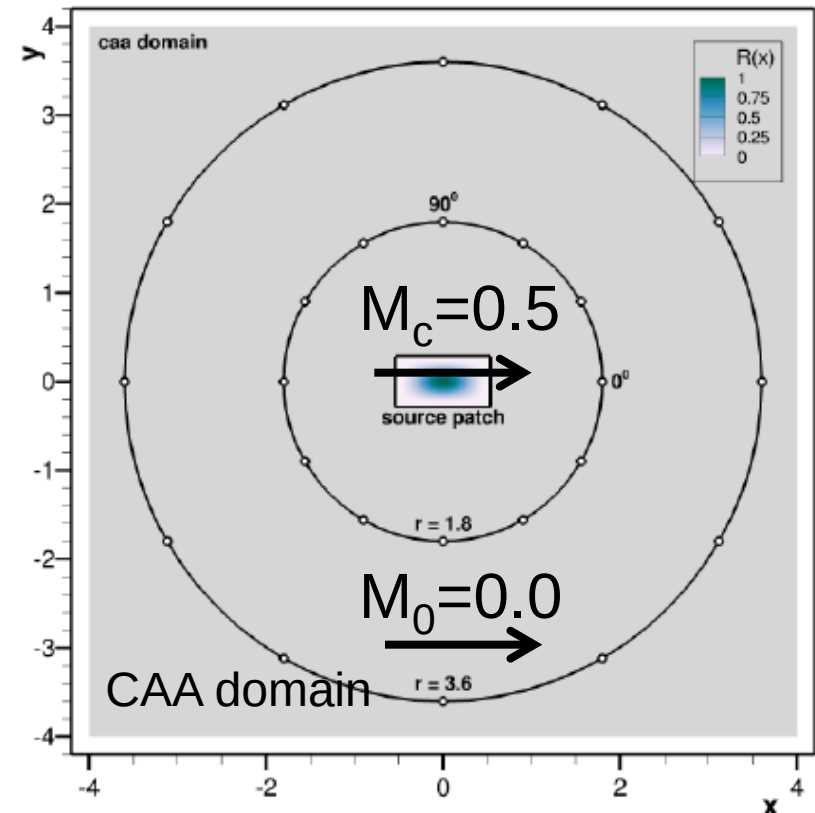
(F)RPM synthetic turbulence generator of DLR

2-D Test problem and comparison FRPM vs. analytical solution

- Verification of FRPM with analytical solution and absolute levels
- CAA-Domain: $u_0=0$ (sound propagation in medium at rest)
- FRPM Patch: $u_c=0.5$
 - Source variance distribution defined by cosine function
 - Tam & Auriault source model with exponential temporal decorrelation
- Comparison with analytical far-field spectrum

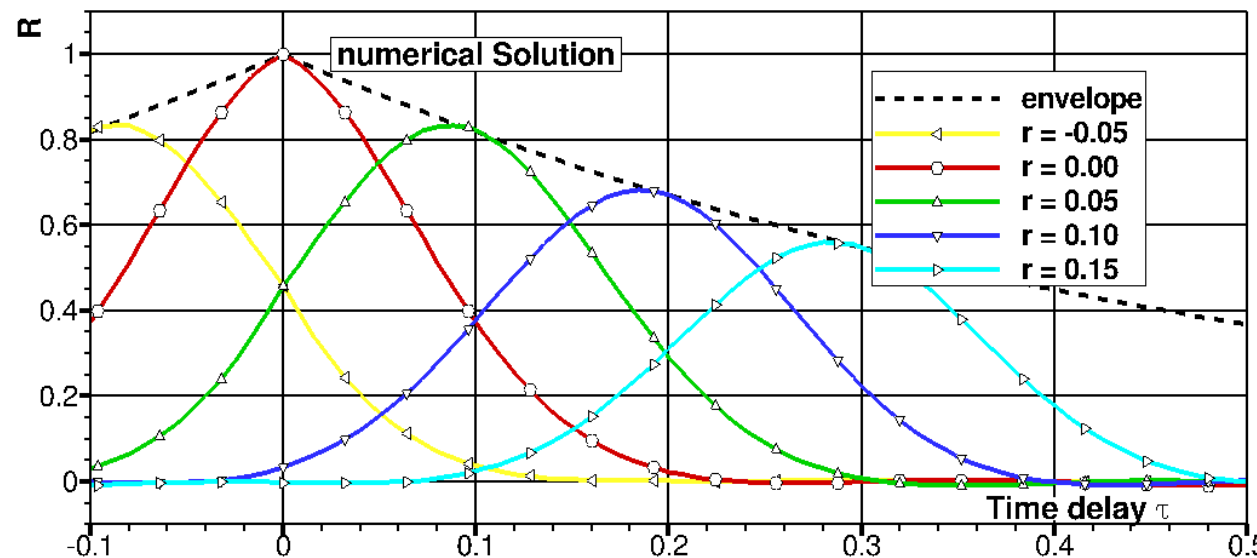
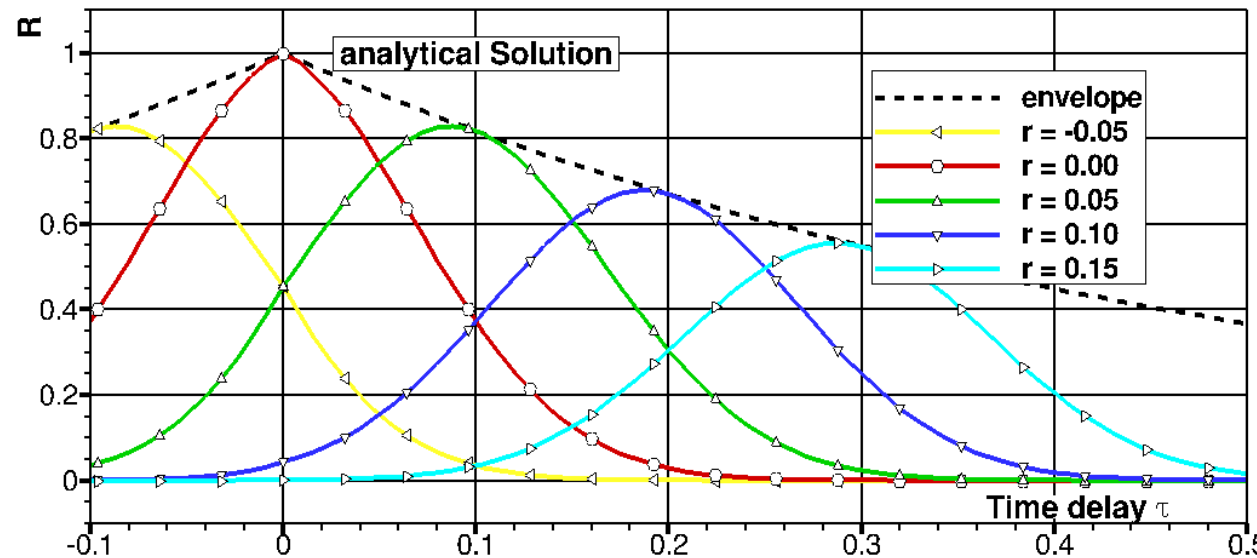


Source patch with source distribution



2-D Test Problem, FRPM based Solution

Evaluation of FRPM cross-correlation

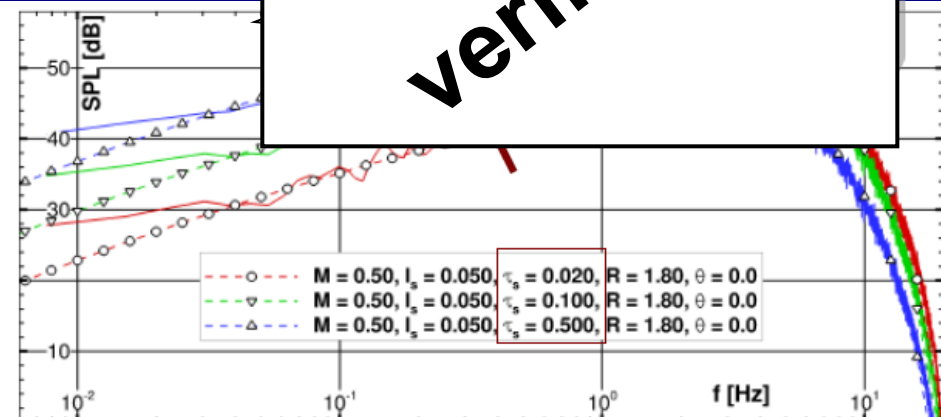
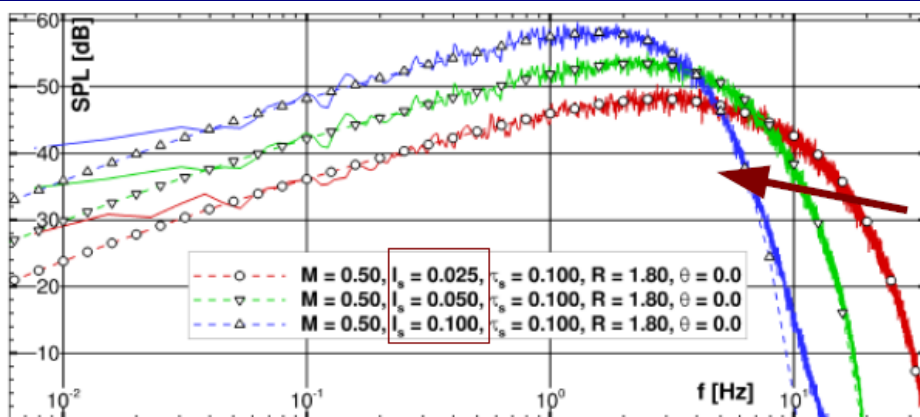


• time-scale

$$\frac{u_c \tau_s}{l_s} \approx 4.0$$

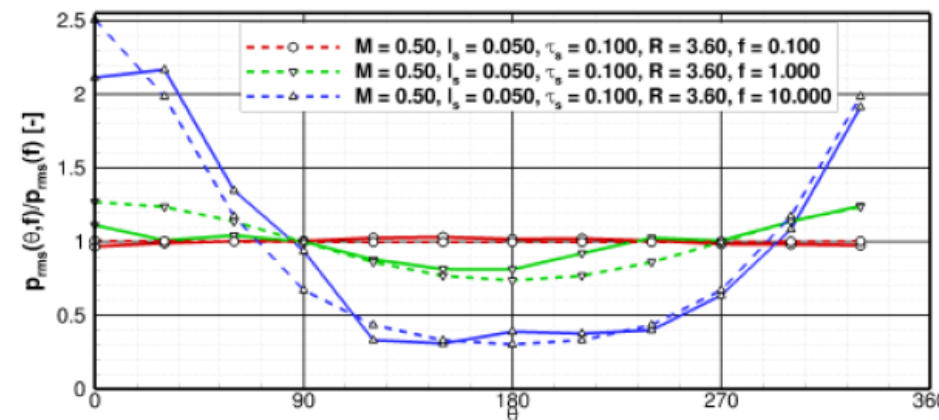
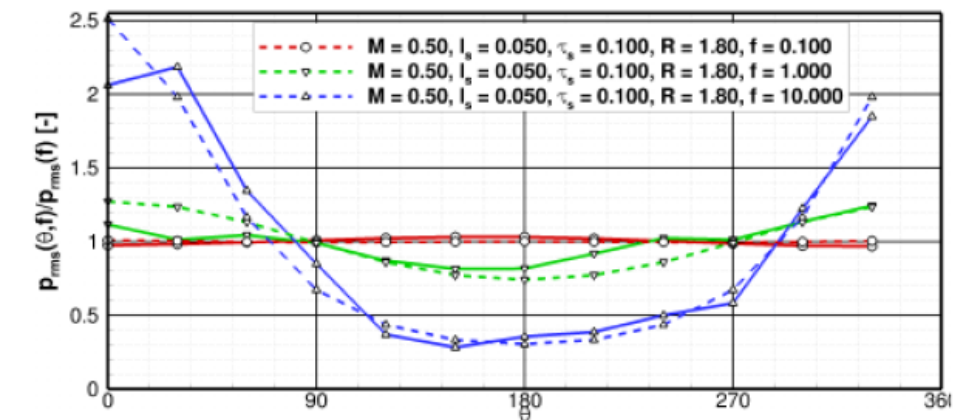
2-D Test Problem, FRPM based Solution

Evaluation of FRPM cross-correlation



Length scale variation, polar angle $\theta=0^\circ$ (downstream direction)

Time scale variation, polar angle $\theta=0^\circ$ (downstream direction)



Radial distance $R=1.8$

Radial distance $R=3.6$

Directivity, $M_c=0.5$, $l=0.05$, $\tau_s=0.1$, $R=1.8$ and $R=3.5$

—, FRPM+CAA, , Analytical



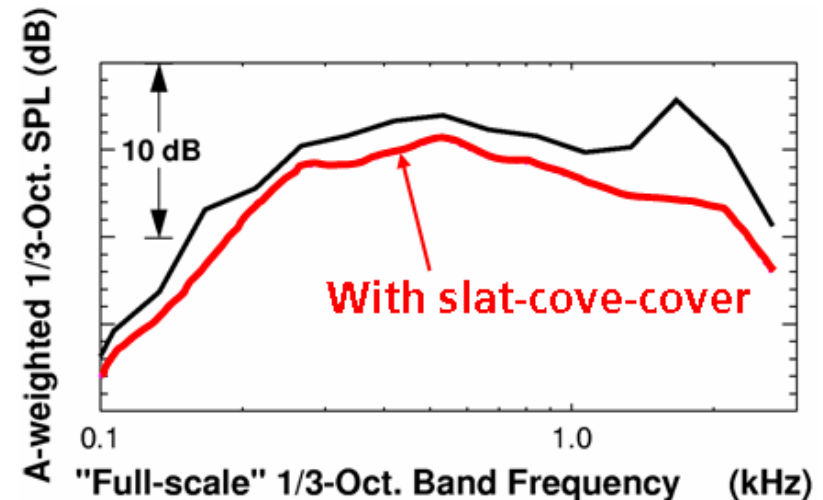
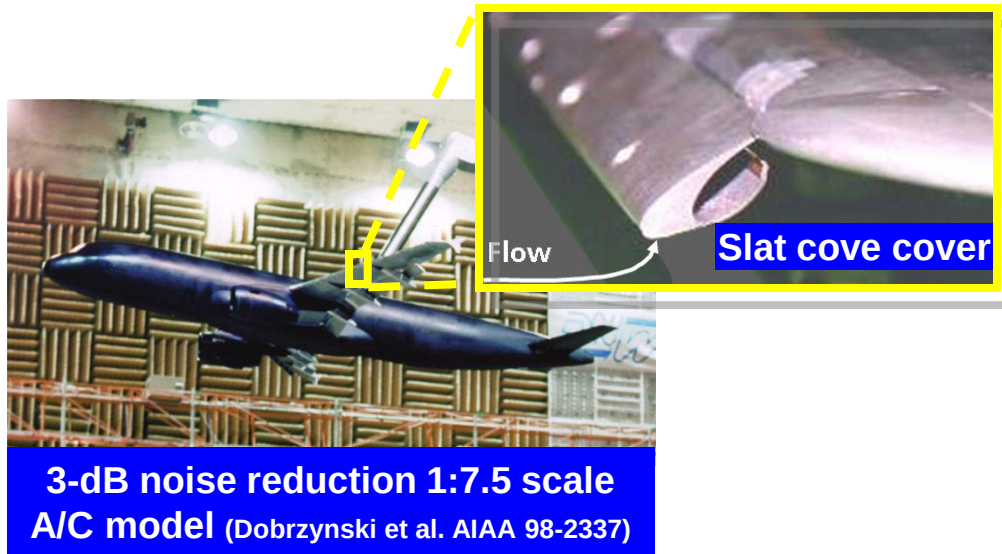
Attila Wohlbrandt



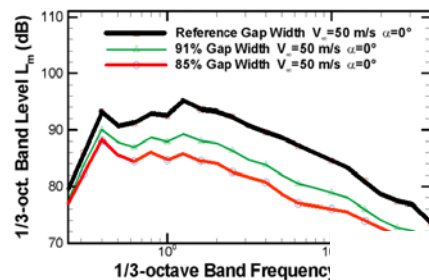
Slat Noise Simulations

Slat noise and slat noise reduction measures

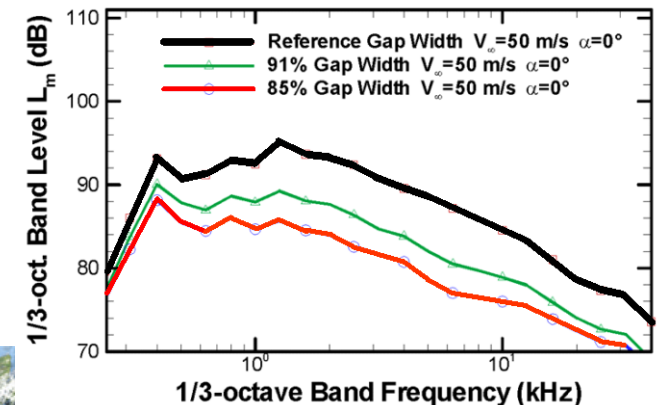
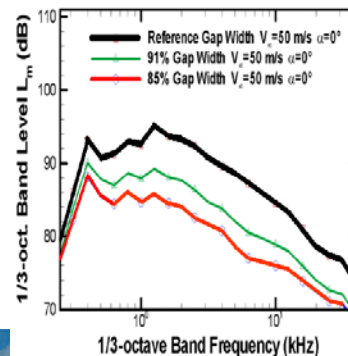
1. Slat-cove cover (filler) to reduce kin. energy of turbulence at the TE



2. Determine low noise slat setting with acceptable loss in lift

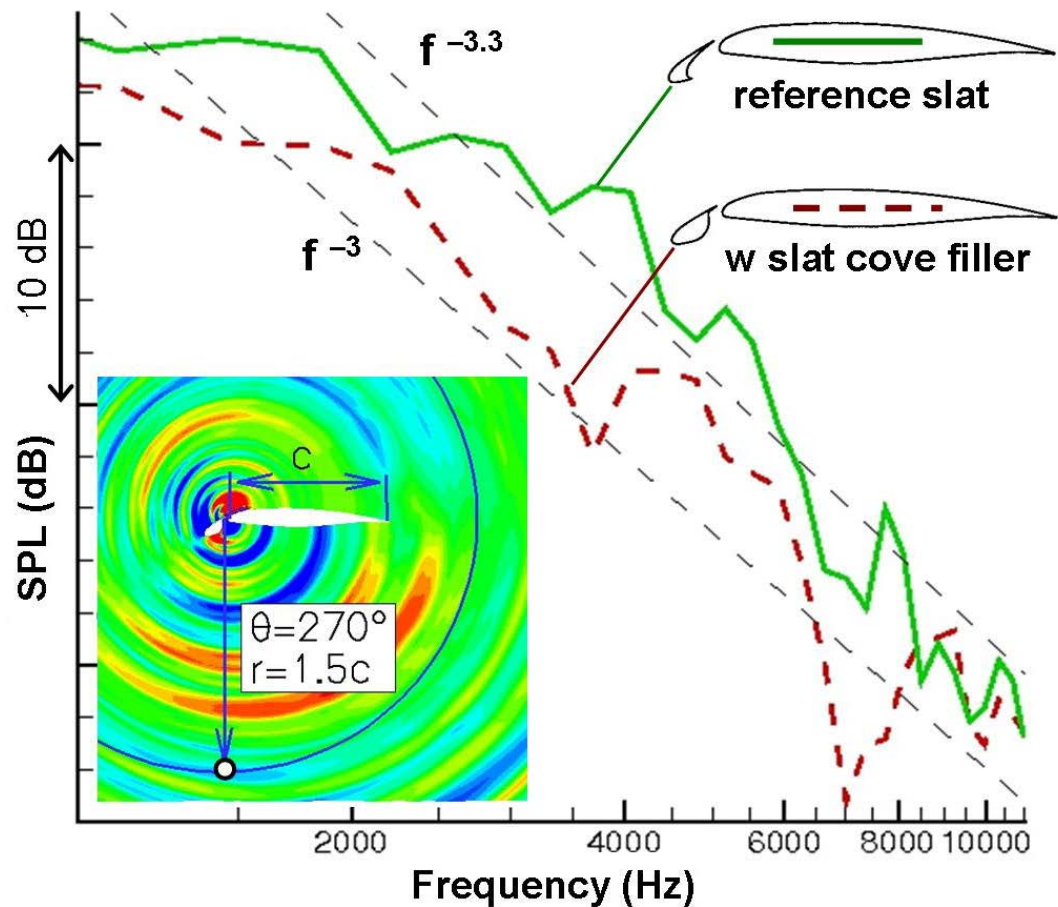
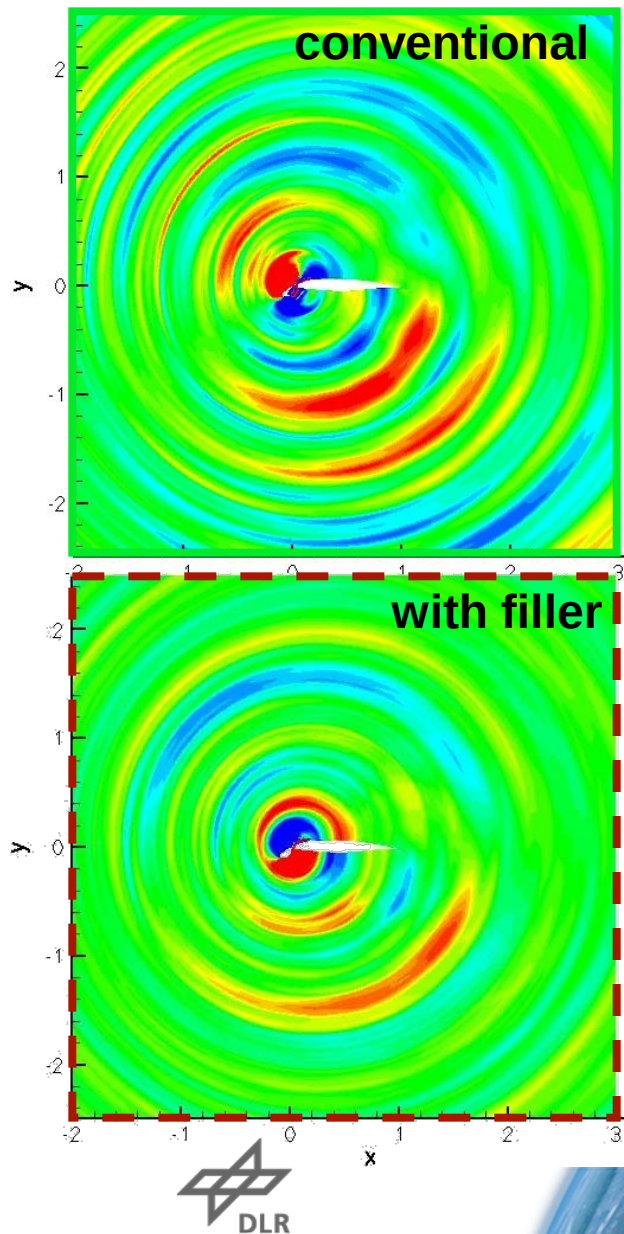
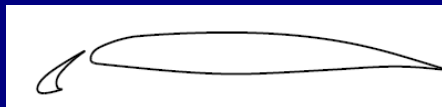


M. Pott-Pollenske



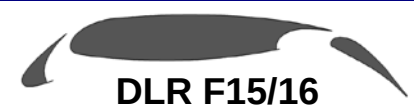
Slat Noise Simulations

Slat cove filler effect on broadband noise (German national project FREQUENZ)



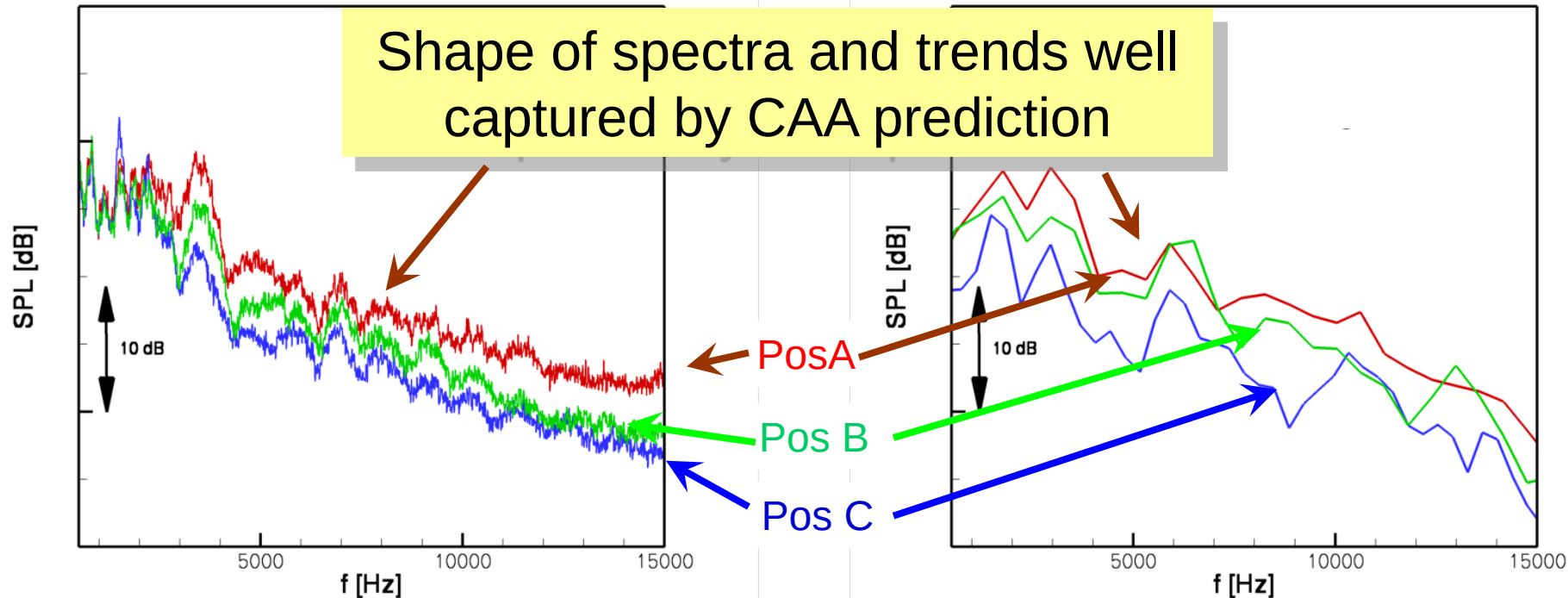
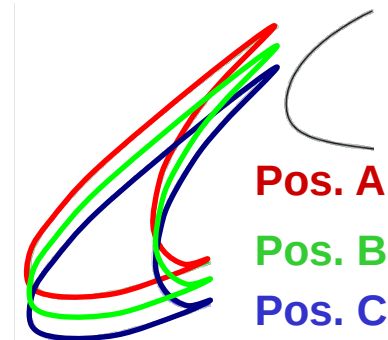
CFD (RANS): TAU (Airbus)
CAA: PIANO (DLR)

Slat Noise Simulations



Slat gap variation and experimental validation (EU TIMPAN)

- *Narrow band spectra at 287° (normal to shear layer)*
- *Prediction made prior to measurements*
- *Prediction based on 0.2sec real time sample, yielding lower frequency resolution and/or larger wiggles*



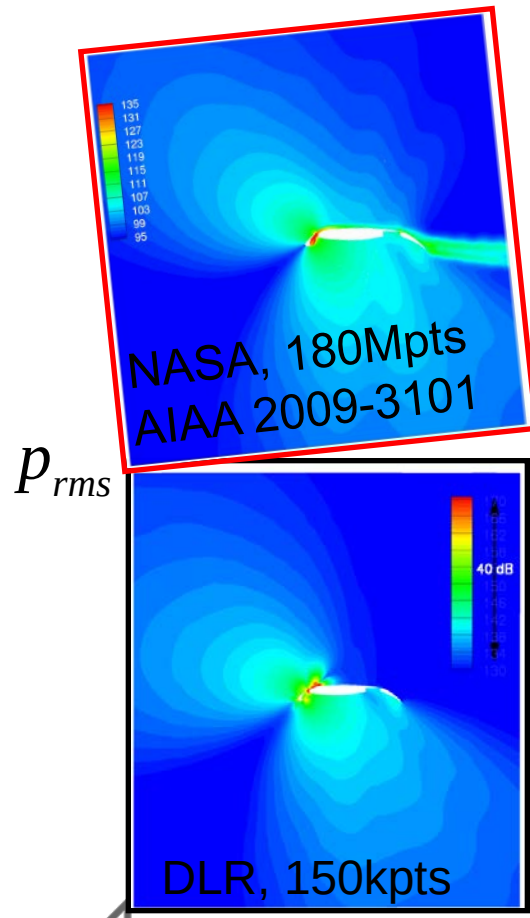
Narrow Band Spectra $\theta=287^\circ$ (below airfoil)

Airframe noise of high lift airfoil 30P30N

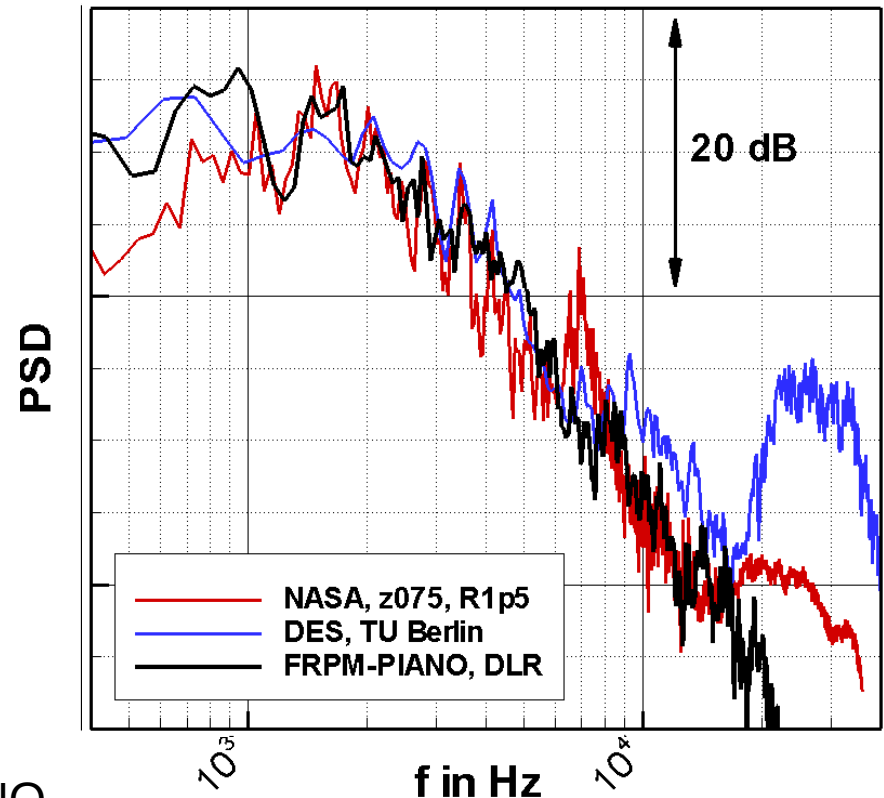
-Comparison of stochastic approach
(PIANO) with other groups



290° w.r.t. flow

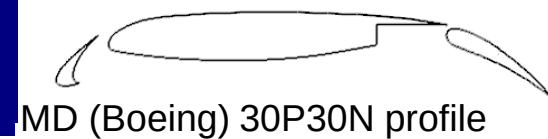


flow: TAU
sound: PIANO

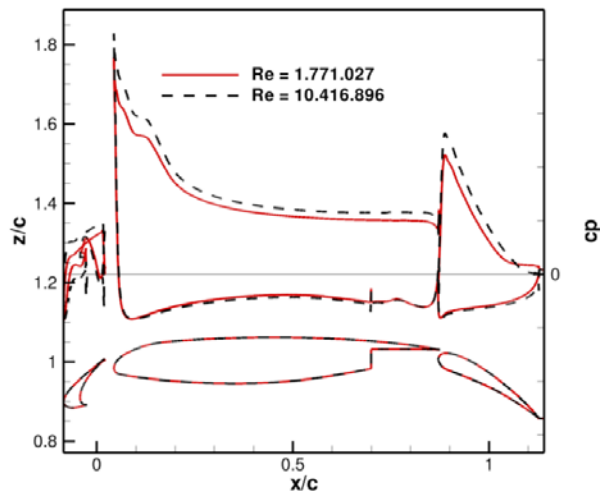


Slat Noise Simulations

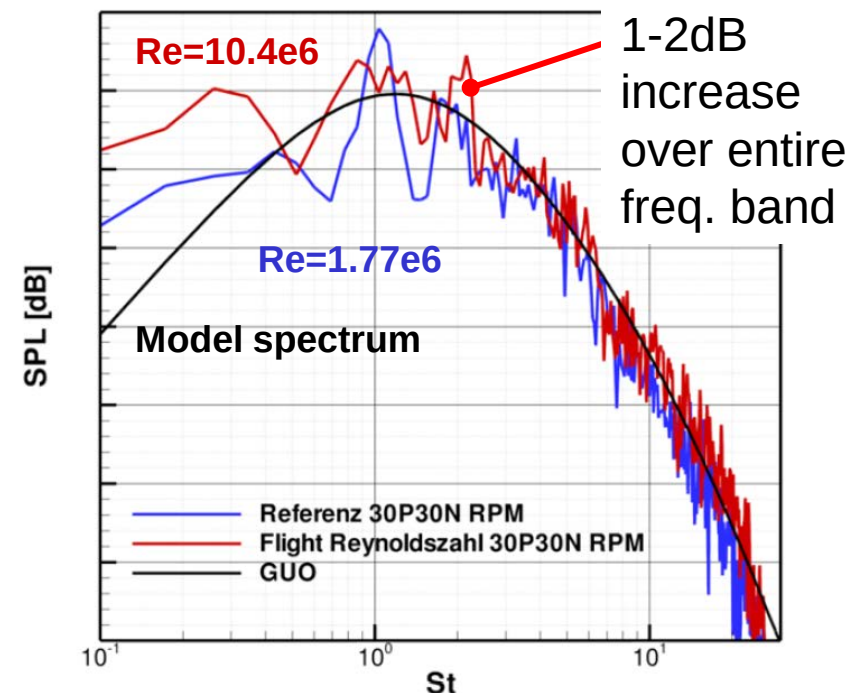
Further predictions, 30P30N high-lift airfoild



- Reynolds number effect ($Re=1.7e6$ vs. $10e6$, Aeronext)
- Extension of CAA simulation capability to unstructured meshes (DG)
- Comparison with scale resolving simulation
- 3-D Sweep effect
- Validation with low Re-number measurements (EU Valiant, $Re=7e5$)
- Validation with high Re-number measurements (OPENAIR, FTEG, $Re=5e6$)
- Source anisotropy and modeling effects
- Understanding of source mechanisms?



Re-no. effect on C_p distribution from RANS



CAA predicted effect on spectrum and comparison with model spectrum of Guo

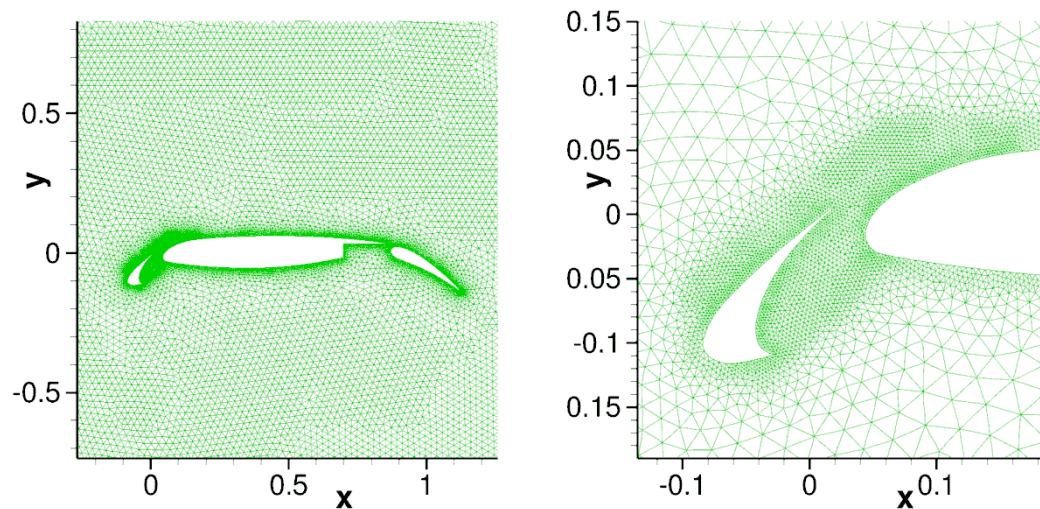


McDonnell Douglas (now Boeing) 30P30N profile

Practical application of the DGM

Slat noise of 30P30N high-lift airfoil configuration [Bauer 2011]

$L = 0.46$ m, $Ma_\infty = 0.17$, $Re \approx 1\,700\,000$, $\alpha = 4^\circ$
spatial discretization of APE (2D) through a DGM using
Lagrange polynomials of degree $p=3$
unstructured, triangular DG grid: $E = 58.774$, $f_{limit} \approx 15$ kHz:



Advantages:

- **local** grid refinement
- **automatic** generation (e.g. with CENTAUR)
- **no grid singularities**



Slat Noise Simulations

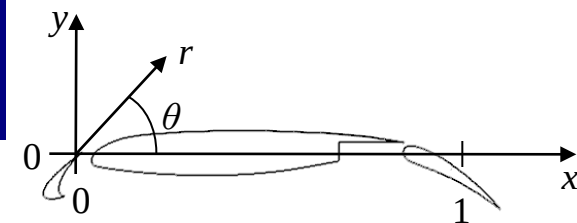
Comparison of noise predictions 30P30N ($r=1.5c$)

- DDES+FW-H, TU-B, 3-D, 30Mpts
- RANS/LES+FW-H NASA, 3-D, 62Mpts
- CAA+FRPM 2-D (DLR), 150kpts

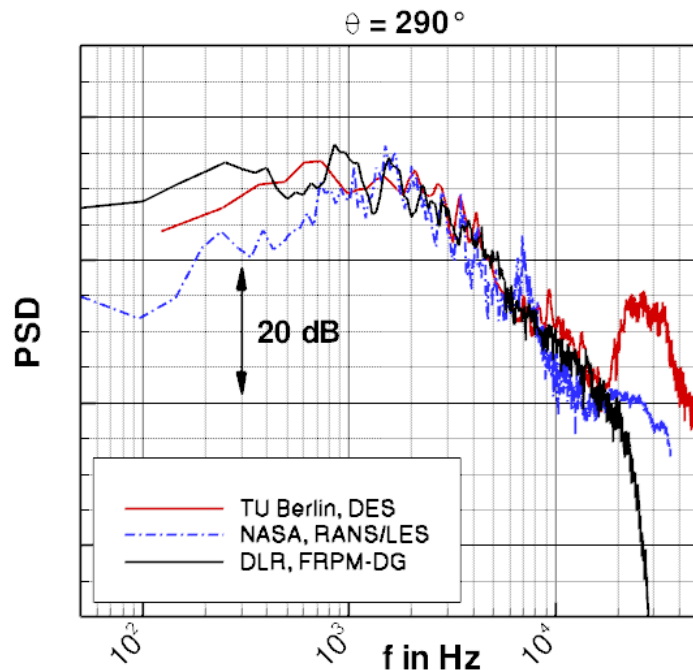
$Re = 1.7 \times 10^6$

$A = 4^\circ$

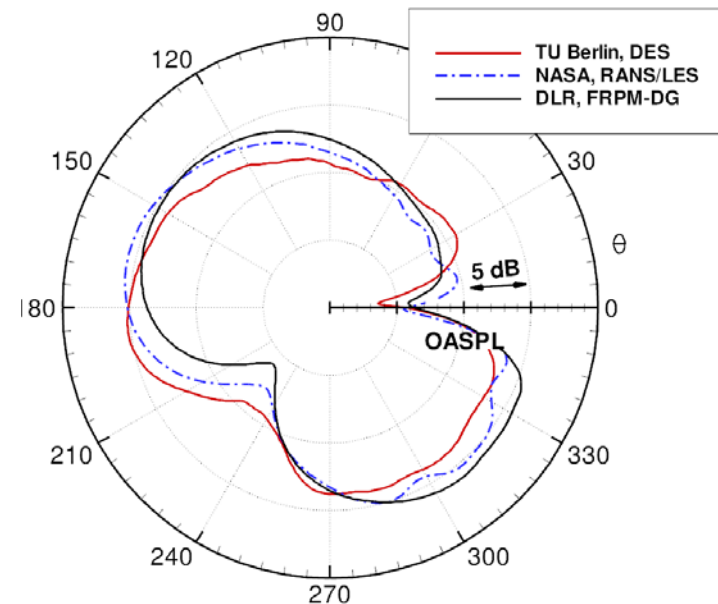
Sweep: 0°



MD (Boeing) 30P30N profile



good agreement between 1 and 10 kHz,
similar trend



good agreement, all approaches predict
minima under $\theta \approx 0^\circ$ and $\theta \approx 225^\circ$

- potential reasons for deviations: vortex shedding from blunt slat upper TE (TU Berlin)

Bauer 2012 & Dierke 2010, Aeronext (LuFo, German)



flow: TAU / sound: DISCO

Slat Noise Simulations

Efficiency of slat noise simulations, DGM vs. PIANO, single processor tests

- comparison of computation times DG Method (DISCO) $\Leftrightarrow$ FD Method (PIANO):
 - same settings in PIANO and DISCO:
 - 300.000 time steps, $dt = 1.0E-04 \rightarrow t_{end} = 30$
 - single 2.8 GHz processor, compilers: gfortran, Intel
 - grids: 653 776 points (PIANO), 587 740 nodes (DISCO)

PIANO-FRPM gfortran / intel	DISCO-FRPM, global dt	DISCO-FRPM, local dt	FRPM only
77h / 90h	59h	18h	9h



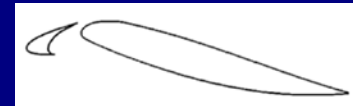
Uniform (global) time stepping Non-uniform time stepping

- **DG method practically as efficient as finite-difference method (PIANO)** on single processor

Bauer 2012

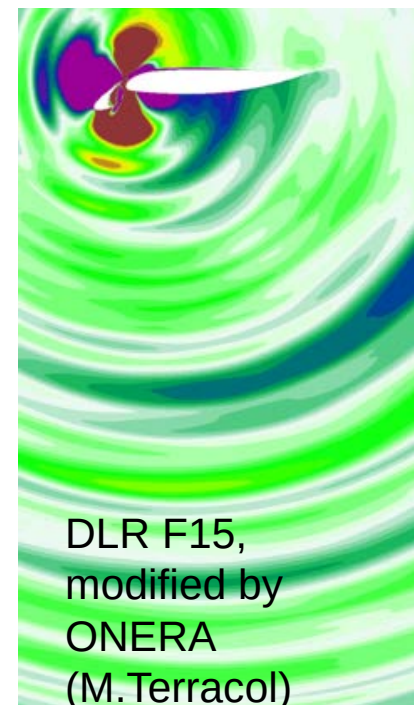
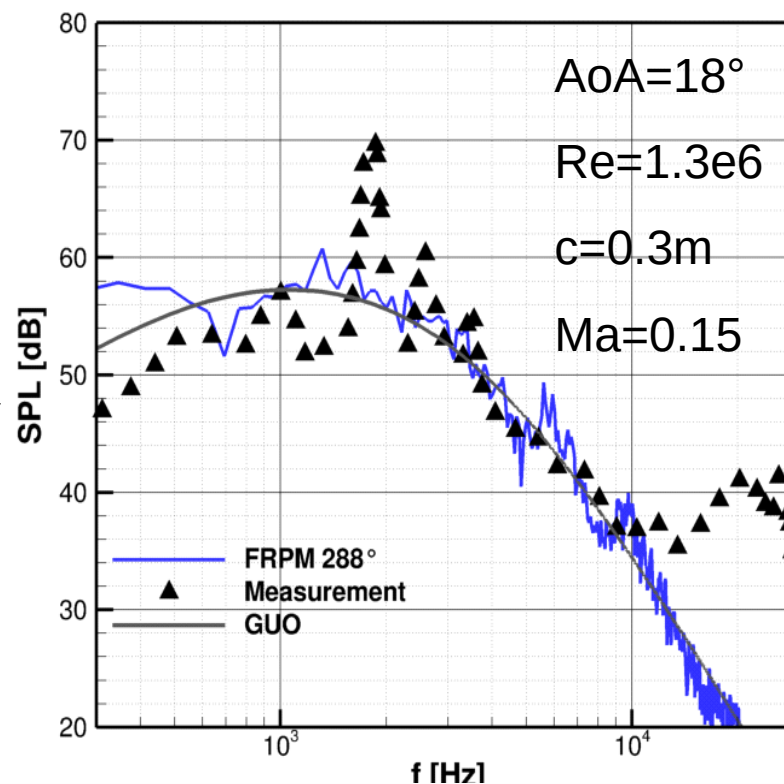


Slat Noise Simulations



Spectral results of stochastic results of slat case VALIANT vs. measurement*

- No tripping of high-lift model in experiments
- Experimental spectra show distinct tones
- BBN noise trends well captured
- But: tones not captured by BBN stochastic approach
- Characteristic slat noise spectrum of Guo (BBN) (black curve):



$$F(f, M) = \frac{M^2 c_s}{c_0} \frac{1}{(1 + \mu_0^2 St^2)(1 + \mu_1^2 (1 + M)^2 St^2)(1 + \mu_2^2 M^2 St^2)(1 + \mu_3 M St)}$$

$$\mu_1 = 0.26, \mu_2 = 1.0399, \mu_3 = 1.78 \text{ and } \mu_4 = 2.2.$$

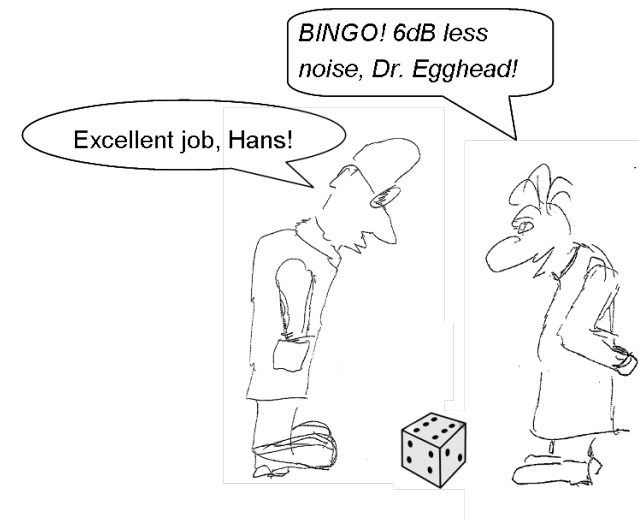


Summary and Conclusion

- Discussion of the different numerical approaches applied at DLR
- Surface integral methods based on FW-H integrals include simplified propagation physics
 - If not all parts of the airframe are entirely wrapped-up -> BEM Problem
 - Efficient realization (general simulation capability) for realistic airframe sizes and interesting frequencies via Fast Multipole BEM
 - Non-uniform flow effects sometimes important -> volume resolving CAA methods necessary for resolving them
- DNC simulation capability based on DRP scheme and NLPE formulation currently implemented and tested
- Design (fast prediction) methods implemented based on linear perturbation equations (APE) plus stochastic sound sources
- For high-lift systems gives qualitatively good prediction of broadband spectra comparable with measurements and scale resolving simulation
- Stochastic tools provide only broadband part of spectra (no tones)
- DGM promising tool for acoustic propagation purposes based on linear governing equations



Thank you for your attention!



Thank you for your attention!

